



Alert Geomaterials



# Advanced multiphysics of geomaterials: multiscale approaches and heterogeneities

ALERT OZ / EURAD GAS & HITEC Summer School  
28 August – 01 September 2023 • Liège (Belgium)

Pierre BÉSUELLE, Frédéric COLLIN,  
Anne-Catherine DIEUDONNÉ, Sebastia OLIVELLA



*The project leading to this application has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement n° 847593.*



Alert Geomaterials



# Advanced multiphysics of geomaterials: Multiscale modelling of gas flow

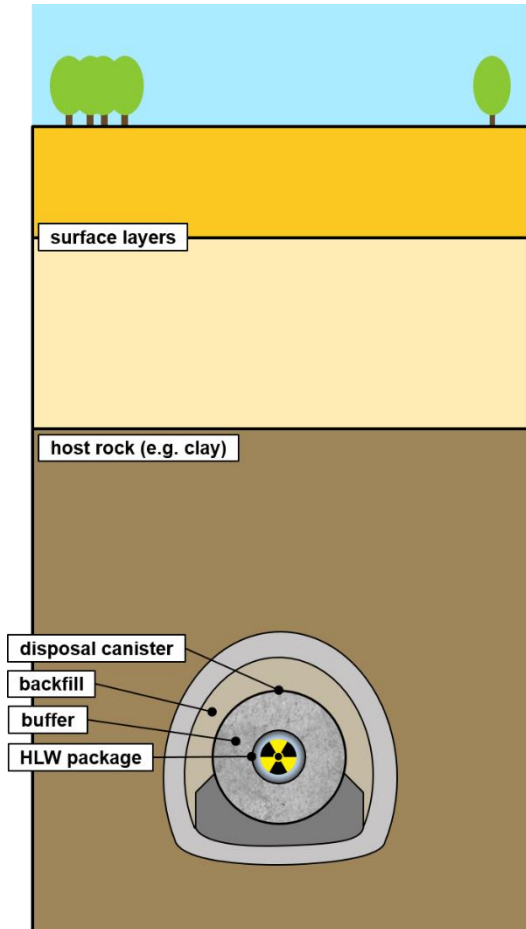
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Gilles Corman, Frédéric COLLIN



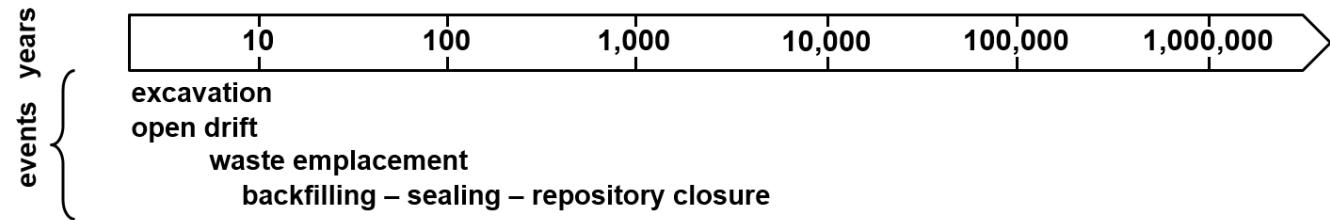
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# Context

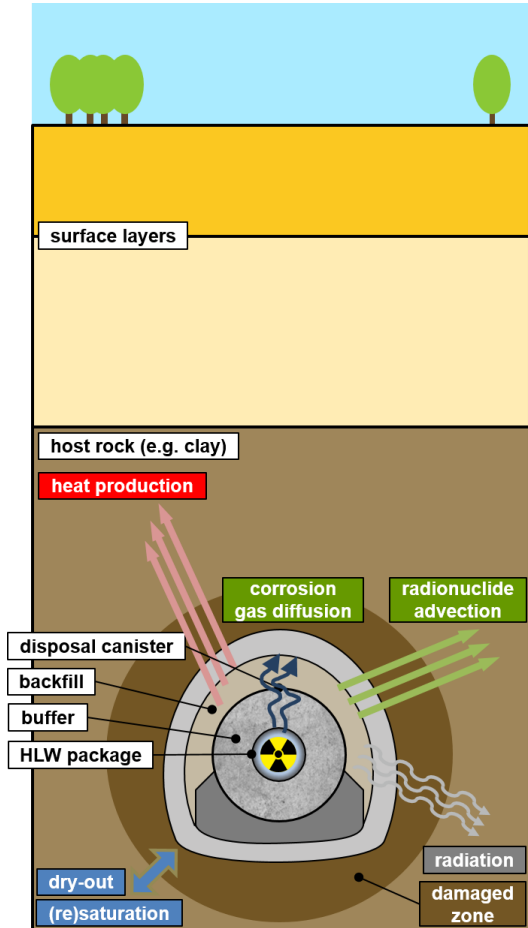


Conceptual scheme of a deep geological repository.

## Geological disposal of radioactive wastes



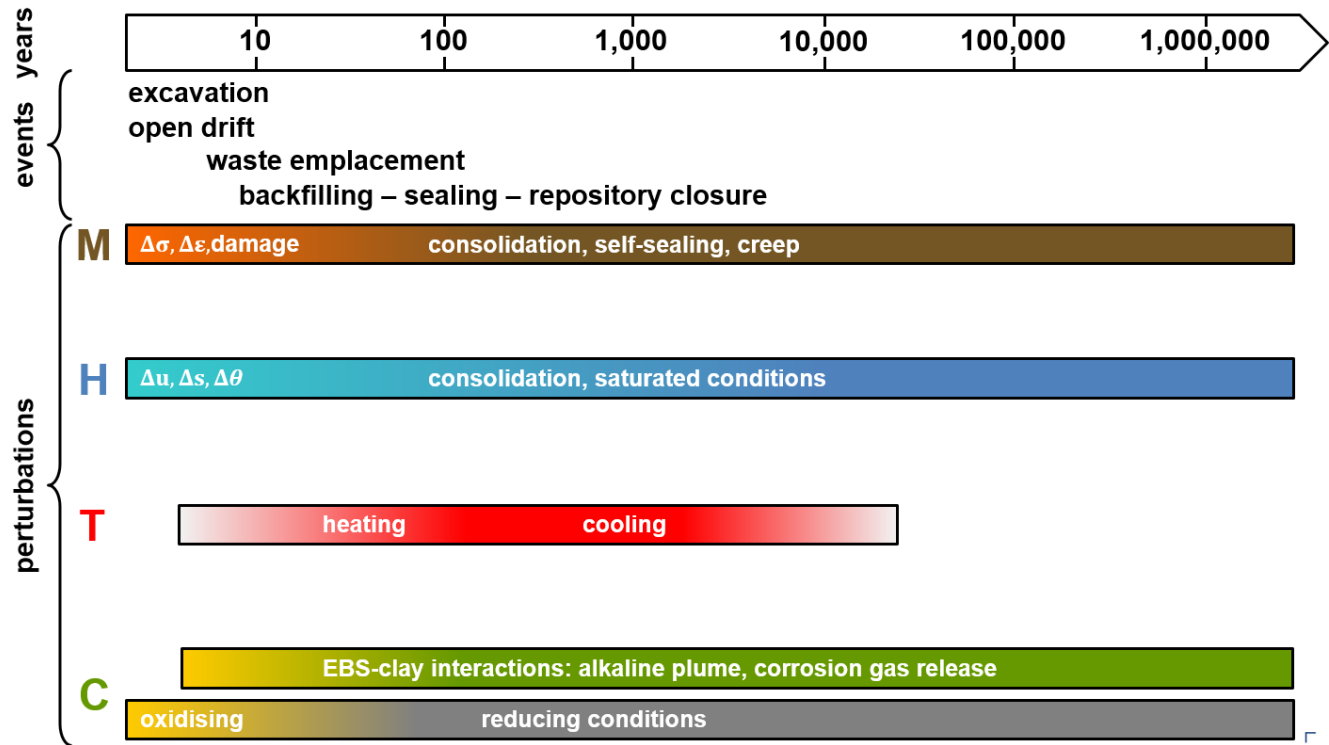
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Conceptual scheme of a deep geological repository.

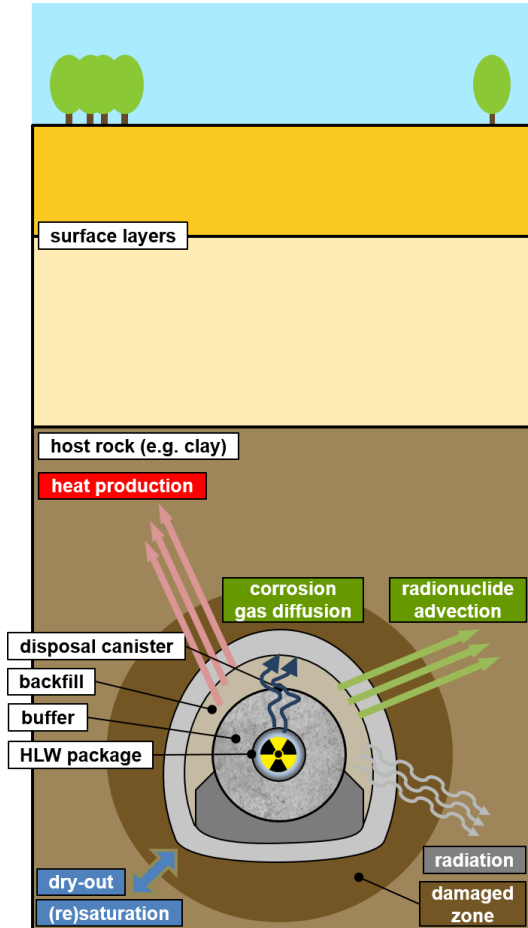
## Geological disposal of radioactive wastes

- ▶ Complex multi-physical (THMC) processes



Major perturbations of the host rock over the lifetime of a geological repository, adapted from *Sillen (2012)*.

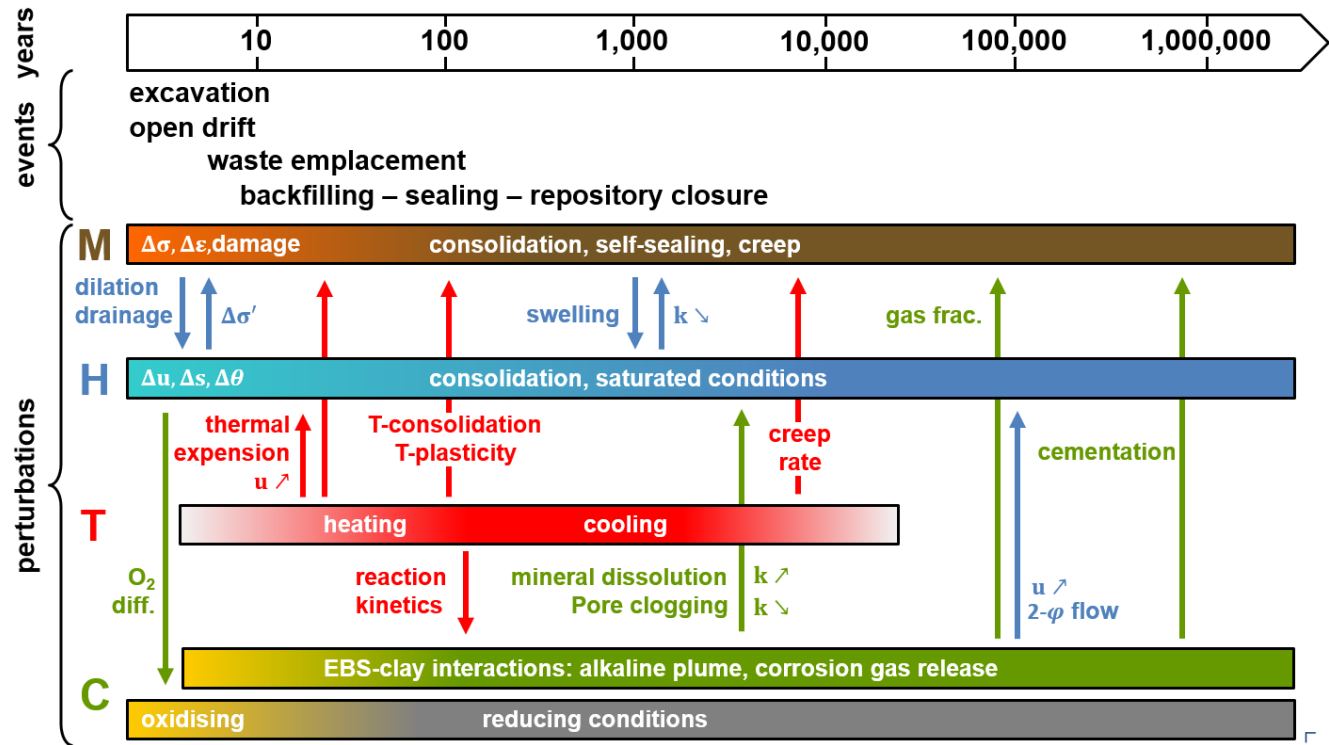
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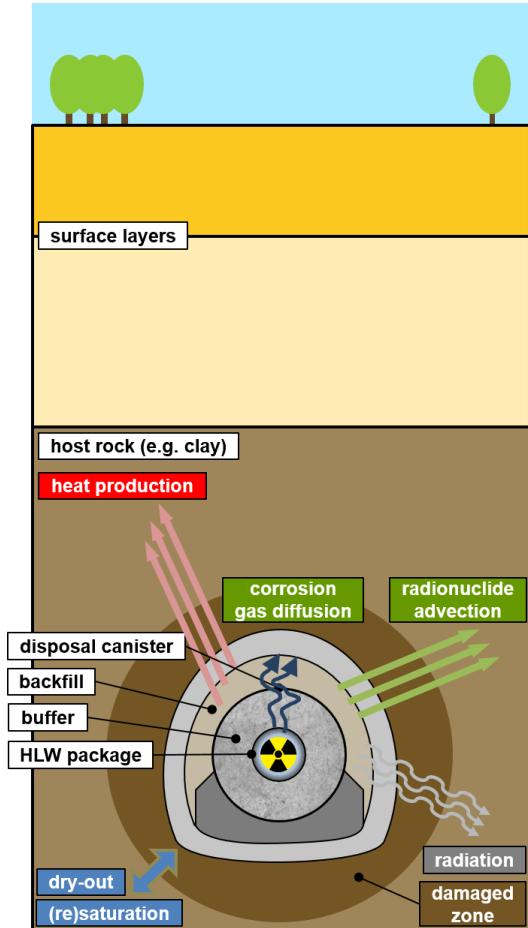
## Geological disposal of radioactive wastes

- ▶ Complex multi-physical (THMC) processes
- ▶ Interactions between processes



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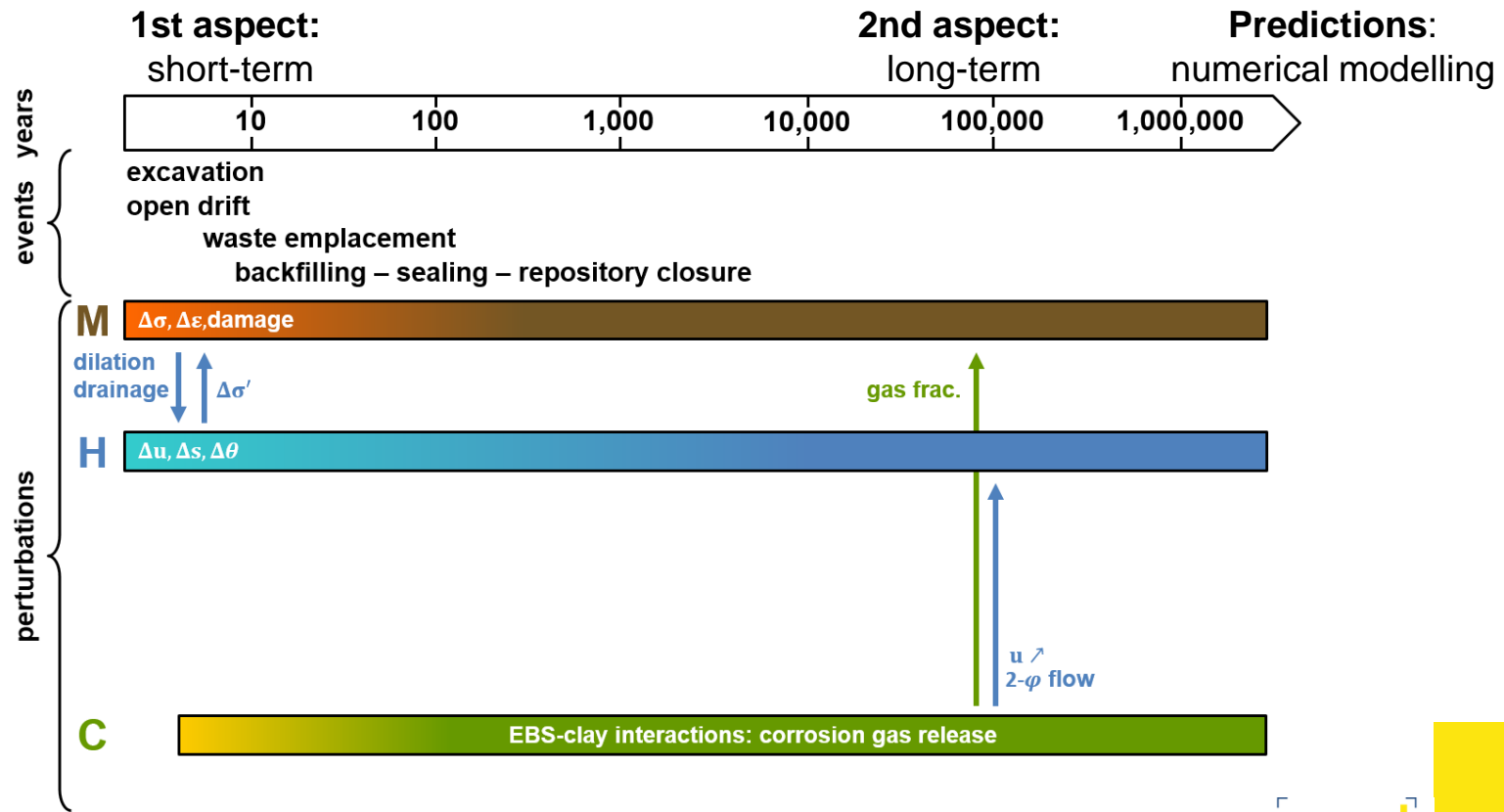
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Conceptual scheme of a deep geological repository.

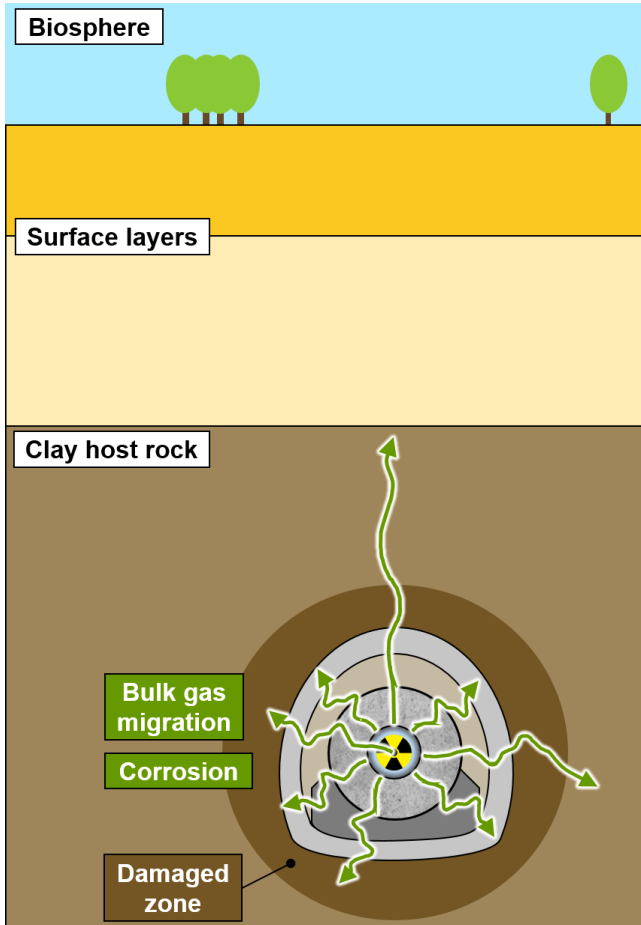
## Geological disposal of radioactive wastes

- ▶ Complex multi-physical (THMC) processes
- ▶ Interactions between processes



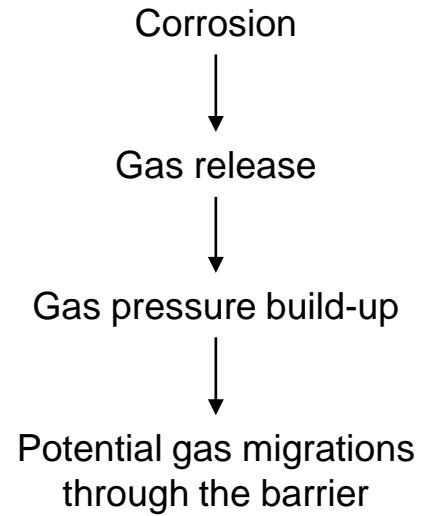
Major perturbations of the host rock over the lifetime of a geological repository, adapted from *Sillen (2012)*.

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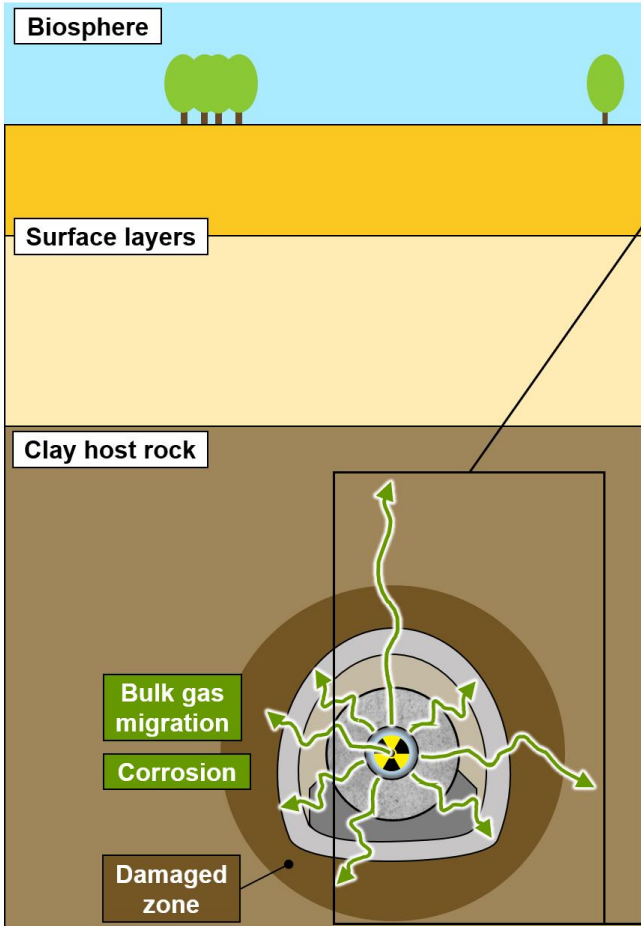


Conceptual scheme of a deep geological repository focussing on the gas generation process.

## Gas migration issue

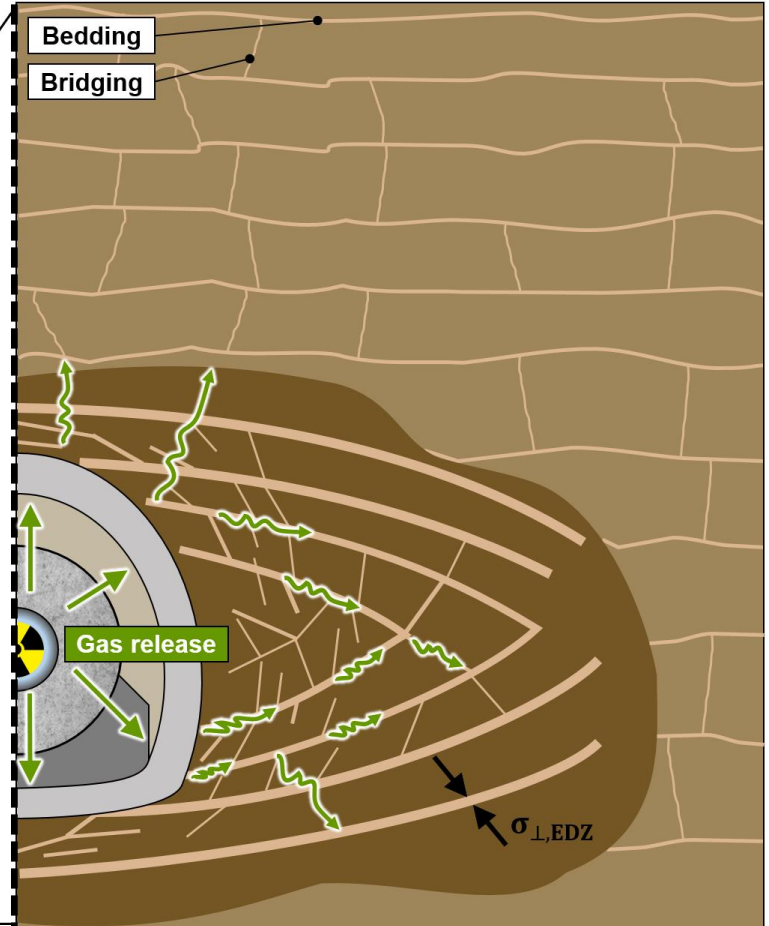


# Context



Conceptual scheme of a deep geological repository focussing on the gas generation process.

## Gas migration issue



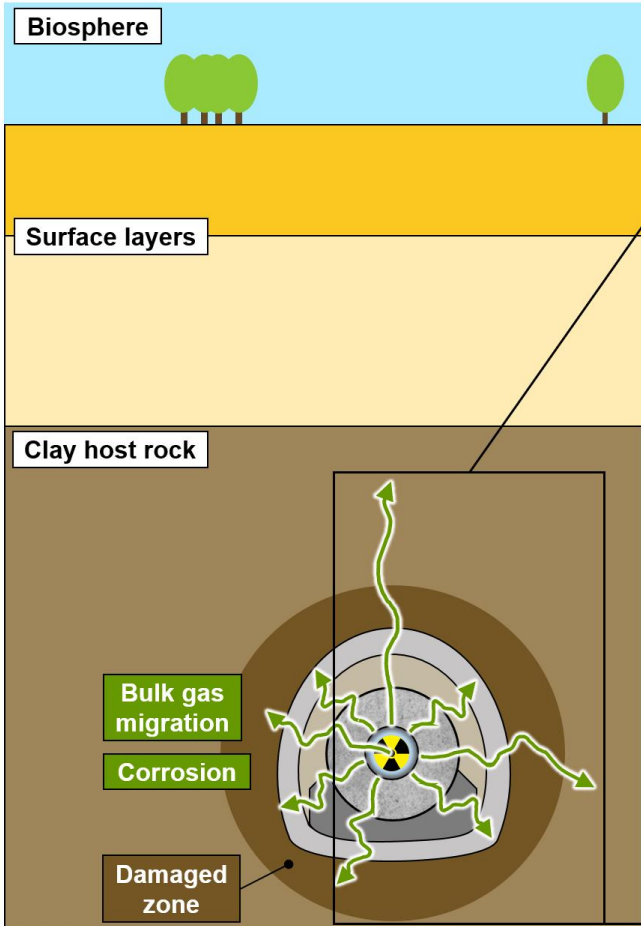
Expected gas transport modes in the EDZ and the sound rock, from ONDRAF/NIRAS (2016).

### Excavation damaged zone (EDZ)

- Governed by the hydraulic properties modifications induced by fracturation

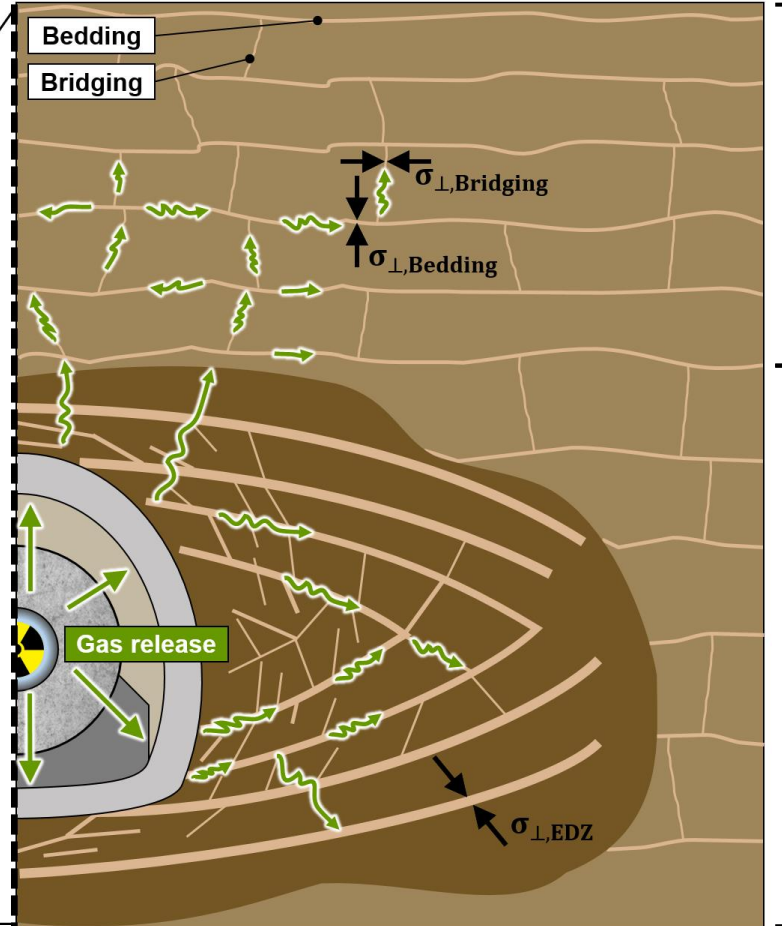


# Context



Conceptual scheme of a deep geological repository focussing on the gas generation process.

## Gas migration issue



Expected gas transport modes in the EDZ and the sound rock, from ONDRAF/NIRAS (2016).

### Sound rock layers

- ▶ Governed by the rock structure at a micro-level
- ▶ Multi-Scale Model

### Excavation damaged zone (EDZ)

- ▶ Governed by the hydraulic properties modifications induced by fracturation

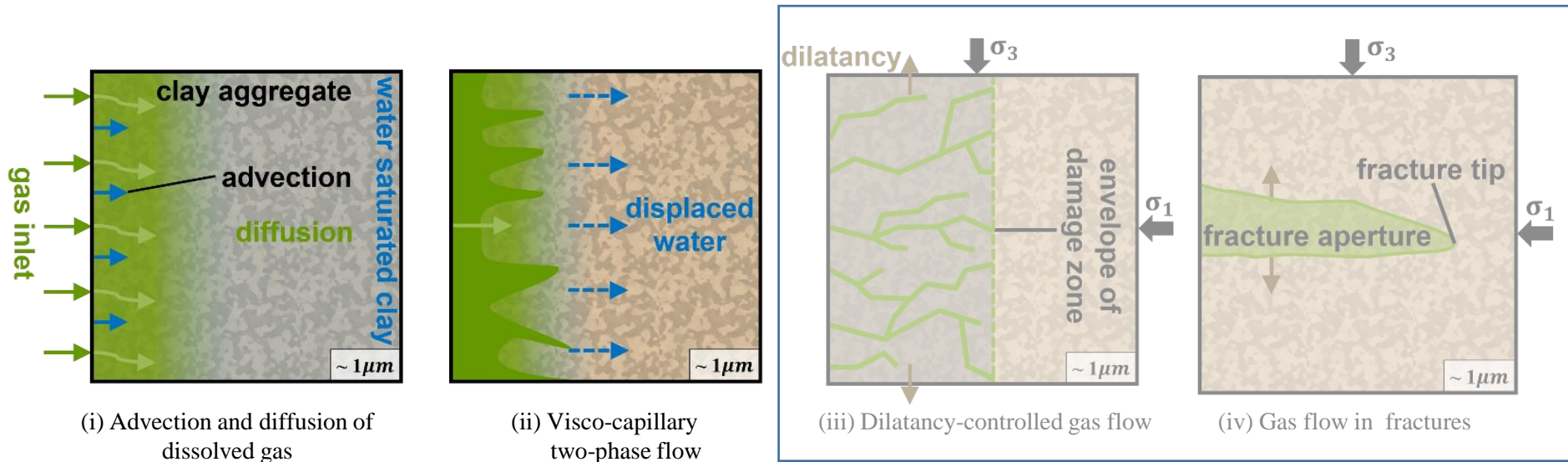


# Content

- ① Context
- ② From experimental evidence to modelling
- ③ Multi-scale modelling approach
- ④ Preliminary modelling
- ⑤ Modelling gas injection experiment
- ⑥ Conclusions

# From experimental evidence to modelling

## Background

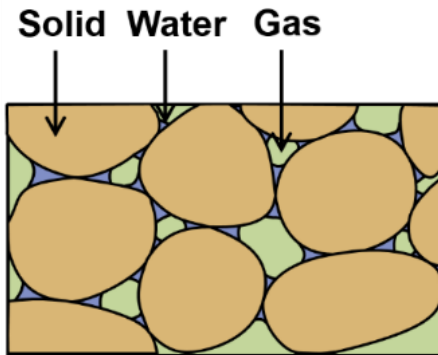


Phenomenological description of the gas transport processes relevant to low-permeable clayey rocks, adapted from Marschall et al. (2005).

Classical HM two-phase flow models

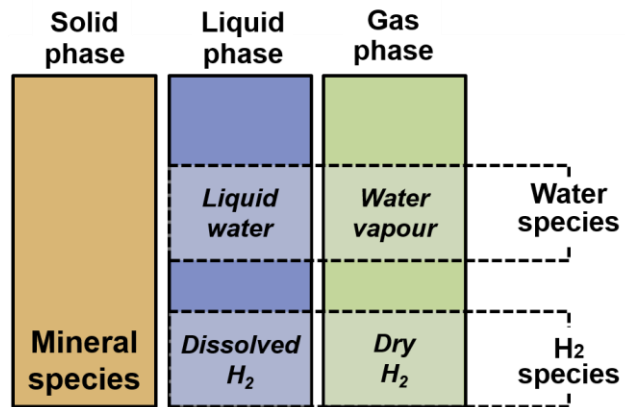
# From experimental evidence to modelling

## Classical HM two-phase flow models



Triphasic porous medium

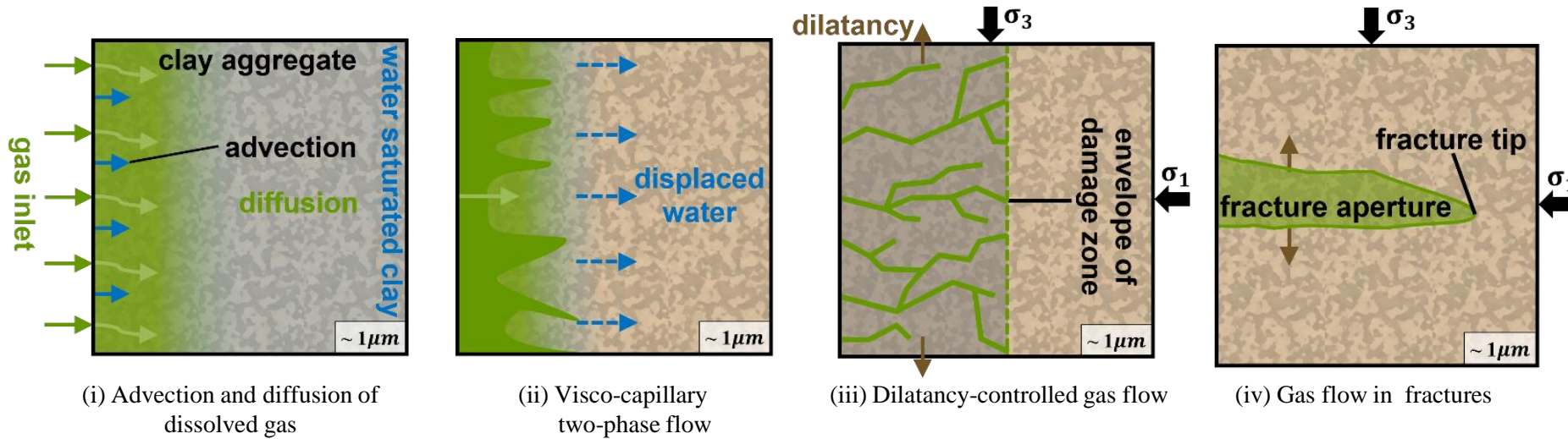
Bright, Aster, Lagamine, OpenGEOSys, Though2/3



Phases and species

# From experimental evidence to modelling

## Background



Phenomenological description of the gas transport processes relevant to low-permeable clayey rocks, adapted from Marschall et al. (2005).

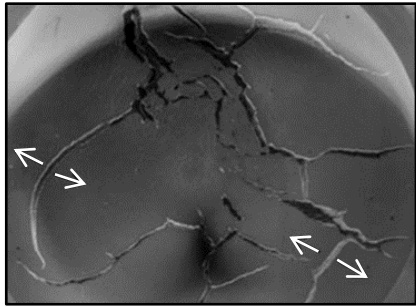
Classical HM two-phase flow models

Supported by experimental data

# From experimental evidence to modelling

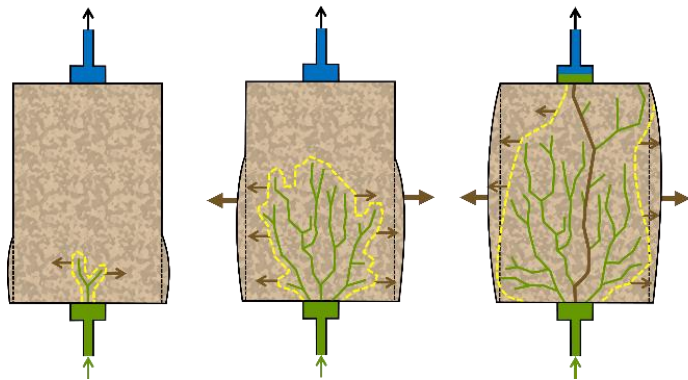
## Laboratory experiments

### Clay-rich material



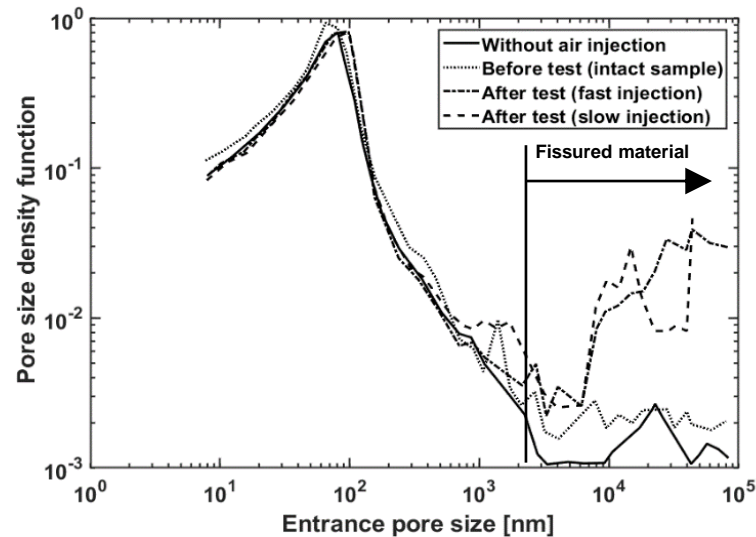
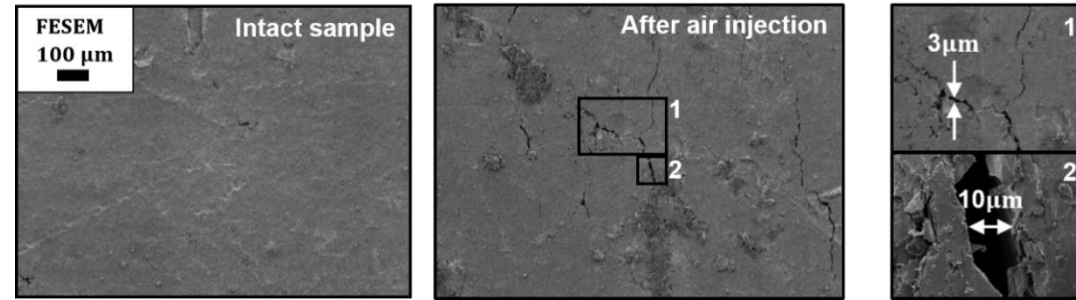
Gas-induced fracturing, *Wiseall et al. (2015)*

### Callovo-Oxfordian claystone



Onset of gas flow, modified after *Cuss et al. (2014)*

### Boom Clay

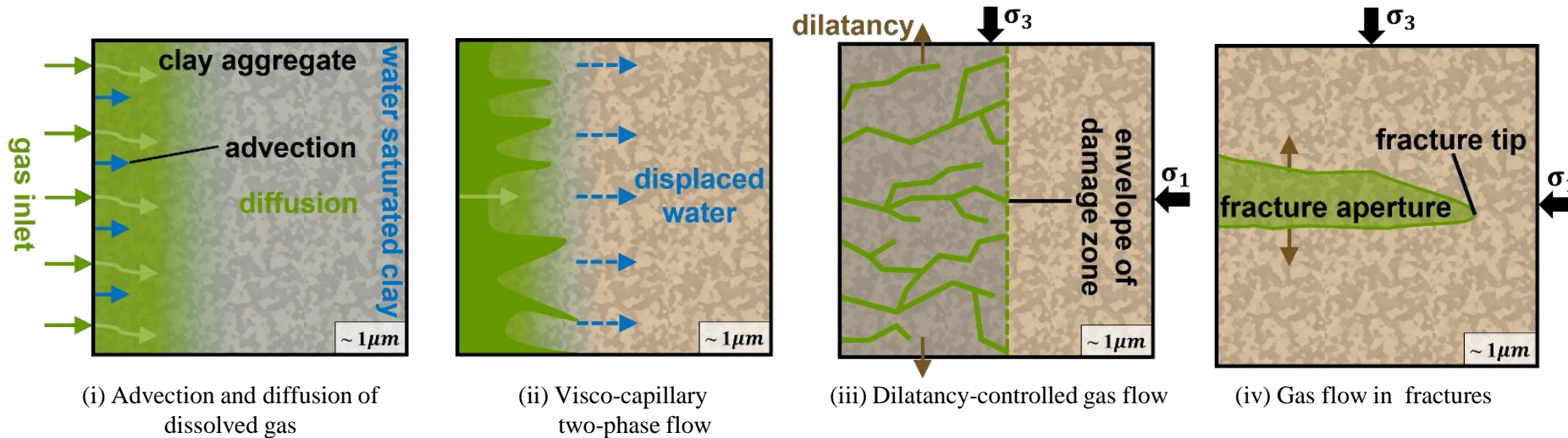


Changes in Boom Clay pore size distribution after air injection, and corresponding FESEM images with zooms on the detected fissures, modified after *Gonzalez-Blanco et al. (2022)*



# From experimental evidence to modelling

## Background



Phenomenological description of the gas transport processes relevant to low-permeable clayey rocks, adapted from Marschall et al. (2005).

## Classical HM two-phase flow models

## Supported by experimental data

- Natural heterogeneities represent preferred weaknesses for the process of opening discrete gas-filled pathway
- Introduce stronger coupling between gas flow and mechanical behaviour into the models.

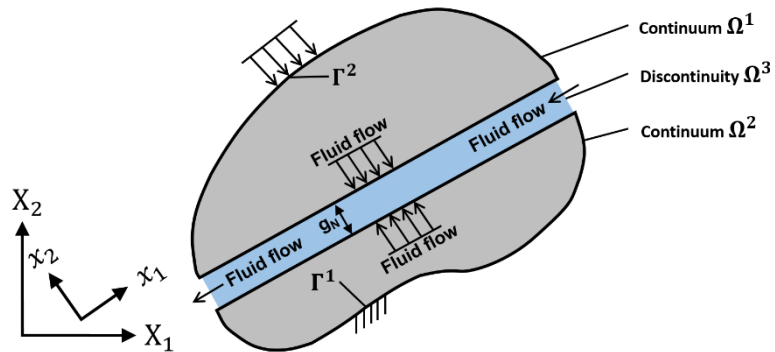
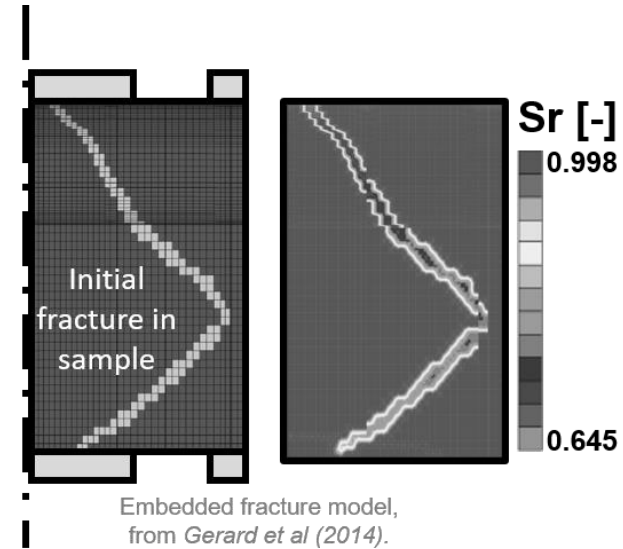
## ► Advanced HM models

# From experimental evidence to modelling

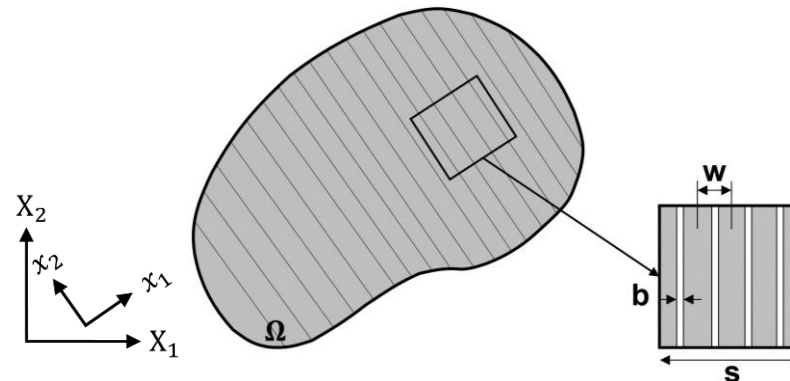
## Advanced HM models

### Macroscopic models

- ▶ No direct representation of local phenomena
- ▶ Enriched with micromechanical effects
- ▶ Examples:
  - Natural heterogeneity based models Olivella and Alonso (2008)
  - Intrinsic permeability based models Pardoen et al. (2016)
  - Embedded fracture models Alonso et al. (2006)
  - Explicit fracture based models Cerfontaine et al. (2015)



Conceptual scheme of the explicit fracture based model, after Cerfontaine et al. (2015)



Conceptual scheme of the embedded fracture model, after Olivella et al. (2008)

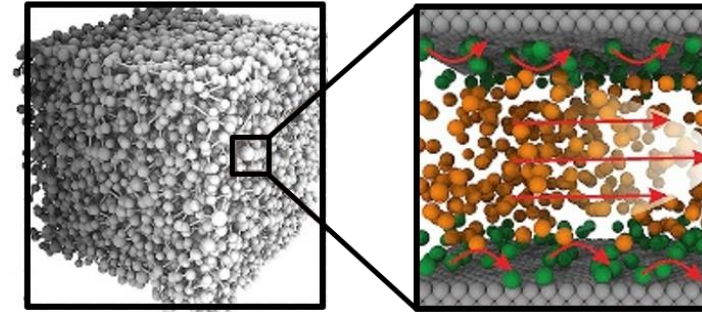


# From experimental evidence to modelling

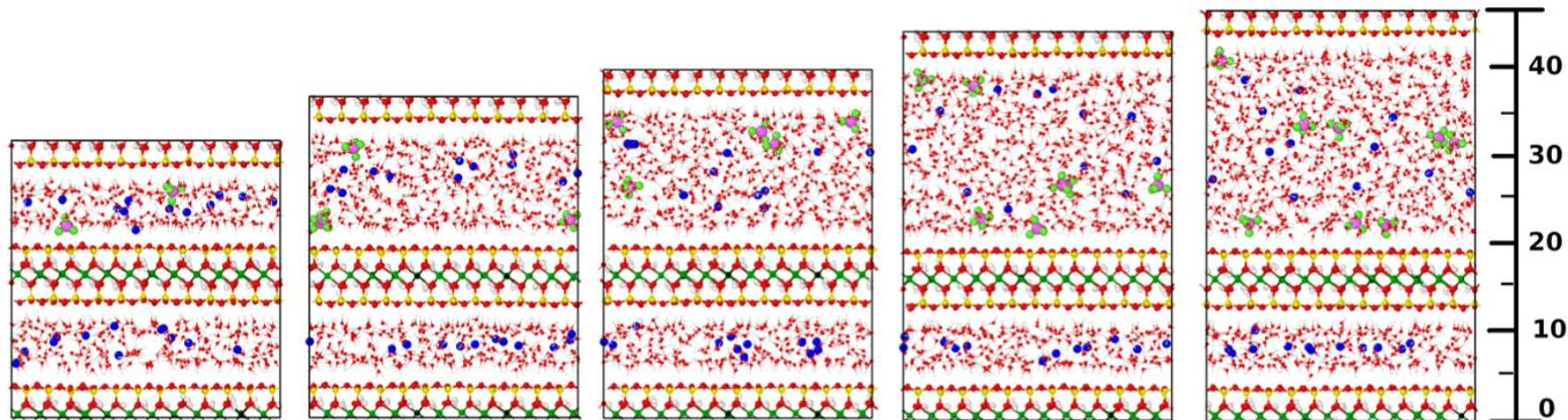
## Advanced HM models

### Microscopic models

- ▶ Direct modelling of all the microstructure complexity at very low scale
- ▶ Useful for modelling at the process scale
- ▶ High computational expense at the scale of a repository



From pore network to molecular model, from *Yu et al. (2019)*.



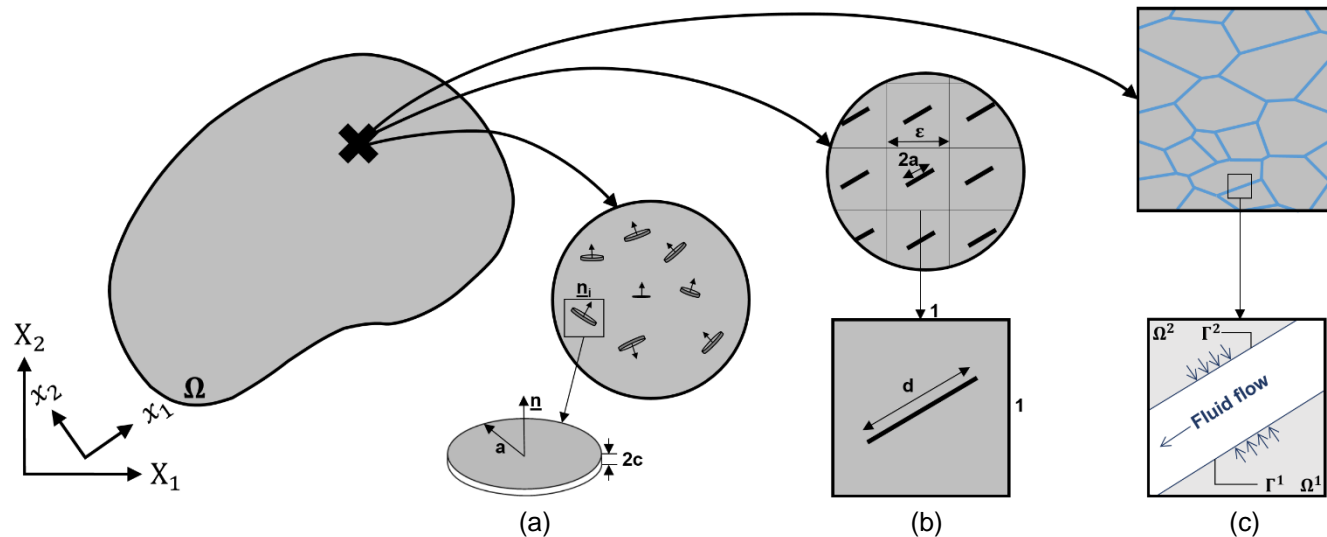
Study of the the physico-chemical properties of dissolved gases in several configurations of a hydrated clay system, from *Owusu et al. (2022)*.

# From experimental evidence to modelling

## Advanced HM models

### Micro-macro based models

- ▶ Combines the benefits from large- and small-scale modelling strategies
- ▶ Explicit description of all the constituents on their specific length scale through a REV definition



Conceptual scheme of micro-macro based models, with microstructure definitions of a microcracked material, after (a) Levasseur (2013), (b) François (2010), and (c) van den Eijnden (2016).



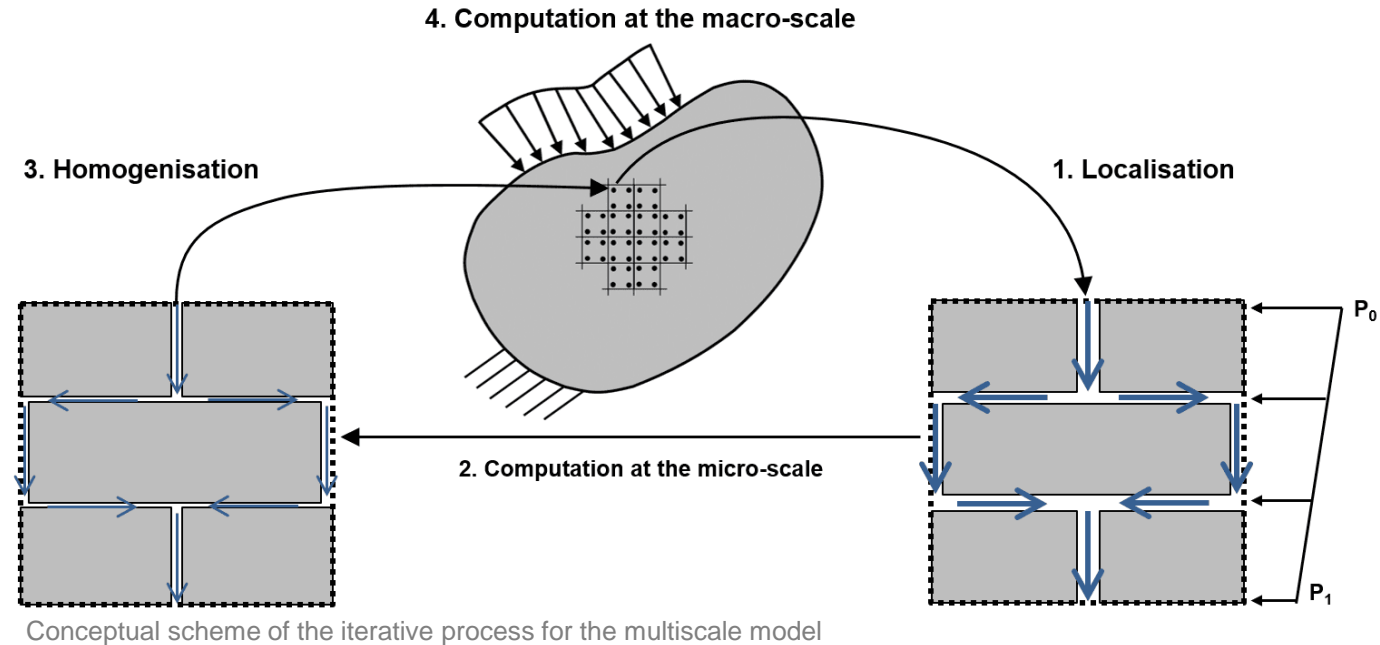
# Content

- ① Context
- ② From experimental evidence to modelling
- ③ Multi-scale modelling approach
- ④ Preliminary modelling
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- ⑥ Conclusions

# Multi-scale modelling approach

## Overview

- Macro-to-micro scale transition: Localisation of the macro-scale deformations to the micro-scale
- Resolution of the boundary value problem at the micro-scale
- Micro-to-macro scale transition: Homogenisation of the micro-scale stresses to compute the macroscopic quantities
- Resolution of the boundary value problem at the macro-scale



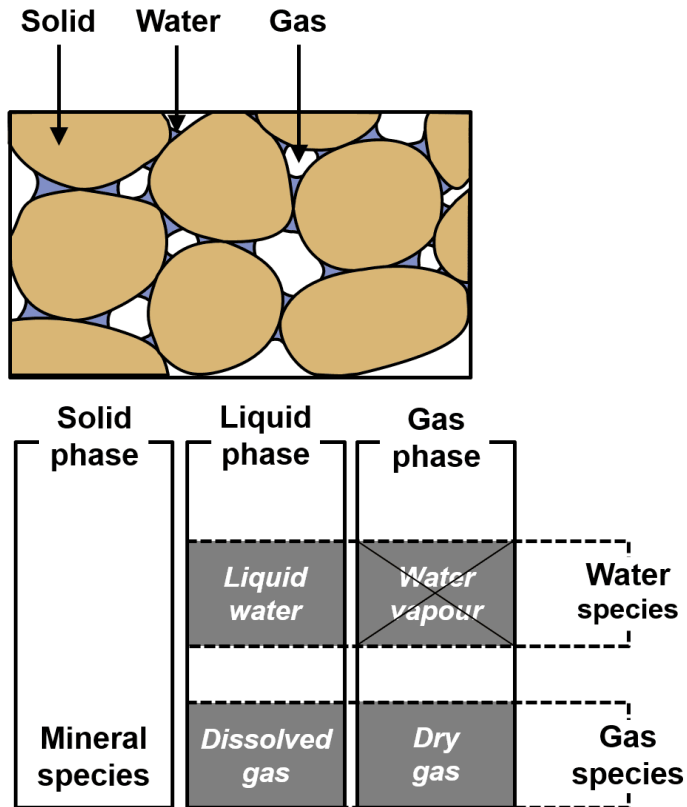
## Hybrid developed tool

- Complete hydraulic system implemented and solved at the micro-scale
- Mechanical effects addressed at the macro-scale and implicitly integrated at the lower scale through HM couplings

# Multi-scale modelling approach

## Model formulation at the macroscopic scale

Clay material treated as a porous medium



Unsaturated triphasic porous medium and definition of phases and species

Balance equations

- Momentum

$$\frac{\partial \sigma_{ij}}{\partial x_j} + \rho g_i = 0$$

- Water

$$\underbrace{\dot{M}_w + \frac{\partial f_{w,i}}{\partial x_i}}_{\text{Liquid water}} - Q_w = 0$$

- Gas

$$\underbrace{\dot{M}_g + \frac{\partial f_{g,i}}{\partial x_i}}_{\text{Dry gas}} + \underbrace{\dot{M}_{dg} + \frac{\partial f_{dg,i}}{\partial x_i}}_{\text{Dissolved gas}} - Q_g = 0$$

Constitutive equations

- Total stress definition

$$\sigma_{ij} = \sigma'_{ij} + b_{ij} \left[ S_{r_w} p_w^M + (1 - S_{r_w}) p_g^M \right] \delta_{ij}$$

- Variation of solid density

$$\frac{\dot{\rho}_s}{\rho_s} = \frac{(b_{ij} - \phi)(S_r^w \dot{p}_w + S_r^g \dot{p}_g) + \dot{\sigma}'}{(1 - \phi)K_s}$$

# Multi-scale modelling approach

## Macro-to-micro scale transition: Localisation

Decomposition of the micro-kinematics:

- Macro-pressure fields ( $\square^M$ ) of water and gas must be identical to the micro-quantities ( $\square^m$ ) for any point of the material

$$p_w^M(\hat{P}) = p_w^m(\hat{P})$$

$$p_g^M(\hat{P}) = p_g^m(\hat{P})$$

- For any point  $P$  close to  $\hat{P}$ , at the macroscopic scale:

$$p_w^M(P) \approx p_w^M(\hat{P}) + \frac{\partial p_w^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j) \quad p_g^M(P) \approx p_g^M(\hat{P}) + \frac{\partial p_g^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j)$$

Higher-order terms neglected

at the microscopic scale:

$$p_w^m(P) \approx p_w^M(\hat{P}) + \frac{\partial p_w^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j) + p_w^f(\hat{P}) \quad p_g^m(P) \approx p_g^M(\hat{P}) + \frac{\partial p_g^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j) + p_g^f(\hat{P})$$

Fluctuation fields to replace higher-order terms

Separation of scales

- Approach restricted to situations where the variations of the macroscopic fields is large compared to the variations of micro-scale fields

$$\frac{\partial p_w^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j) + p_w^f(\hat{P}) \ll p_w^M(\hat{P})$$

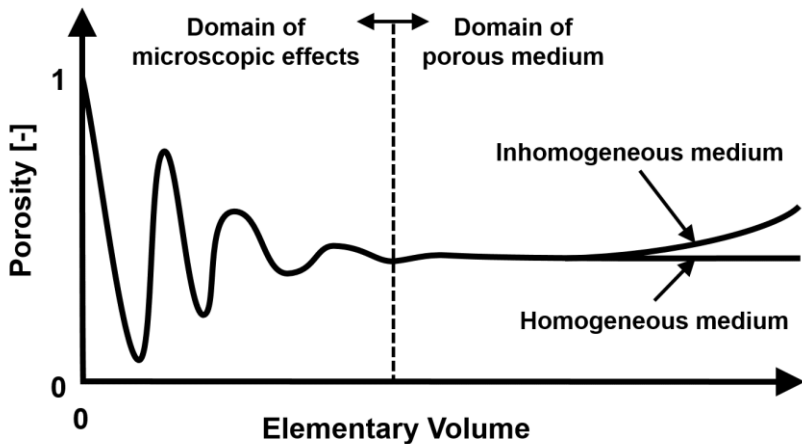
$$\frac{\partial p_g^M(\hat{P})}{\partial x_j} (x_j - \hat{x}_j) + p_g^f(\hat{P}) \ll p_g^M(\hat{P})$$

# Multi-scale modelling approach

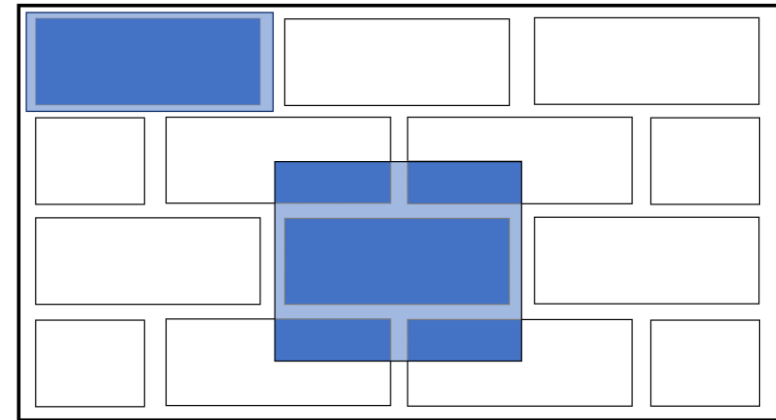
## Micro-scale boundary value problem

REV generation in general

- Representative of the microstructure
  - Large enough to represent the microstructure
  - Small enough to satisfy the principle of scale separation
- Spatial repetition of a very small part of the whole microstructure
  - Relevant statistical representation of any random part of the micro-scale
  - Not a unique choice



Representativeness of an elementary volume applied to the concept of porosity, *Bear (1972)*.



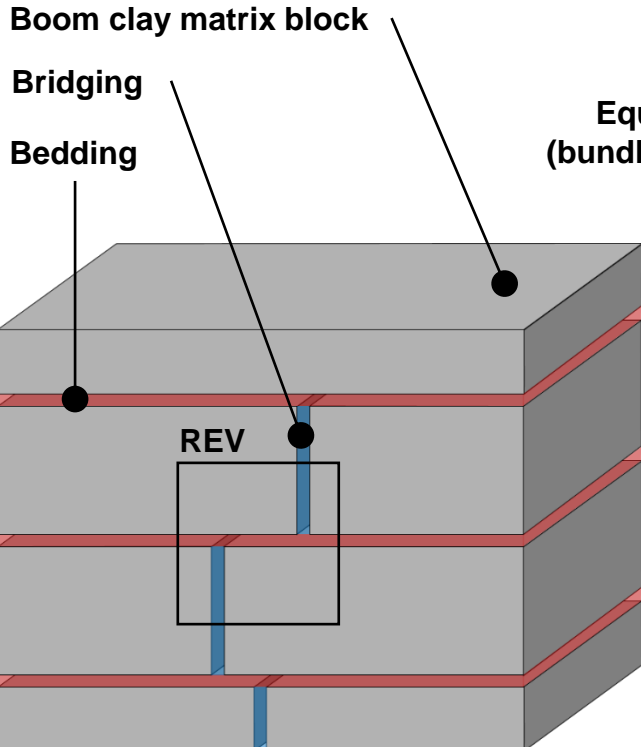
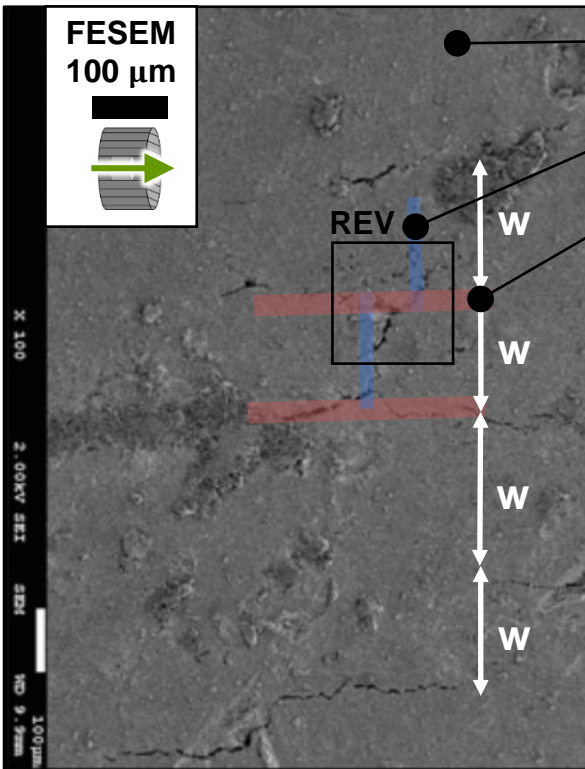
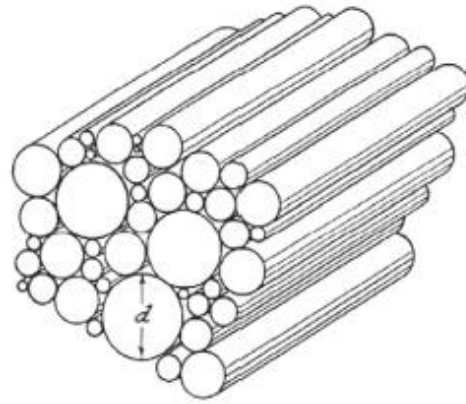
Examples of two rectangular unit cells, *Anthoine (1995)*



# Multi-scale modelling

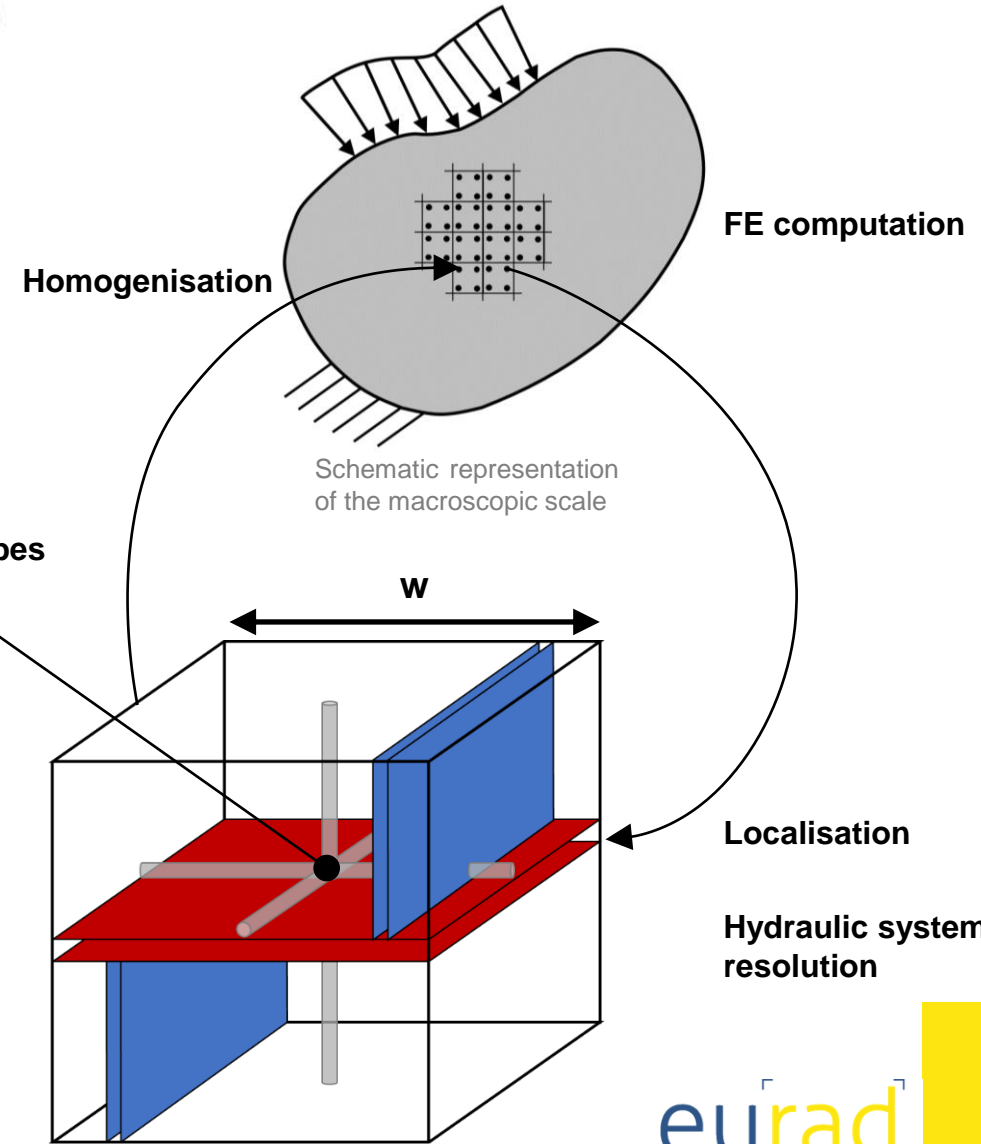
## Micro-scale boundary value problem

Multi-scale model supported by experimental data



Internal visualisation of a Boom Clay sample using FESEM, from Gonzalez-Blanco (2017).

Physical idealisation of the microstructure.



Homogenisation

FE computation

Schematic representation of the macroscopic scale

Equivalent (bundle of) tubes

Localisation

Hydraulic system resolution

Definition of the representative element volume (REV)



# Multi-scale modelling approach

## Micro-scale boundary value problem

Balance equations at the micro-scale

- Gas

$$\cancel{\rho_g} + \frac{\partial f_{g_i}^m}{\partial x_i} + \cancel{\rho_g} + \frac{\partial f_{dg_i}^m}{\partial x_i} = 0$$

- Water

$$\cancel{\rho_w} + \frac{\partial f_{w_i}^m}{\partial x_i} = 0$$

$\dot{M}_g^m \quad \dot{M}_{dg}^m \quad \dot{M}_w^m$  Variations of fluid contents

$$f_{w_i}^m = \rho_w q_{w_i}$$

$$f_{g_i}^m = \rho_g q_{g_i} \quad \text{Mass flows}$$

$$f_{dg_i}^m = \rho_{dg} q_{w_i} + i_{dg_i}$$

- Mechanical effects: computed at the macro-scale and transferred to the micro-scale through HM couplings

# Multi-scale modelling approach

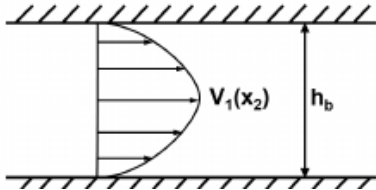
## Micro-scale boundary value problem

Constitutive equations: Hydraulic problem considering a channel flow model (Navier-Stokes equations)

- Advective component:

$$q_{\alpha_i} = -\frac{k_{r\alpha}}{\mu_\alpha} \frac{1}{A} \kappa_{frac} \frac{\partial p_\alpha}{\partial x_i} = -\frac{k_{r\alpha}}{\mu_\alpha} \frac{h_b^3}{12w} \frac{\partial p_\alpha}{\partial x_i}$$

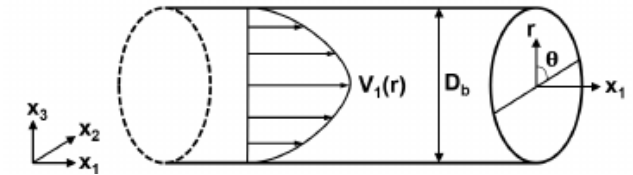
$$q_{\alpha_i} = -\frac{k_{r\alpha}}{\mu_\alpha} \frac{1}{A} \kappa_{tube} \frac{\partial p}{\partial x_i} = -\frac{k_{r\alpha}}{\mu_\alpha} \pi \frac{D^4}{128w^2} \frac{\partial p}{\partial x_i}$$



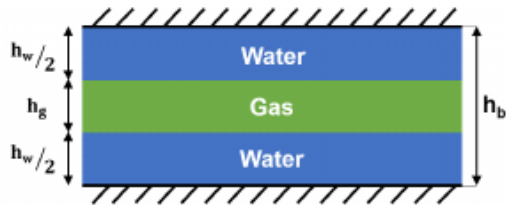
Laminar fluid flow profiles between two parallel plates

$$\kappa_{frac} = -\frac{h_b^2}{12} h_b \cdot w$$

$$\kappa_{tube} = -\pi \frac{D^4}{128}$$



Laminar fluid flow profiles in a circular pipe



Gas flow in between of water flows in a fracture space

$$k_{r_w} = \frac{S_r^2}{2} (3 - S_r)$$

$$k_{r_g} = (1 - S_r)^3$$

$$k_{r_w} = S_r^2$$

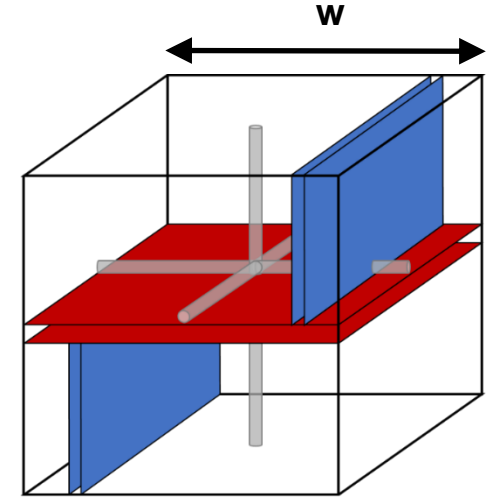
$$k_{r_g} = (1 - S_r)^2$$



Gas flow in between of water flows in a circular pipe

- Diffusive component

$$i_{dgi} = -S_{r_w} \bar{\tau} D_{dg/w} \rho_w \frac{\partial}{\partial x_i} \left( \frac{\rho_{dg}}{\rho_w} \right)$$



# Multi-scale modelling approach

## Micro-scale boundary value problem

Constitutive equations: Hydro-mechanical couplings

- Stress-dependent evolution of micro-elements aperture

$$\Delta\sigma' = K_n \Delta h$$

$$K_n = \frac{K_n^0}{\left(1 + \frac{\Delta h}{h_0}\right)^2}$$

$$\Delta\sigma' = K \Delta D_b$$

$$K = \frac{2G}{D_0}$$

- Stress-dependent formulation of the transmissivity and the entry pressure of micro-elements

$$\kappa_{frac} = -\frac{h_b^2}{12} h_b \cdot w$$

$$p_e = p_{e0} \left(\frac{h_{b0}}{h_b}\right)^m$$

$$p_{e0} = \frac{2\sigma_{GL}\cos\theta}{h_b}$$

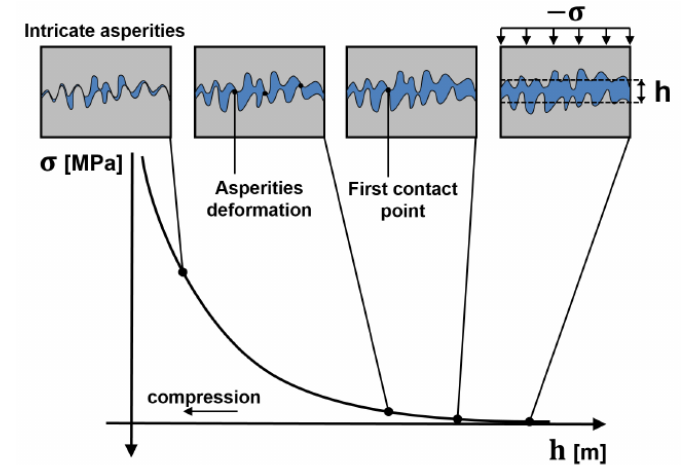
$$h_b = h_0 + h$$

$$\kappa_{tube} = -\pi \frac{D^4}{128}$$

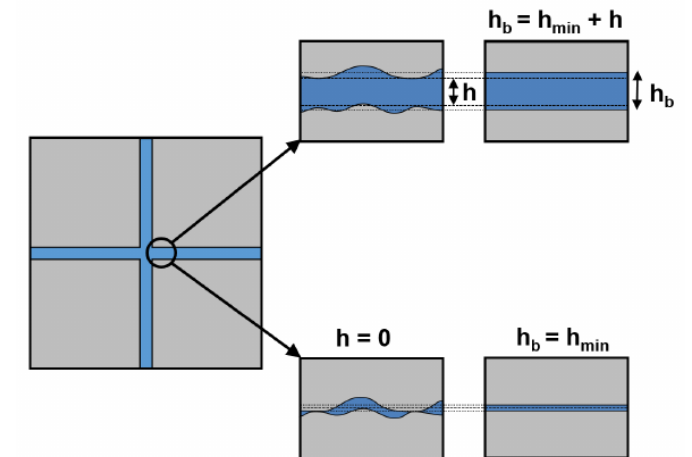
$$p_e = p_{e0} \left(\frac{D_{b0}}{D_b}\right)^m$$

$$p_{e0} = \frac{2\sigma_{GL}\cos\theta}{D_b/2}$$

$$D_b = D_0 + D$$



Constitutive law describing the normal behaviour of a rough rock joint, *Cerfontaine (2015)*



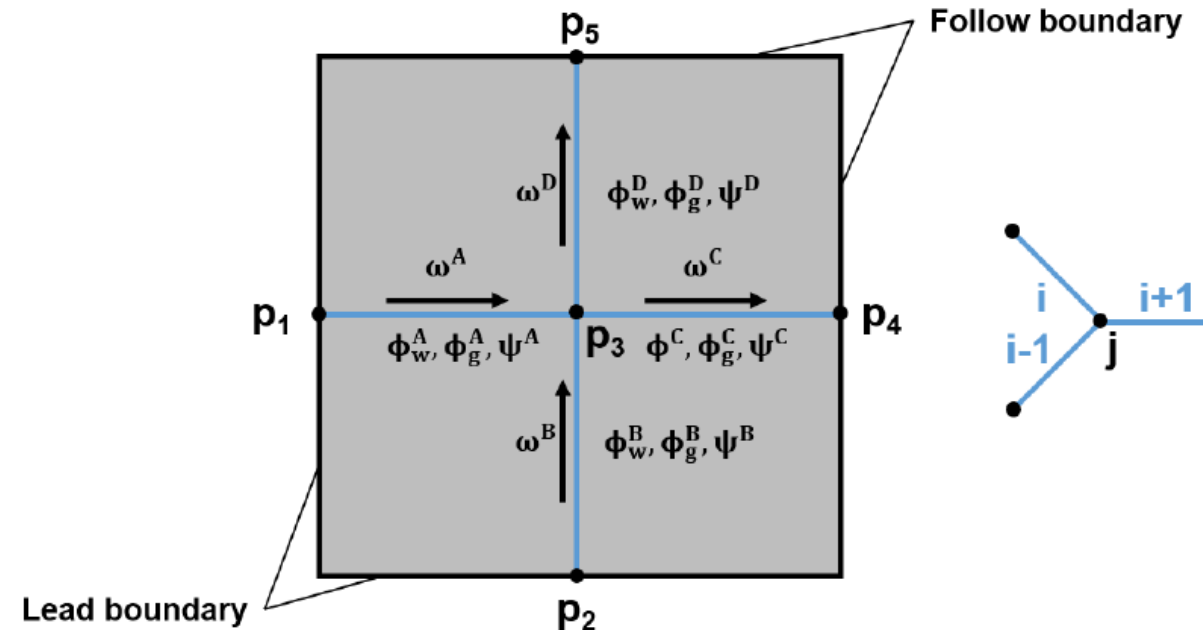
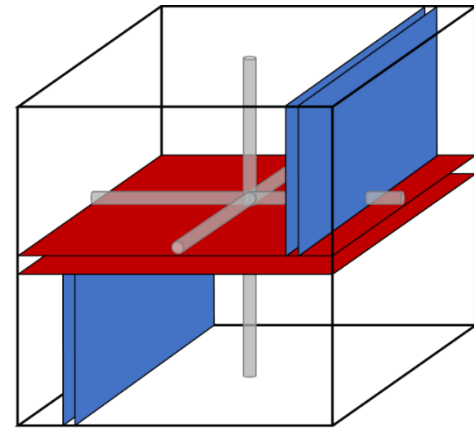
Definitions of the hydraulic and the mechanical aperture in reality (left) and in the modelling (right), *Marinelli (2016)*

# Multi-scale modelling approach

## Micro-scale boundary value problem

General principles for numerical resolution of the hydraulic system

- Hydraulic network respecting these conditions:
  - Anti-symmetric boundary fluxes
  - Macroscopic pressure gradient between the boundaries
- Hydraulic problem established through mass balance on each node (j)
- Hydraulic problem solved
  - For a given configuration
  - Under steady-state conditions
  - By applying the macro-pressure to one node



Example of a channel network with the mass balance on node j

# Multi-scale modelling approach

## Micro-scale boundary value problem

General principles for numerical resolution of the hydraulic system

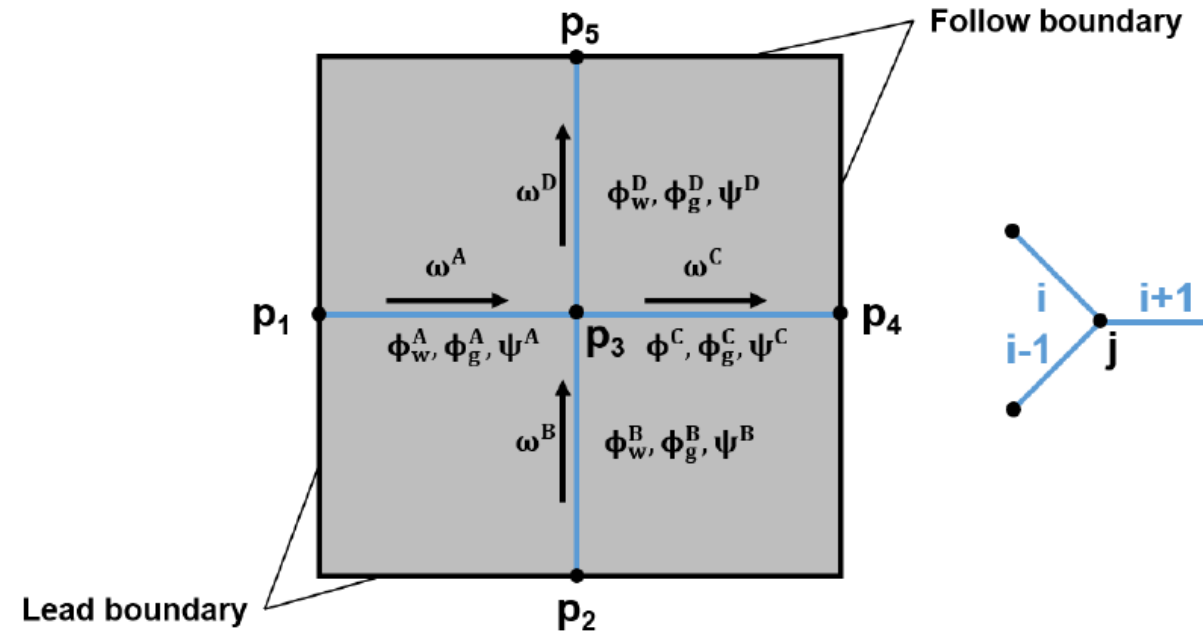
- Hydraulic network respecting these conditions:
  - Anti-symmetric boundary fluxes
  - Macroscopic pressure gradient between the boundaries

=> Channel (fracture or tube) mass fluxes of water and gas

$$\omega_w = - \underbrace{\frac{\rho_w k_{rw}}{\mu_w} \kappa \frac{\partial p_w^m}{\partial s}}_{\text{Advection of liquid water}}$$

$$\omega_g = - \underbrace{\frac{\rho_g k_{rg}}{\mu_g} \kappa \frac{\partial p_g^m}{\partial s}}_{\text{Advection of gaseous gas}} - \underbrace{H_g \frac{\rho_g k_{rw}}{\mu_w} \kappa \frac{\partial p_w^m}{\partial s}}_{\text{Advection of dissolved gas}}$$

$$- \underbrace{S_{rw} \bar{\tau} D_{dg/w} \frac{H_g}{\rho_w} \left( \frac{\rho_w \rho_{g,0}}{p_{g,0}} \frac{\partial p_g^m}{\partial s} - \frac{\rho_g \rho_{w,0}}{\chi_w} \frac{\partial p_w^m}{\partial s} \right)}_{\text{Diffusion of dissolved gas}}$$



Example of a channel network with the mass balance on node j

# Multi-scale modelling approach

## Micro-scale boundary value problem

General principles for numerical resolution of the hydraulic system

- Hydraulic problem established through mass balance on each node (j)
  - Mass conservation principle, *i.e.* for each node of the network, the sum of the input flows is equal to the sum of the output flows

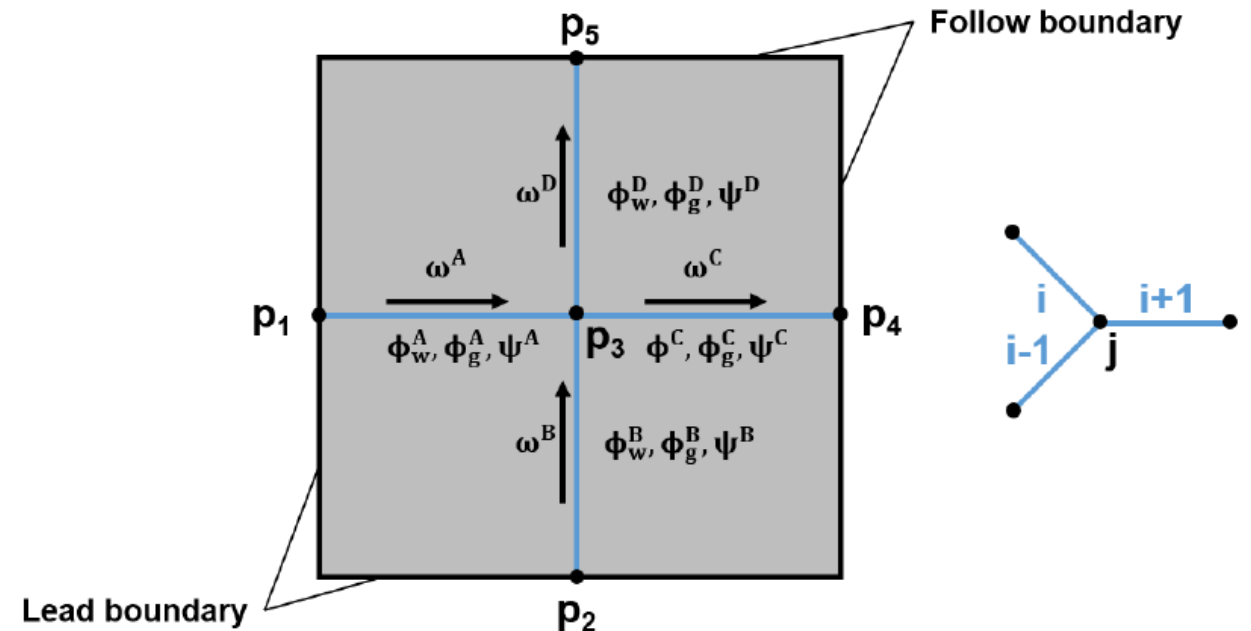
$$\frac{d\omega_\alpha^i}{ds^i} = 0 \quad \Leftrightarrow \quad \omega_\alpha^{i-1} + \omega_\alpha^i + \omega_\alpha^{i+1} = 0$$

$\alpha = w, g$  Liquid or gaseous phase

- Well-posed hydraulic system to solve

$$[G_{ww}] \{p_w^m\} = 0 \quad [G_{gg}] \{p_g^m\} + [G_{gw}] \{p_w^m\} = 0$$

- For a given configuration
- Under steady-state conditions
- By applying the macro-pressure to one node



Example of a channel network with the mass balance on node j

# Multi-scale modelling approach

## Micro-to-macro scale transition: Homogenisation

- Fluid fluxes

$$\begin{aligned} f_{w_i}^M \frac{\partial p_w^{*,M}}{\partial x_i} &= \frac{1}{\Omega} \int_{\Omega} f_{w_i}^m \frac{\partial p_w^{*,M}}{\partial x_i} d\Omega = \frac{1}{\Omega} \int_{\Gamma} \bar{q}_w^m p_w^{*,M} d\Gamma \\ &= \frac{1}{\Omega} \frac{\partial p_w^{*,M}}{\partial x_i} \int_{\Gamma} \bar{q}_w^m x_i d\Gamma \\ &= \frac{1}{\Omega} \int_{\Gamma} \bar{q}_w^m x_i d\Gamma \end{aligned}$$

$$f_{g_i}^M + f_{dg_i}^M = \frac{1}{\Omega} \int_{\Gamma} \bar{q}_g^m x_i d\Gamma$$

- Fluid masses: total amount of fluids inside the fractures and tubes

$$\begin{aligned} M_w^M &= \frac{1}{\Omega} \int_{\Omega_w^{int}} \rho_w d\Omega \\ &= \rho_w S_{r_w} \phi_n \end{aligned}$$

$$\begin{aligned} M_g^M &= M_g^m + M_{dg}^m \\ &= \frac{1}{\Omega} \left( \int_{\Omega_g^{int}} \rho_g d\Omega + \int_{\Omega_w^{int}} \rho_{dg} d\Omega \right) \\ &= \rho_g (1 - S_{r_w}) \phi_n + \rho_{dg} S_{r_w} \phi_n \end{aligned}$$

# Multi-scale modelling approach

## Macro-scale boundary value problem

- Under matrix form:

$$\begin{bmatrix} [K_{ww}^M]_{(3 \times 3)} & [K_{wg}^M]_{(3 \times 3)} \\ [K_{gw}^M]_{(3 \times 3)} & [K_{gg}^M]_{(3 \times 3)} \end{bmatrix} \begin{Bmatrix} \begin{Bmatrix} \delta \nabla p_w^M \\ \delta p_w^M \end{Bmatrix}_{(3)} \\ \begin{Bmatrix} \delta \nabla p_g^M \\ \delta p_g^M \end{Bmatrix}_{(3)} \end{Bmatrix} = \begin{Bmatrix} \begin{Bmatrix} \delta f_w^M \\ \delta \dot{M}_w^M \end{Bmatrix}_{(3)} \\ \begin{Bmatrix} \delta f_g^M \\ \delta \dot{M}_g^M \end{Bmatrix}_{(3)} \end{Bmatrix}$$

Summarized as:

$$[A^M]_{(10 \times 10)} \{\delta U^M\}_{(10)} = \{\delta \Sigma^M\}_{(10)}$$





# Content

- ① Context
- ② From experimental evidence to modelling
- ③ Multi-scale modelling approach
- ④ Preliminary modelling
- ⑤ Modelling gas injection experiment
- ⑥ Conclusions

# Preliminary modelling

## One-element simulation

Bedding plane separation:

- $300\mu m$

Bedding plane aperture:

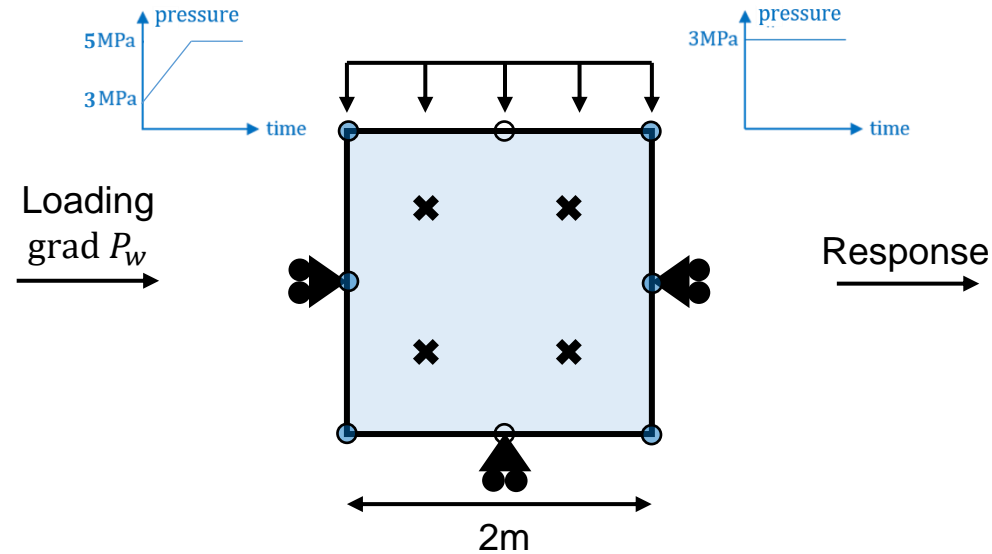
- $0.1\mu m$

Tubes diameter

→ Distribution curve

Bridging plane aperture

→ not considered

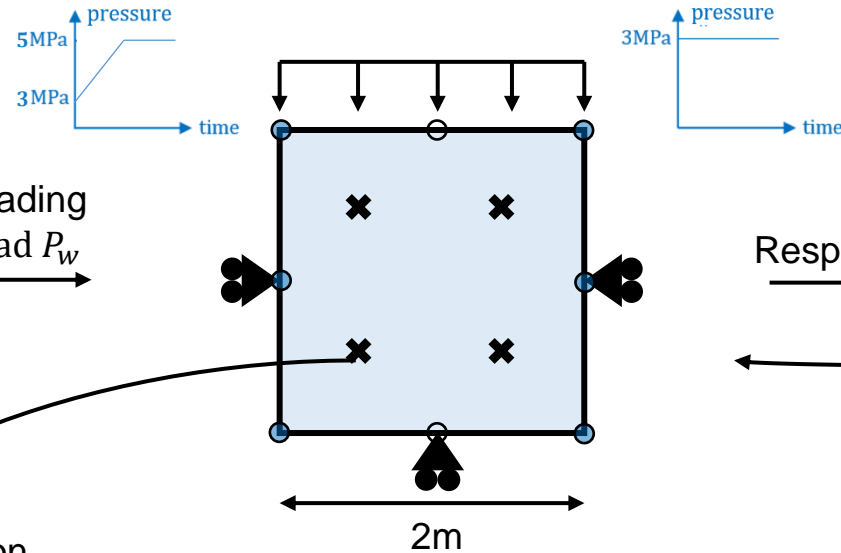


Injection test

- Mechanically blocked
- Water pressure increase
  - 3MPa to 5MPa
- Gas pressure imposed at 3MPa

# Preliminary modelling

## One-element simulation



Bedding plane separation:

- $300\mu\text{m}$

Bedding plane aperture:

- $0.1\mu\text{m}$

Tubes diameter

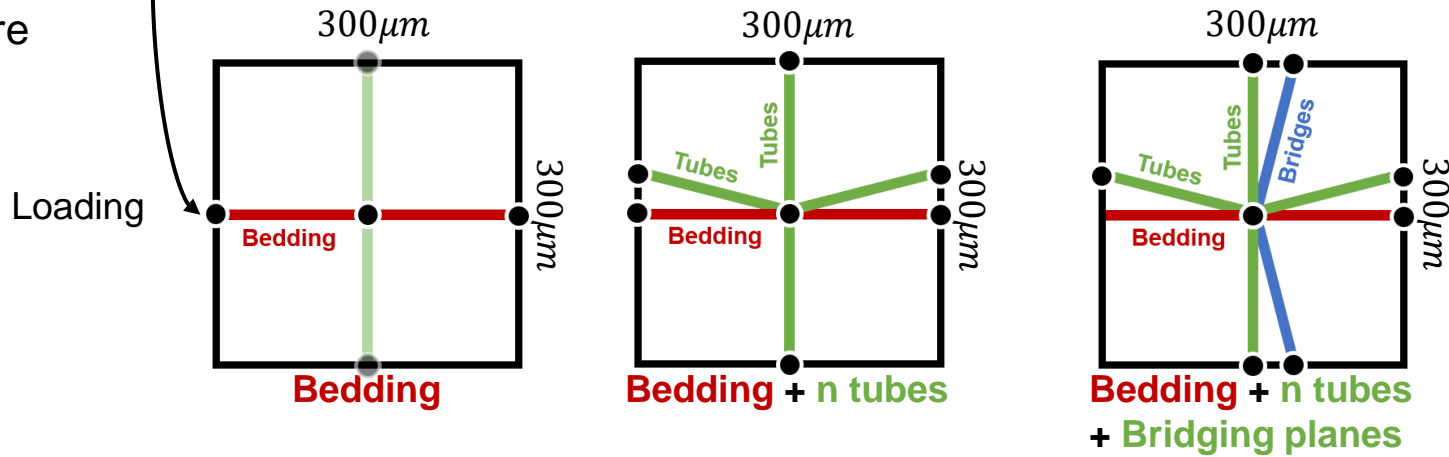
→ Distribution curve

Bridging plane aperture

→ not considered

Injection test

- Mechanically blocked
- Water pressure increase from 3MPa to 5MPa
- Gas pressure imposed at 3MPa

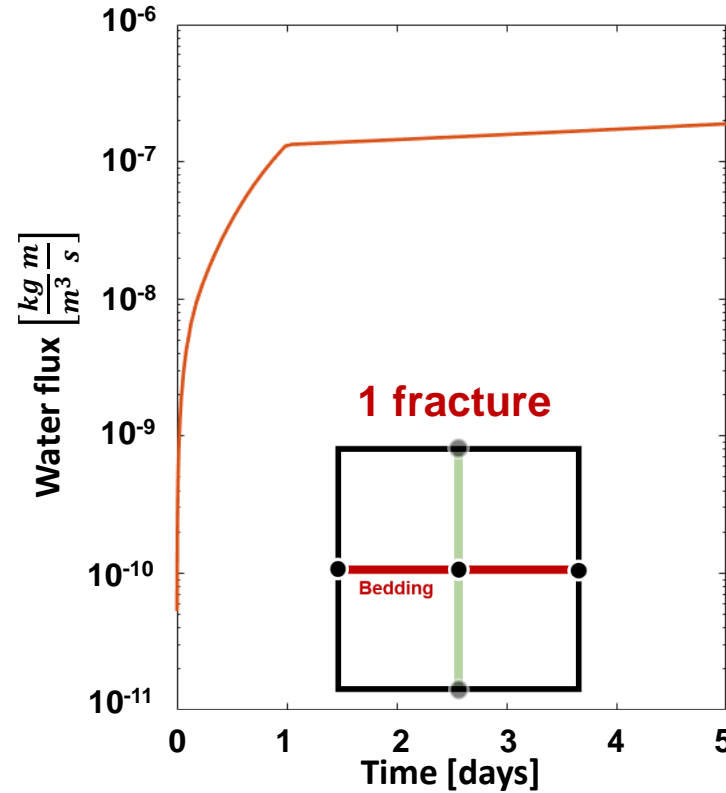
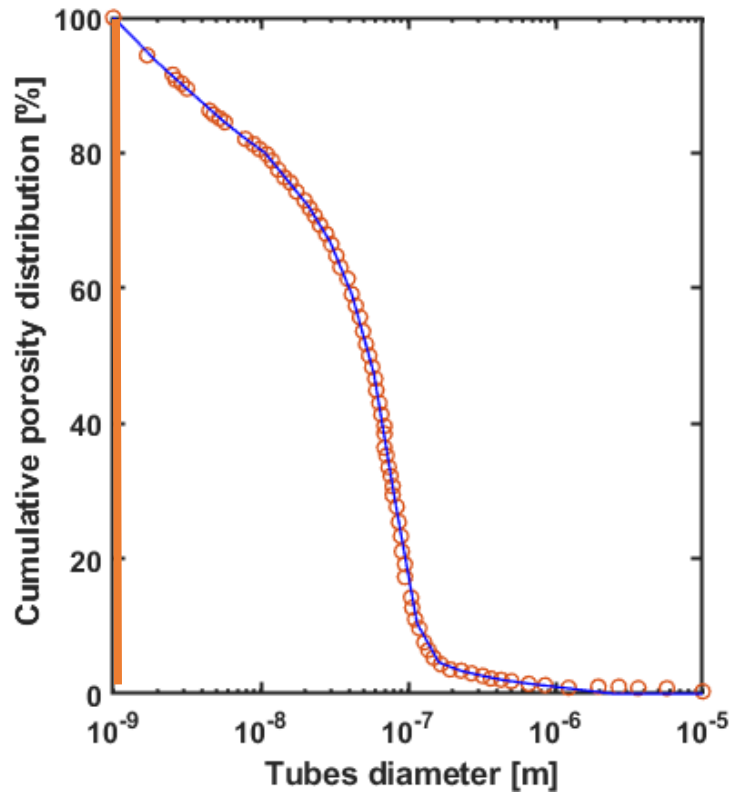


Homogenisation

Response

# Preliminary modelling

## One-element simulation

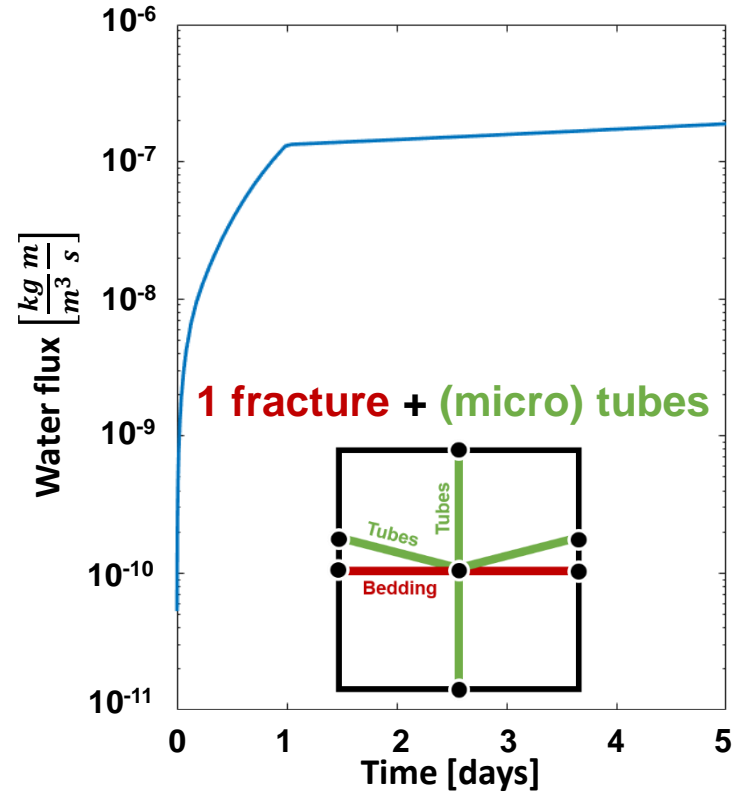
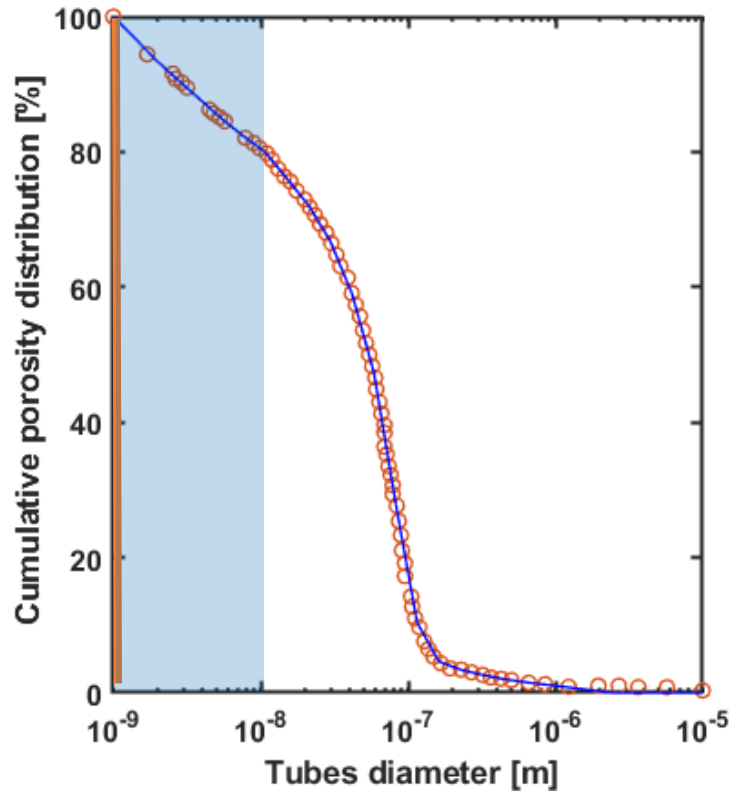


$$k_{int} = \frac{\mu_w}{\rho_w} Flux \frac{\Delta x}{\Delta p} \quad \text{with} \quad \begin{array}{l} \Delta x = 2m \\ \Delta p = 2 MPa \\ \text{Aperture} = 2.0 \cdot 10^{-6}m \end{array}$$

Number of tubes	Flux [ $\frac{kg \cdot m}{m^3 \cdot s}$ ]	$k_{int,x}$ [ $m^2$ ]
<b>0</b>	<b><math>1.581 \cdot 10^{-7}</math></b>	<b><math>1.581 \cdot 10^{-19}</math></b>

# Preliminary modelling

## One-element simulation

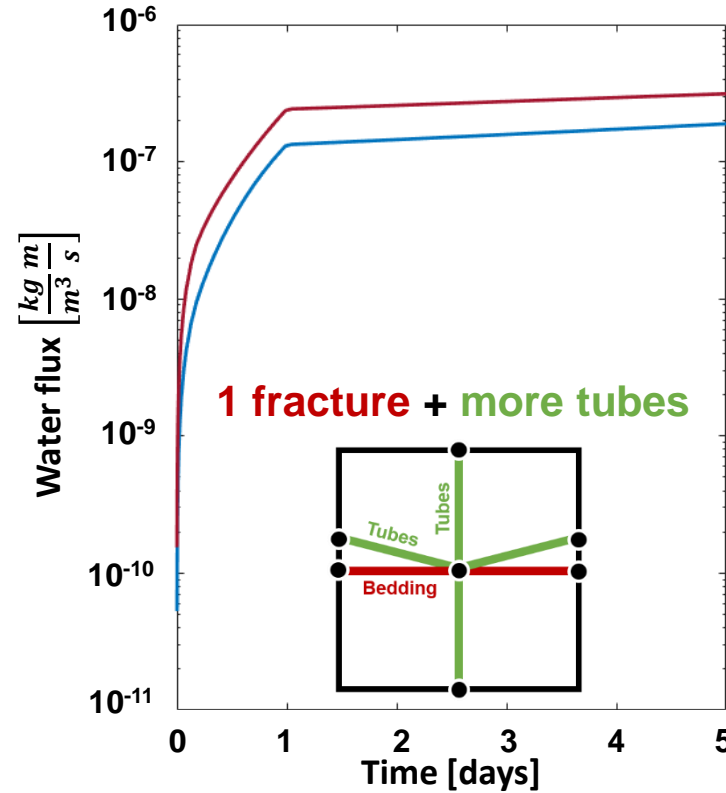
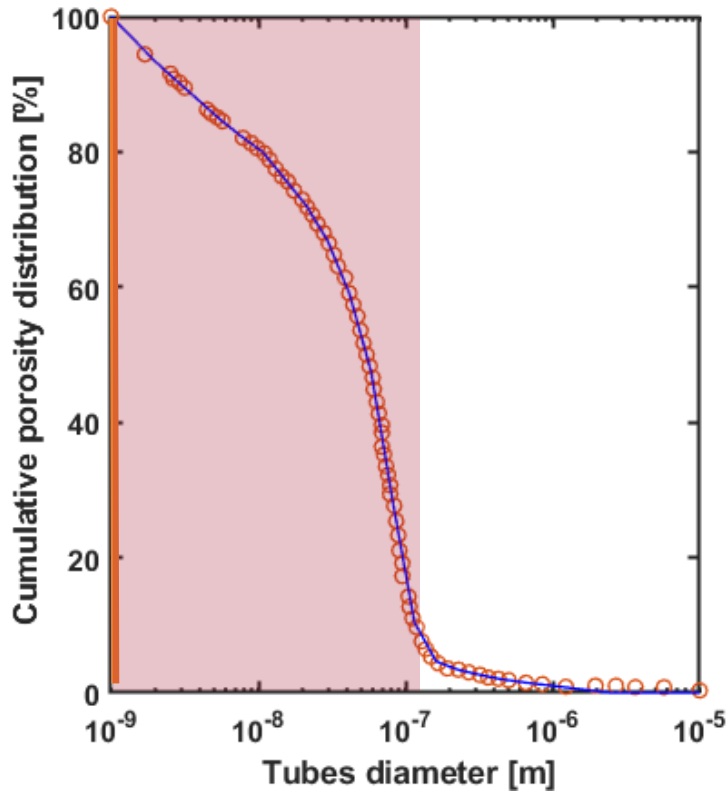


$$k_{int} = \frac{\mu_w}{\rho_w} Flux \frac{\Delta x}{\Delta p} \quad \text{with} \quad \begin{array}{l} \Delta x = 2m \\ \Delta p = 2\ MPa \\ \text{Aperture} = 2.0 \cdot 10^{-6}m \end{array}$$

Number of tubes	Flux [ $\frac{kg\ m}{m^3\ s}$ ]	$k_{int,x}$ [m <sup>2</sup> ]
0	$1.581 \cdot 10^{-7}$	$1.581 \cdot 10^{-19}$
770	$1.643 \cdot 10^{-7}$	$1.643 \cdot 10^{-19}$

# Preliminary modelling

## One-element simulation



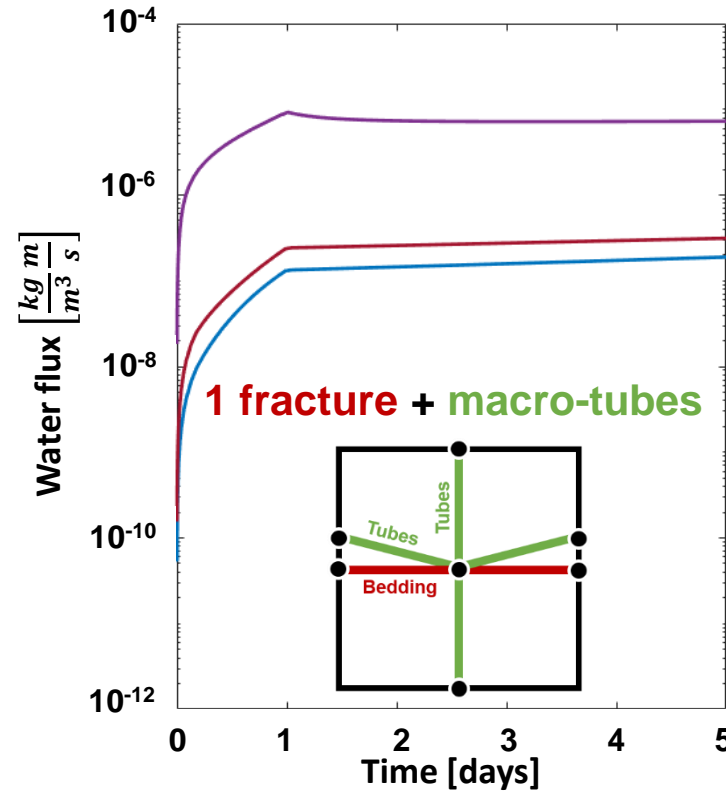
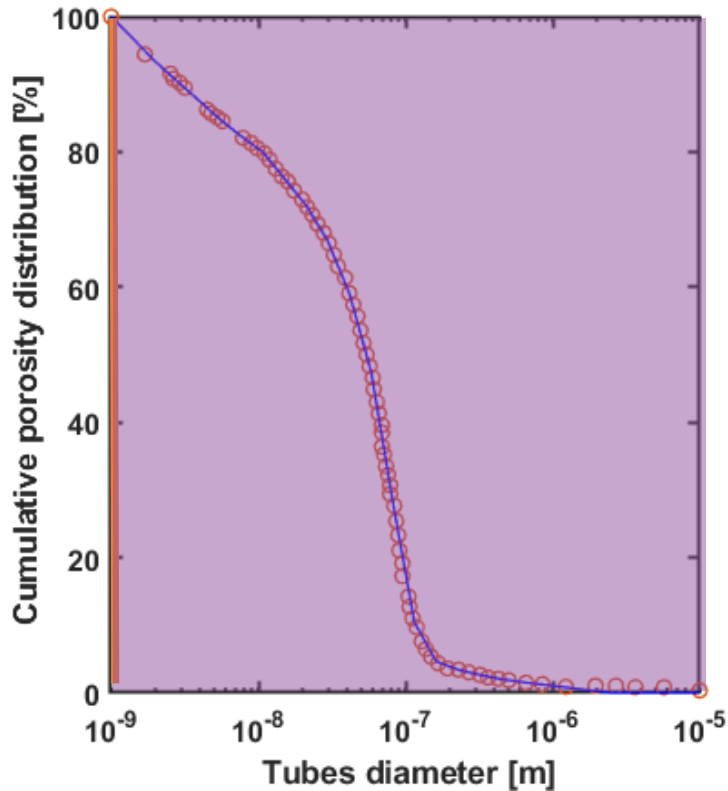
$$k_{int} = \frac{\mu_w}{\rho_w} Flux \frac{\Delta x}{\Delta p} \quad \text{with} \quad \begin{aligned} \Delta x &= 2m \\ \Delta p &= 2\ MPa \\ \text{Aperture} &= 2.0 \cdot 10^{-6}m \end{aligned}$$

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6394	$3.057 \cdot 10^{-7}$	$3.057 \cdot 10^{-19}$

Fracture-controlled flow

# Preliminary modelling

## One-element simulation



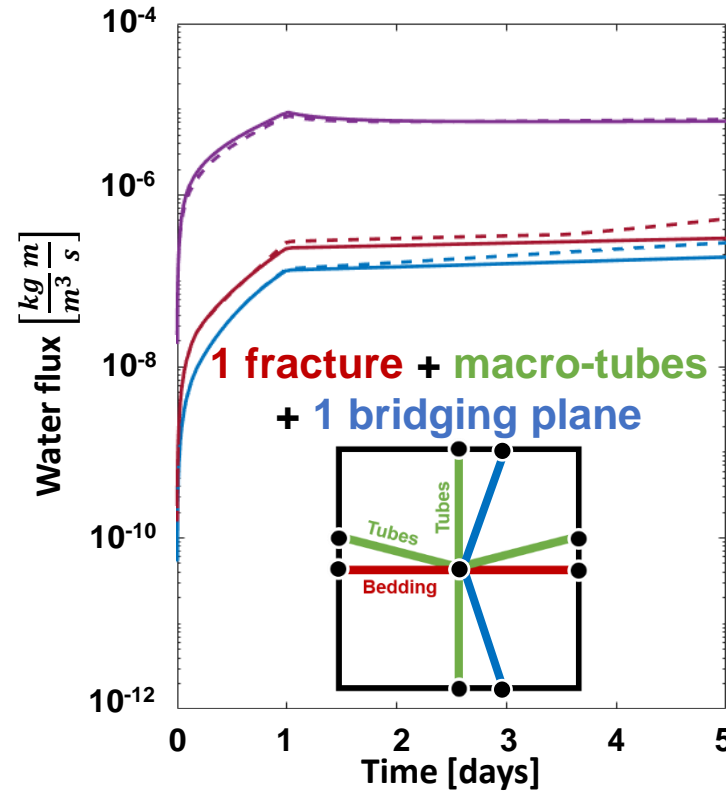
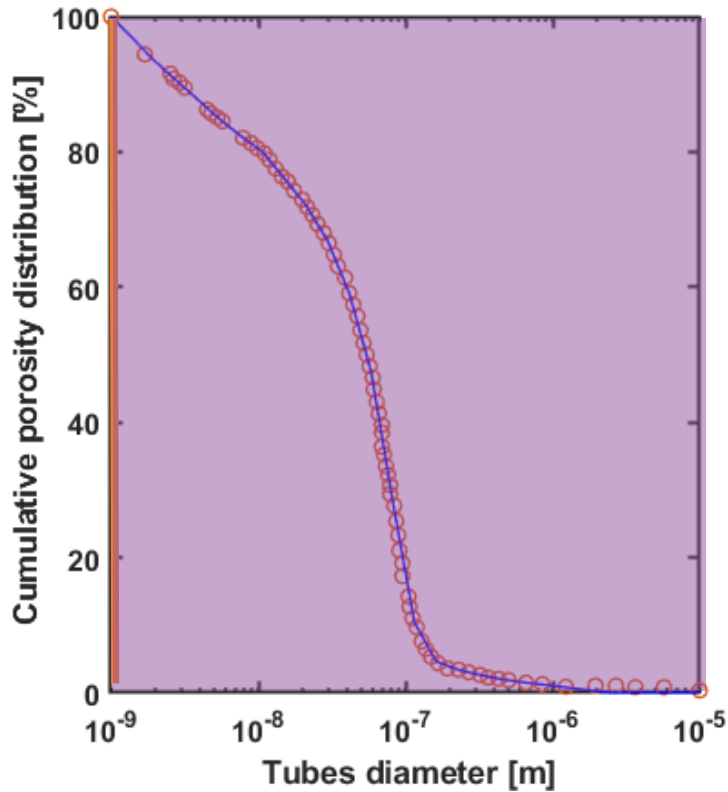
$$k_{int} = \frac{\mu_w}{\rho_w} Flux \frac{\Delta x}{\Delta p} \quad \text{with} \quad \begin{aligned} \Delta x &= 2m \\ \Delta p &= 2\ MPa \\ \text{Aperture} &= 2.0 \cdot 10^{-6}m \end{aligned}$$

Number of tubes	Flux [ $\frac{kg\ m}{m^3\ s}$ ]	$k_{int,x}$ [ $m^2$ ]
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6394	$3.057 \cdot 10^{-7}$	$3.057 \cdot 10^{-19}$
<b>Fracture-controlled flow</b>		
9995	$7.200 \cdot 10^{-6}$	$7.200 \cdot 10^{-18}$

Effect of large pores

# Preliminary modelling

## One-element simulation



$$k_{int} = \frac{\mu_w}{\rho_w} Flux \frac{\Delta x}{\Delta p} \quad \text{with} \quad \begin{aligned} \Delta x &= 2m \\ \Delta p &= 2\ MPa \\ \text{Aperture} &= 2.0 \cdot 10^{-6}m \end{aligned}$$

Number of tubes	Flux [ $\frac{kg\ m}{m^3\ s}$ ]	$k_{int,x}$ [ $m^2$ ]
<b>0</b>	<b><math>1.581 \cdot 10^{-7}</math></b>	<b><math>1.581 \cdot 10^{-19}</math></b>
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<b>Fracture-controlled flow</b>		
<b>9995</b>	<b><math>7.200 \cdot 10^{-6}</math></b>	<b><math>7.200 \cdot 10^{-18}</math></b>

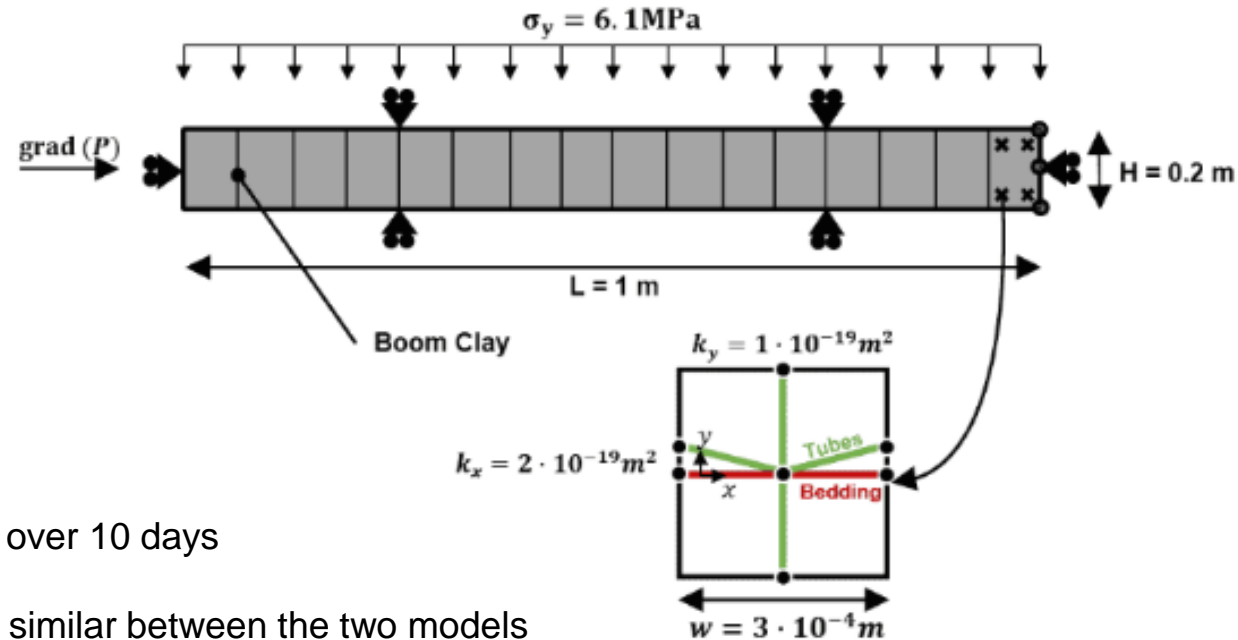
Effect of large pores



# Model verification

## Comparison with a macro-scale THM coupled model

Geometry



$$P_{w0} = 0.6\text{ MPa}$$

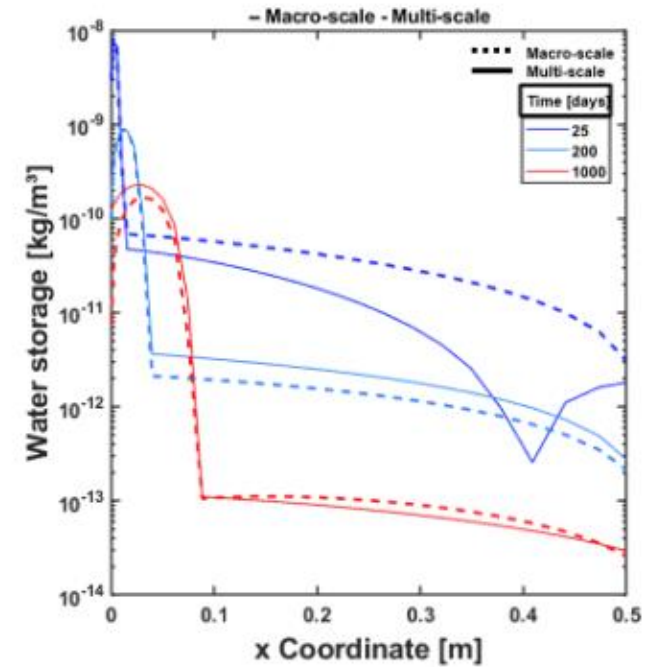
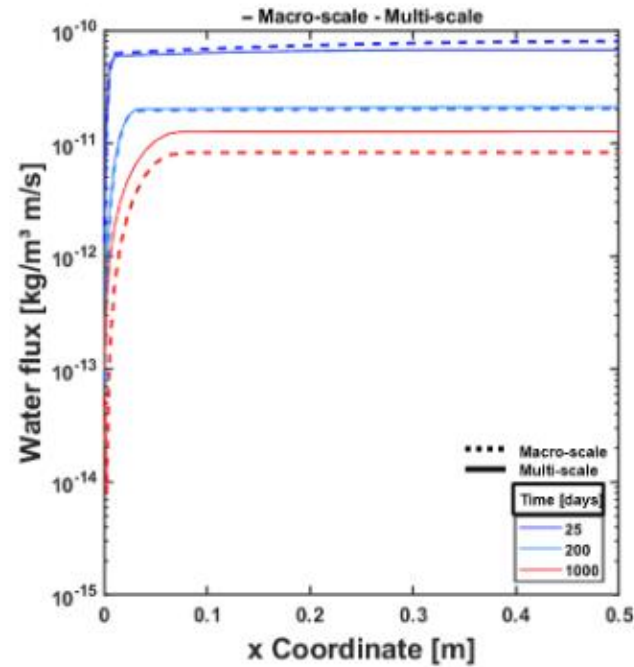
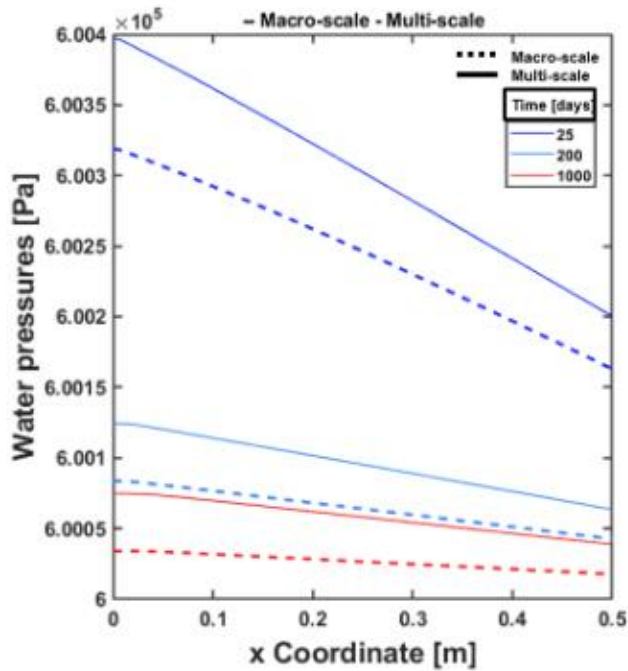
$$P_{g0} = 0.1\text{ MPa} \rightarrow P_g = 1.0\text{ MPa over 10 days}$$

All the parameters are taken similar between the two models

# Model verification

Comparison with a macro-scale THM coupled model

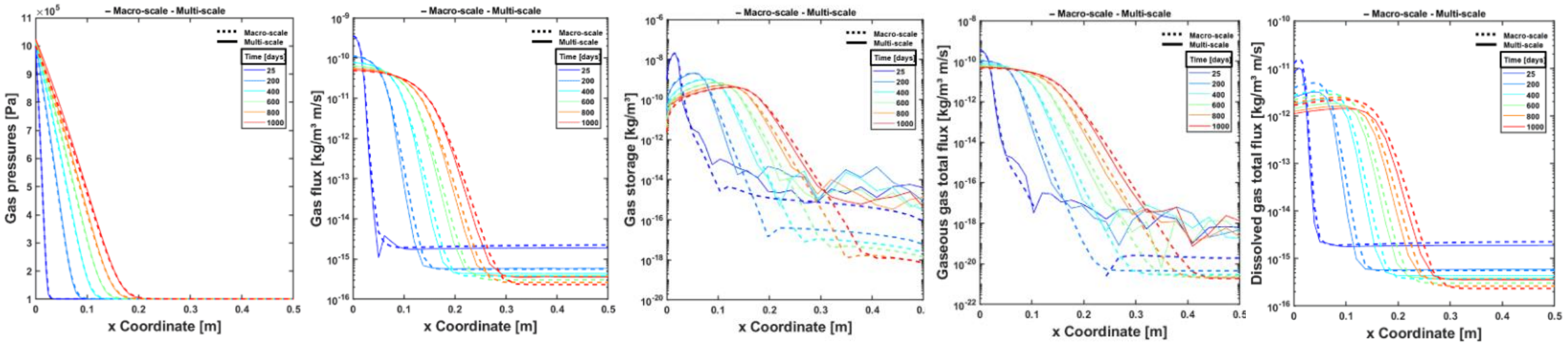
Water-related results



# Model verification

## Comparison with a macro-scale THM coupled model

### Gas-related results





# Content

- ① Context
- ② From experimental evidence to modelling
- ③ Multi-scale modelling approach
- ④ Preliminary modelling
- ⑤ Modelling gas injection experiment
- ⑥ Conclusions

# Gas injection experiment

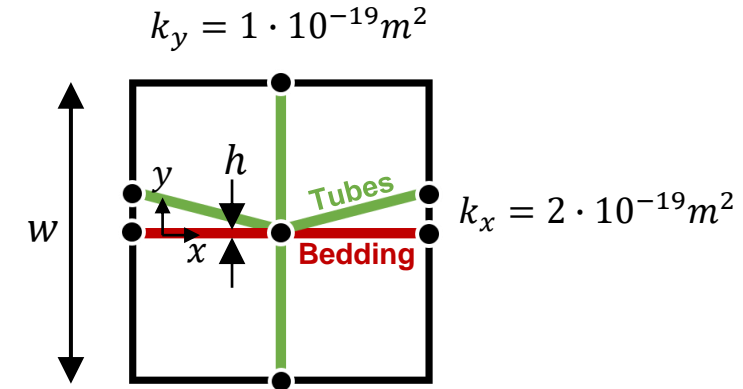
## Characterisation of the microstructure parameters

### ► 1. Size of the REV

Bedding plane separation  
 $w = 300 \mu m$

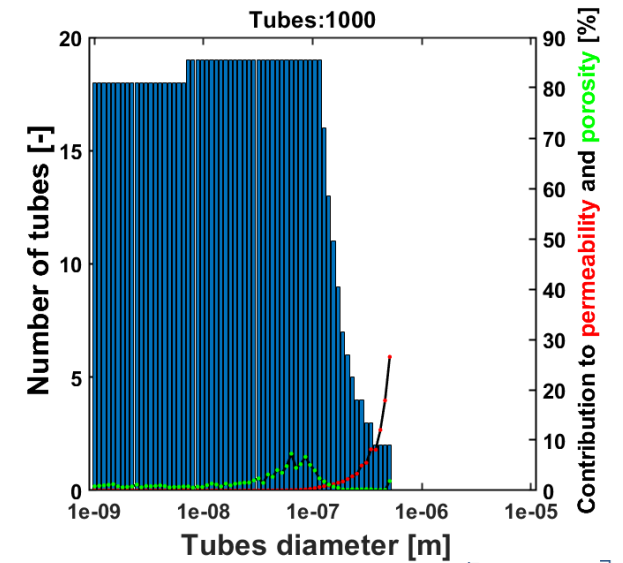
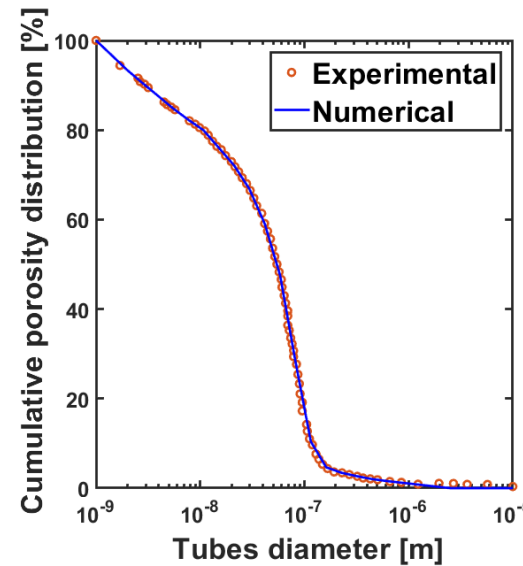
Experimental estimations of bedding plane separation,  
 from *Gonzalez-Blanco (2017)*

FESEM	$\mu$ -CT
150 – 270 $\mu m$	410 – 560 $\mu m$



### ► 2. Macroporosity

Fitting of the pore size distribution  
 Effect of small-size pores  
 (Tortuosity = Calibration factor)



# Gas injection experiment

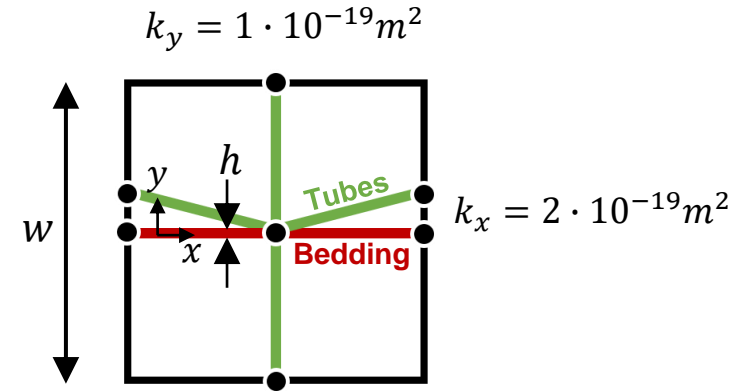
## Characterisation of the microstructure parameters

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 $w = 300 \mu m$

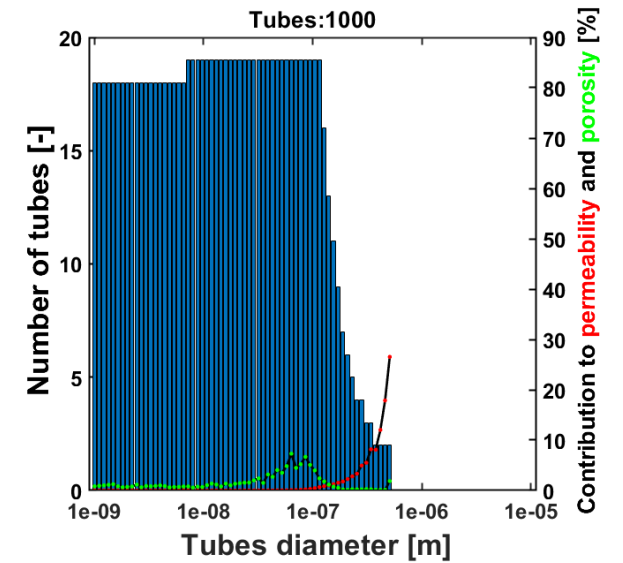
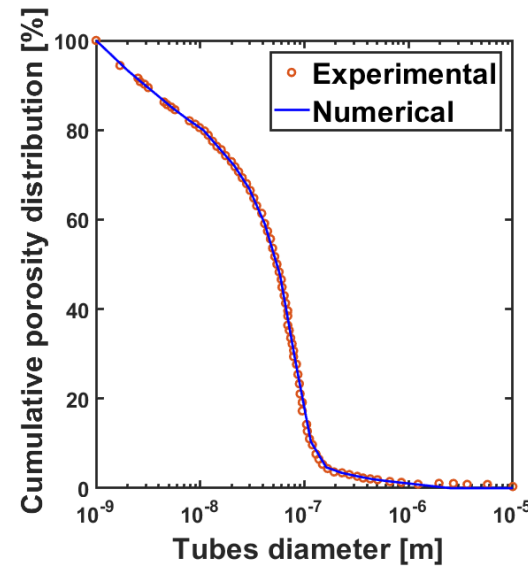
Experimental estimations of bedding plane separation,  
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### ► 2. Macroporosity

Fitting of the pore size distribution  
 Effect of small-size pores  
 (Tortuosity = Calibration factor)



### ► 3. Intrinsic permeability Effect of large-size pores

Fracture aperture

$$k_{x,frac,0} = 10^{-19} m^2$$

$$\rightarrow h_0 = \sqrt[3]{12 w k}$$

Macropores

$$k_x = \frac{\pi}{8} \left(\frac{D}{2}\right)^4 \left(\frac{1}{w^2}\right) + \frac{k_{x,frac}}{12} \left(\frac{h}{w}\right)$$

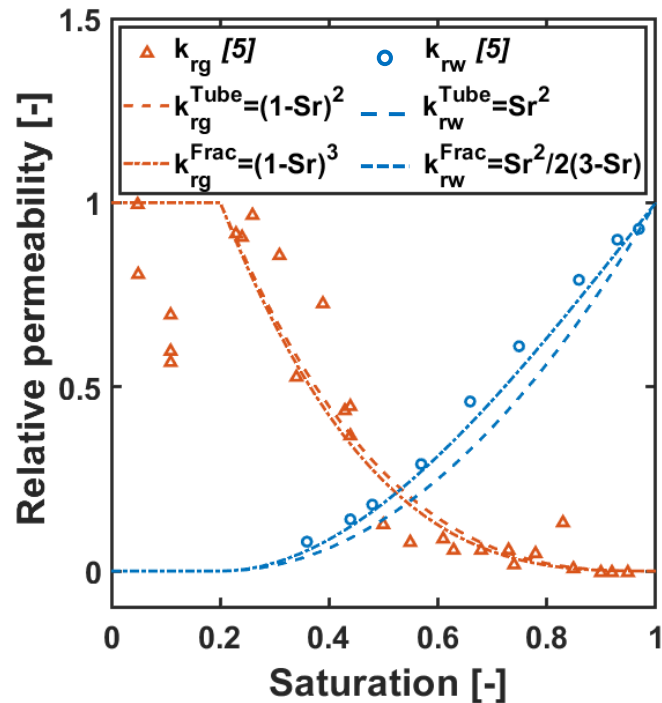
$$k_y = \frac{\pi}{8} \left(\frac{D}{2}\right)^4 \left(\frac{1}{w^2}\right)$$

# Gas injection experiment

## Characterisation of the microstructure parameters

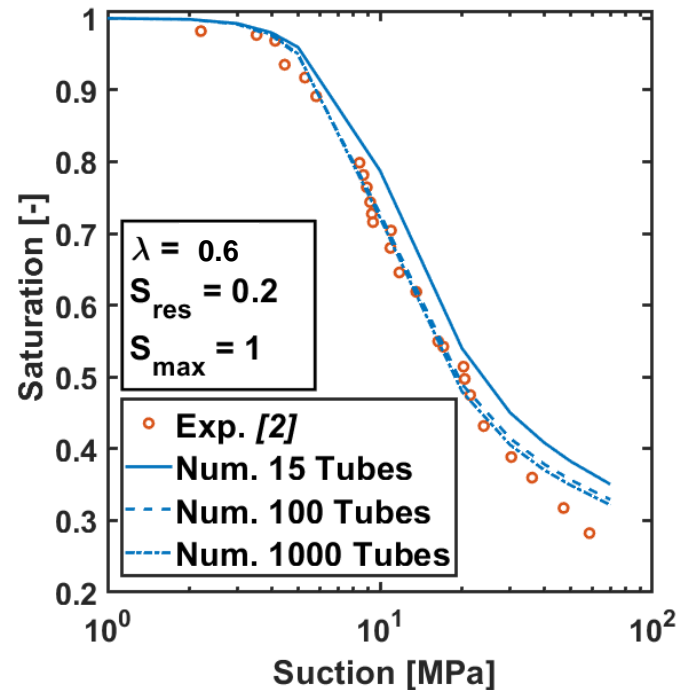
### ► 4. Relative permeability curves

*Yuster et al. (1951)*



### ► 5. Retention curve

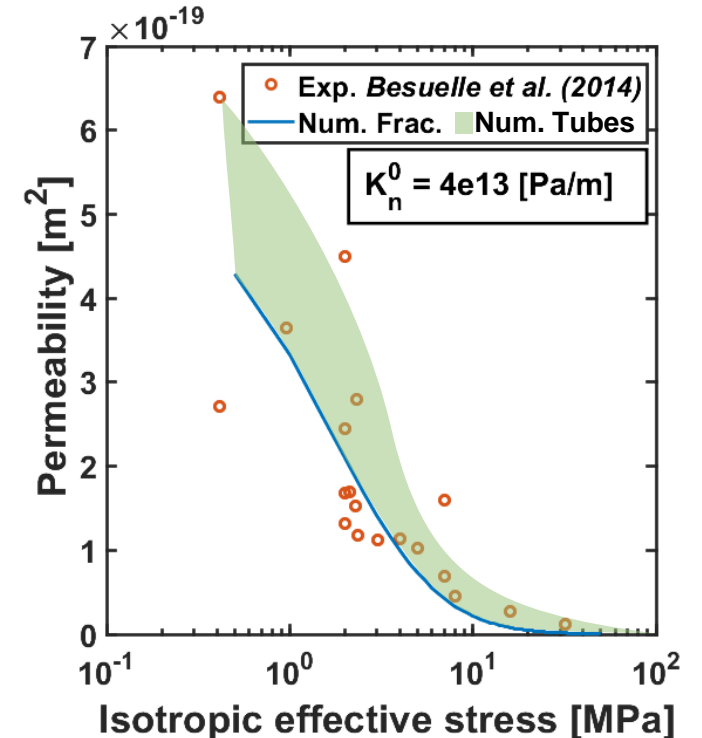
*Van Genuchten (1980)*



$$S_r = S_{res} + (S_{max} - S_{res}) \left( 1 + \left( \frac{s}{P_e} \right)^{\frac{1}{1-\lambda}} \right)^{-\lambda}$$

### ► 6. Normal stiffness of the fracture

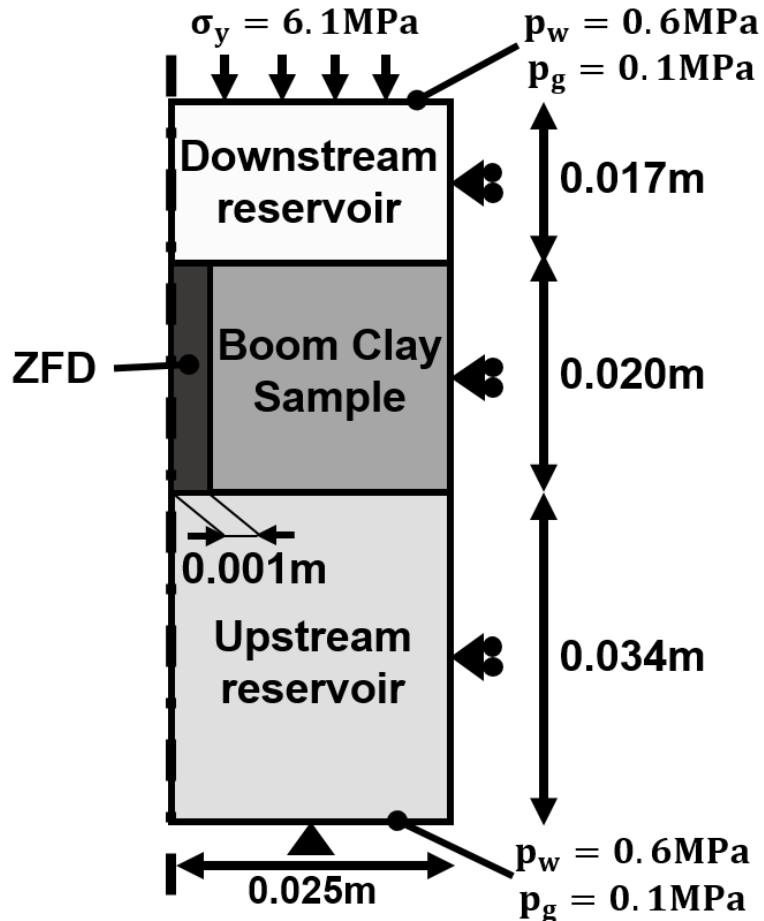
*Goodman (1976)*



$$\Delta\sigma' = K_n \Delta h \quad \text{with} \quad K_n = \frac{K_n^0}{\left( 1 + \frac{\Delta h}{h_0} \right)^2}$$

# Gas injection experiment

## Geometry and boundary conditions



## Parameters

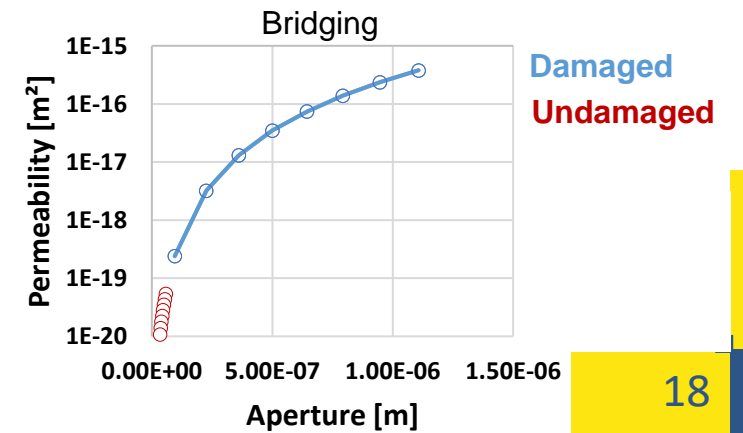
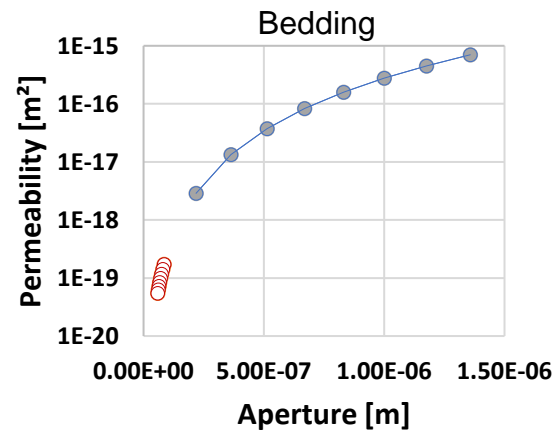
### Reservoirs

- Stiff elements:  $E = 10000\text{MPa}$   $\nu = 0.3$
- Highly conductive:  $n = 0.5$   $k = 10^{-10}\text{m}^2$
- Flat retention curve:  $P_{\text{entry}} = 0.01\text{MPa}$

### Boom Clay matrix

- Mechanical:  $E = 200 - 400\text{MPa}$   $\nu = 0.33$
- Hydraulic:
  - Initial aperture:  $0.80 - 1.27 \cdot 10^{-7}\text{m}$
  - Initial permeability:  $2.0 - 4.0 \cdot 10^{-19}\text{m}^2$
  - Initial porosity: 0.363

### Boom Clay Zone of Fracture Development (ZFD)

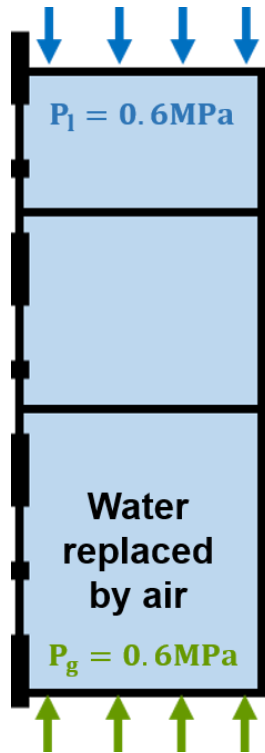




# Gas injection experiment

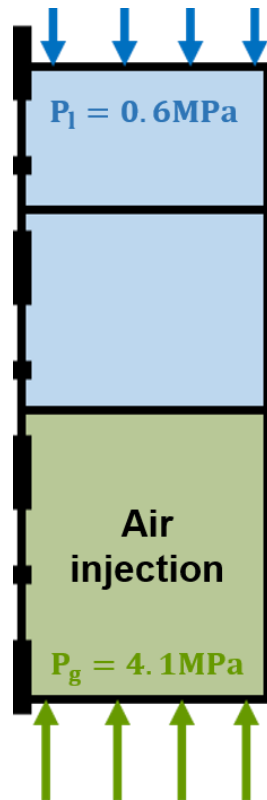
## Simulation stages

Stage 1



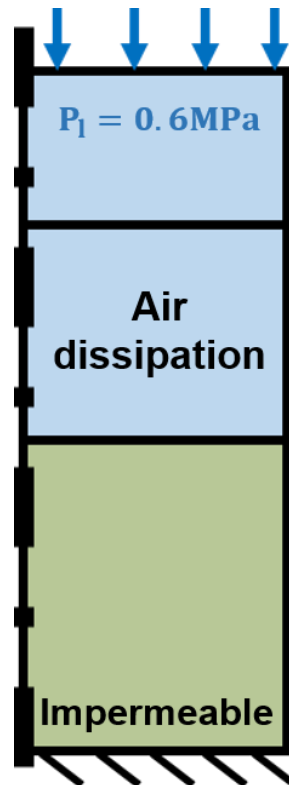
0-500 [min]

Stage 2

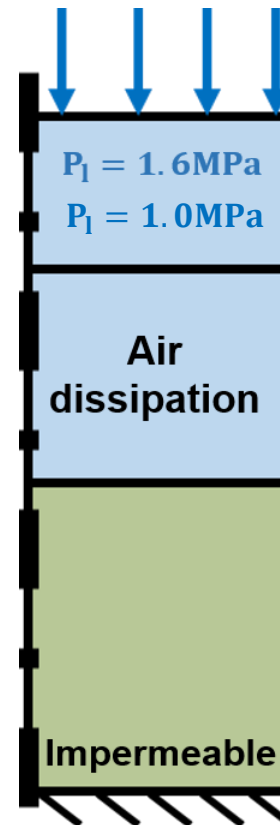


500-745 [min]

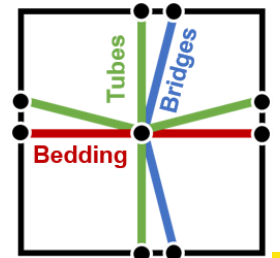
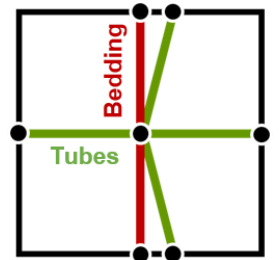
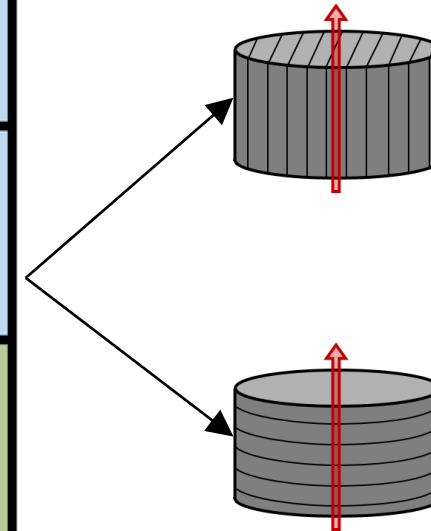
Stage 3



745-1080 [min]

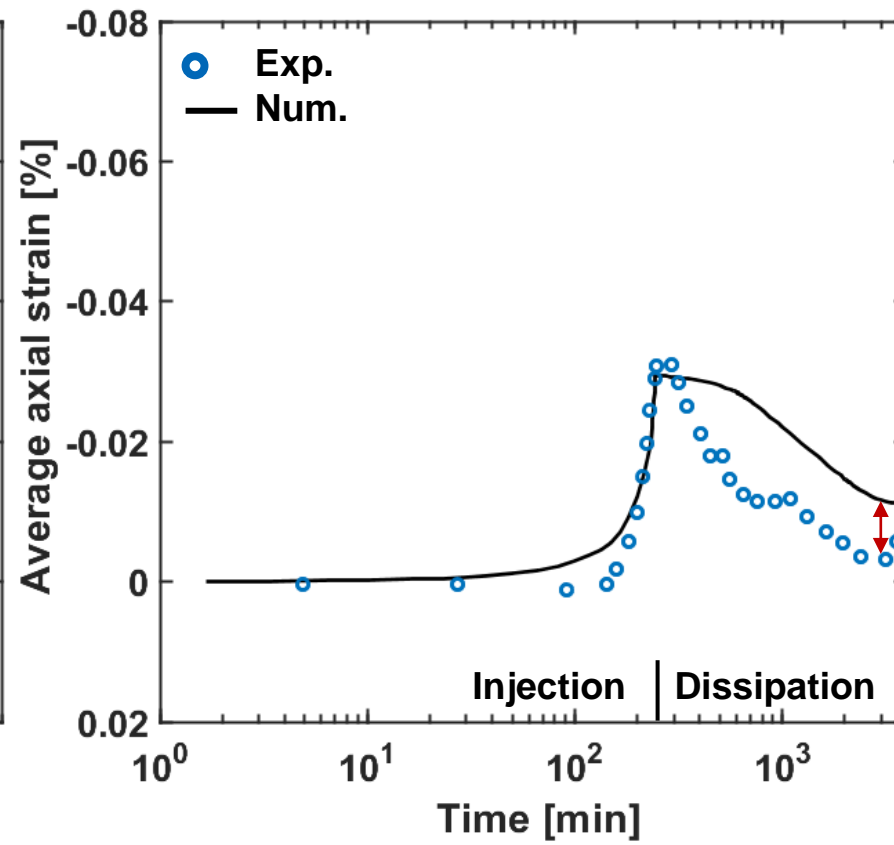
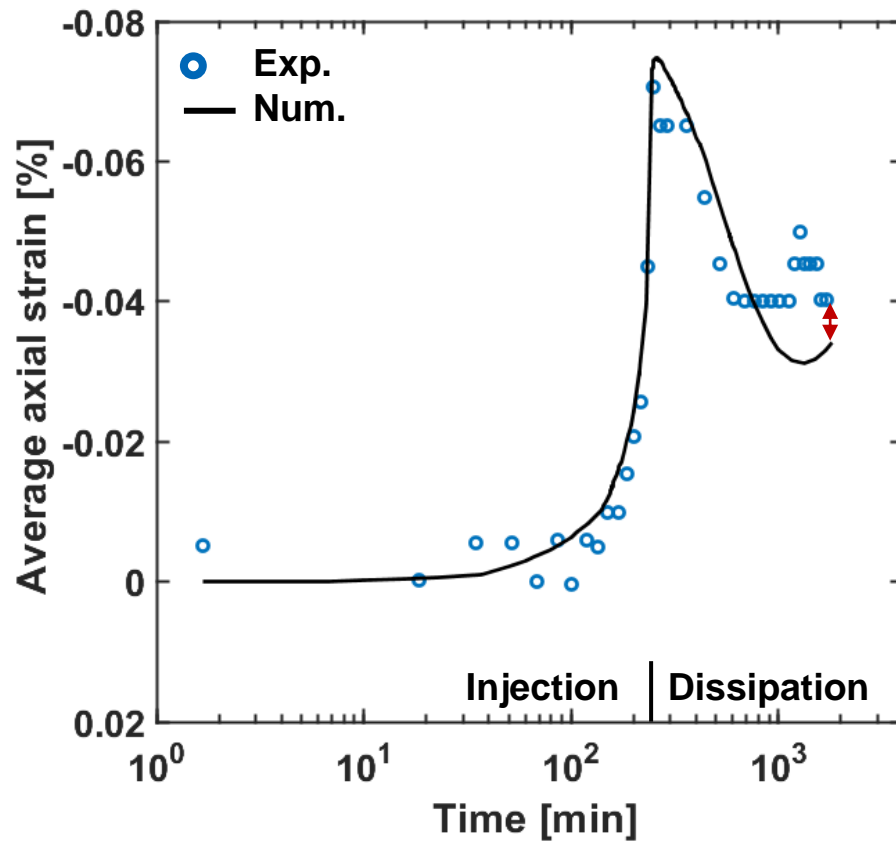
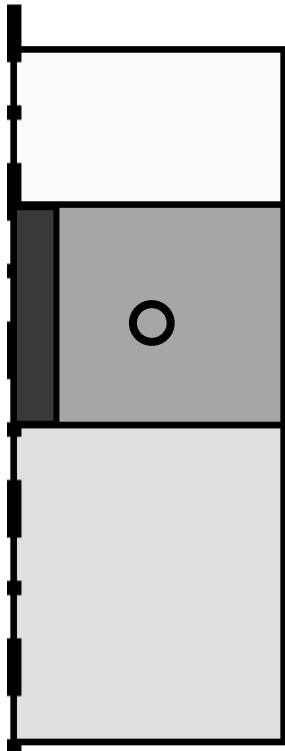
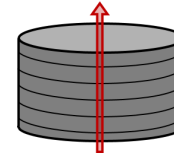
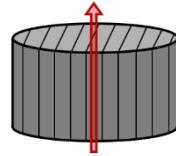


1080-2300 [min]



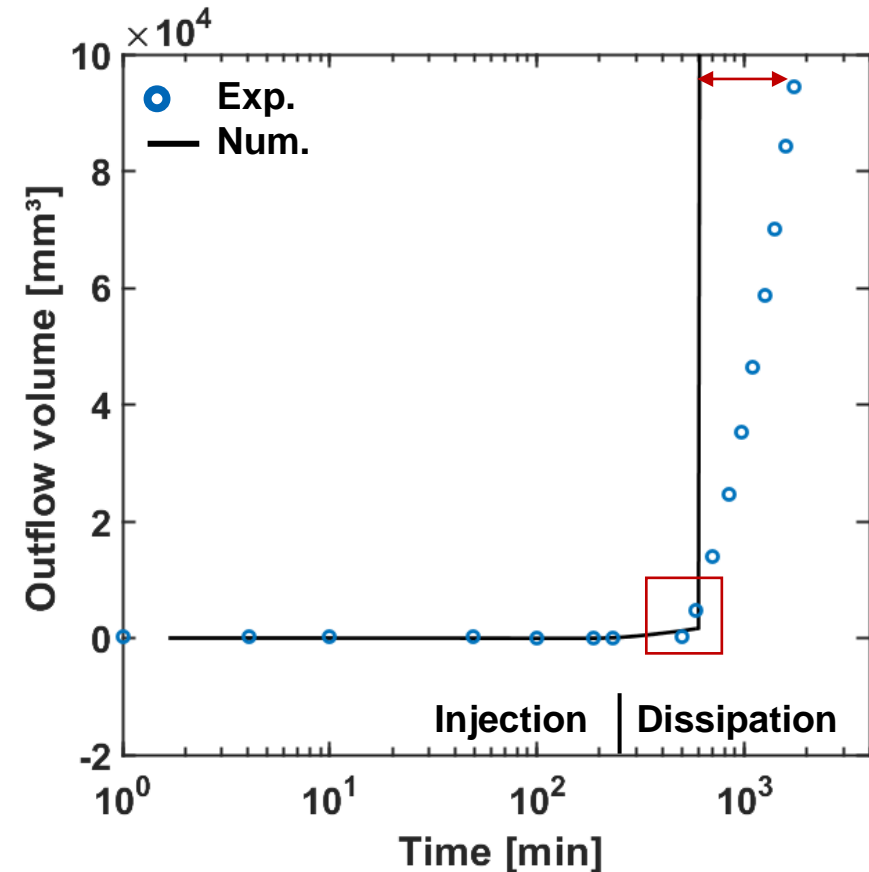
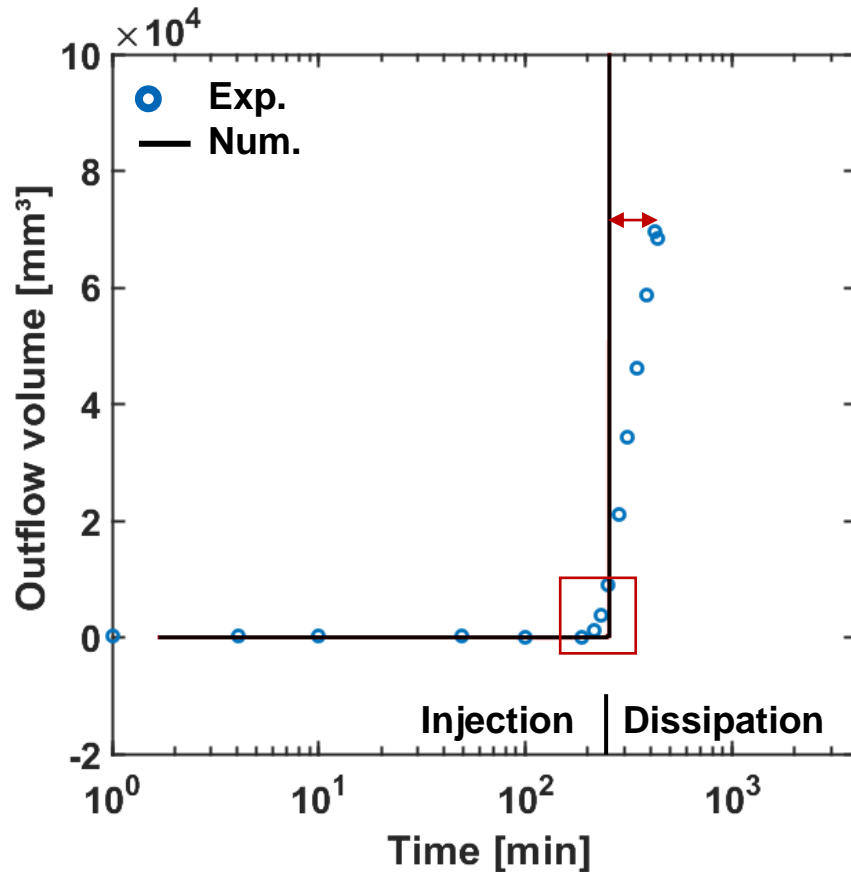
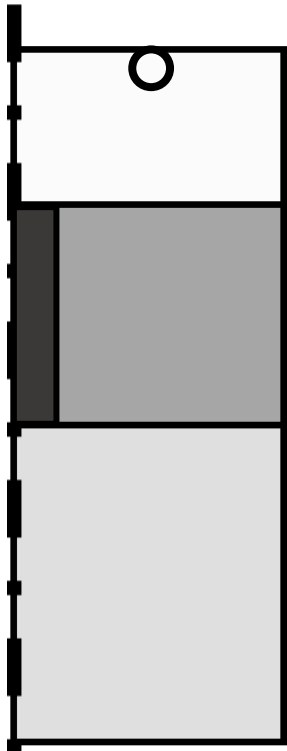
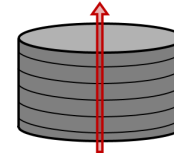
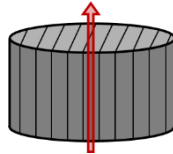
# Gas injection experiment

Average axial strain



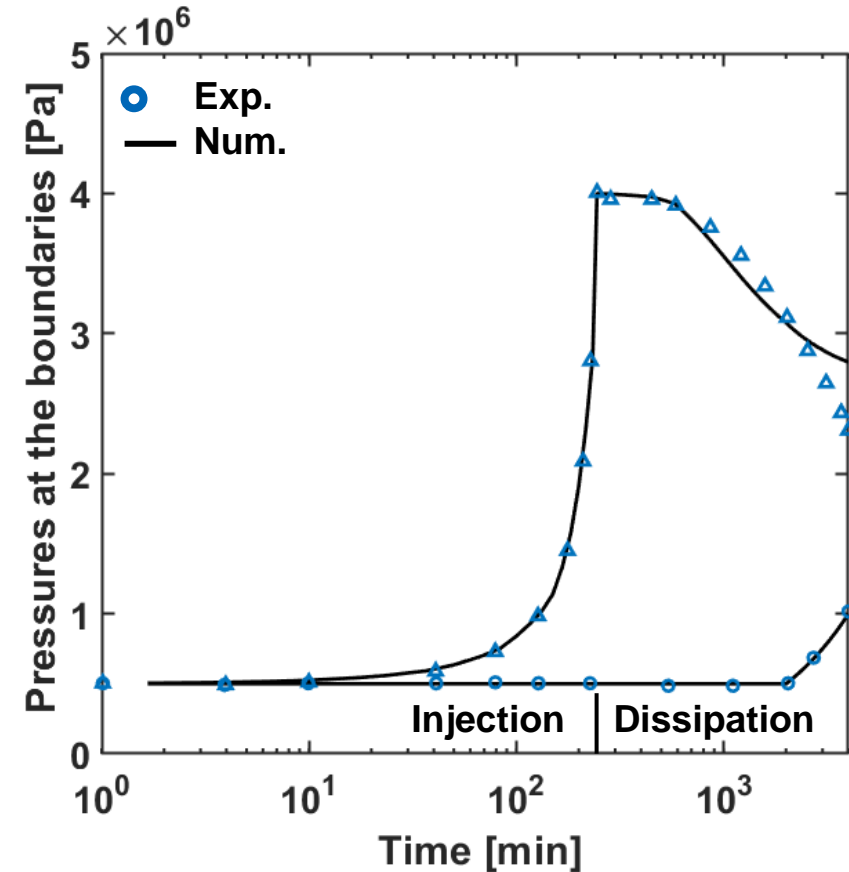
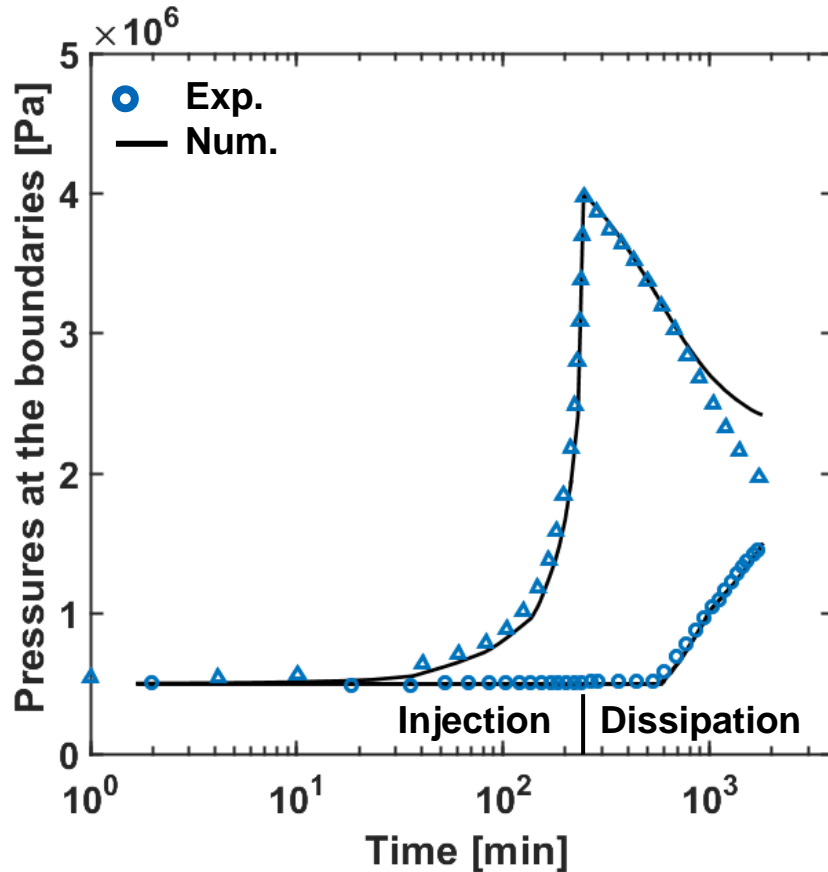
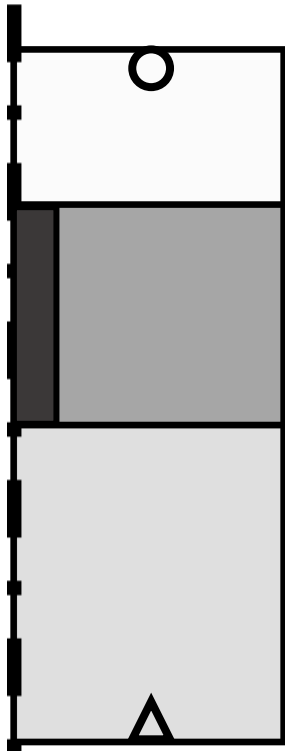
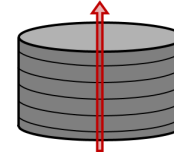
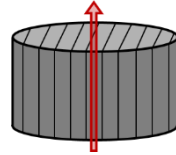
# Gas injection experiment

Outflow volume



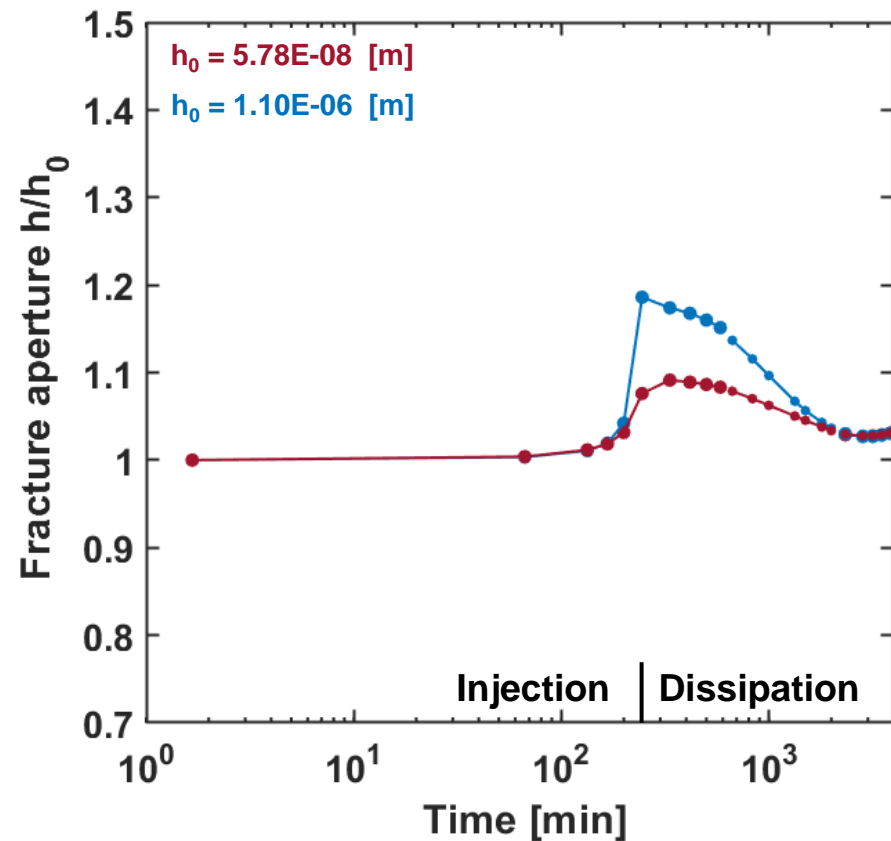
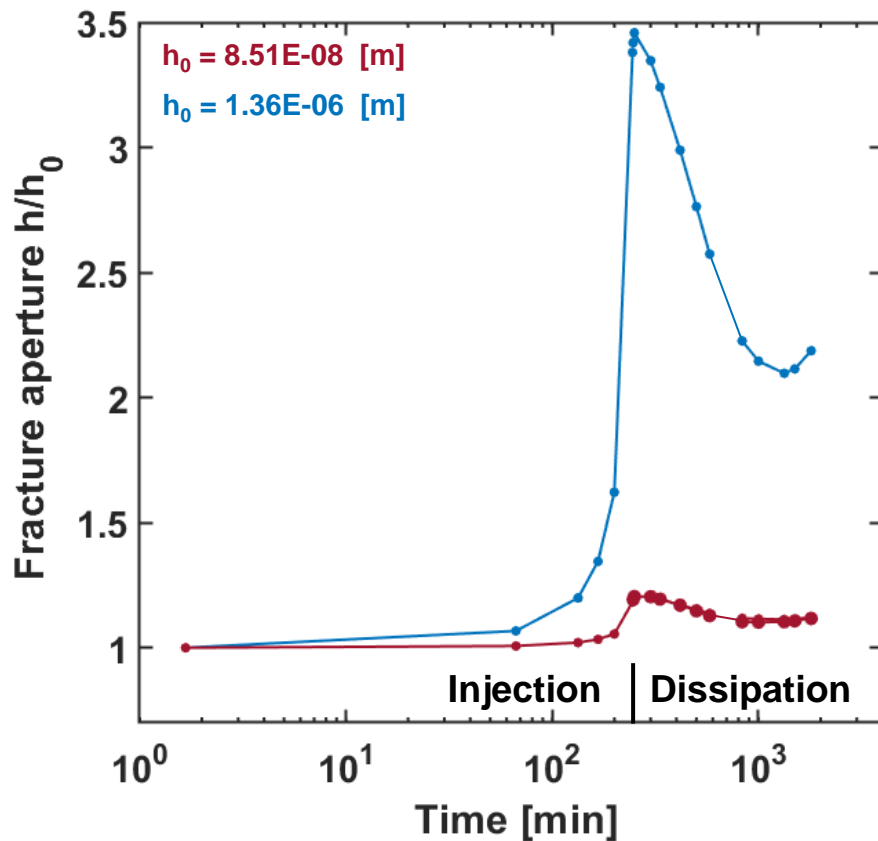
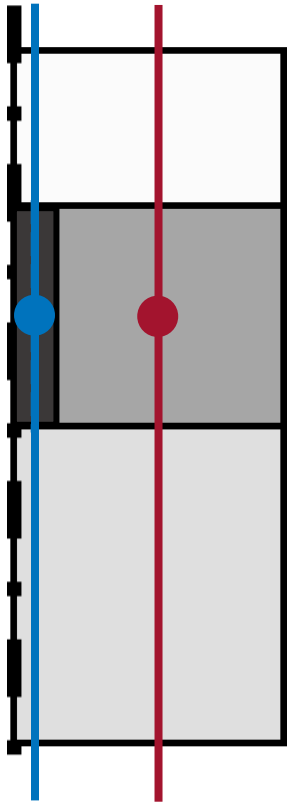
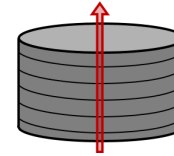
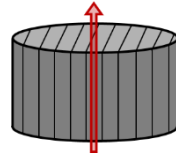
# Gas injection experiment

Injection and recovery pressures



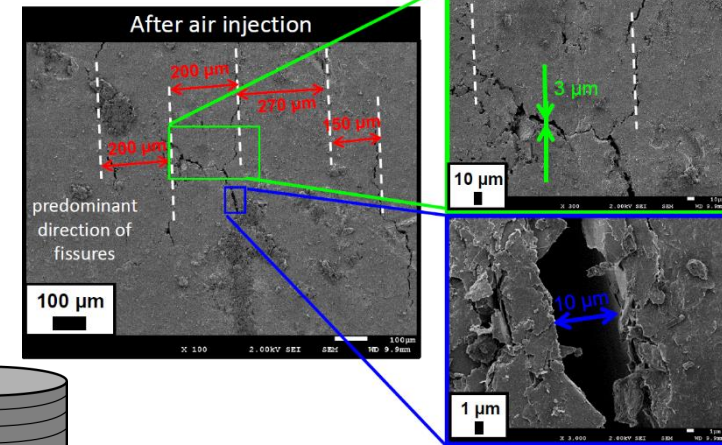
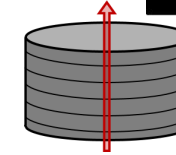
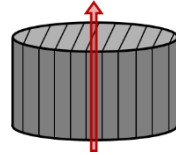
# Gas injection experiment

Fracture aperture

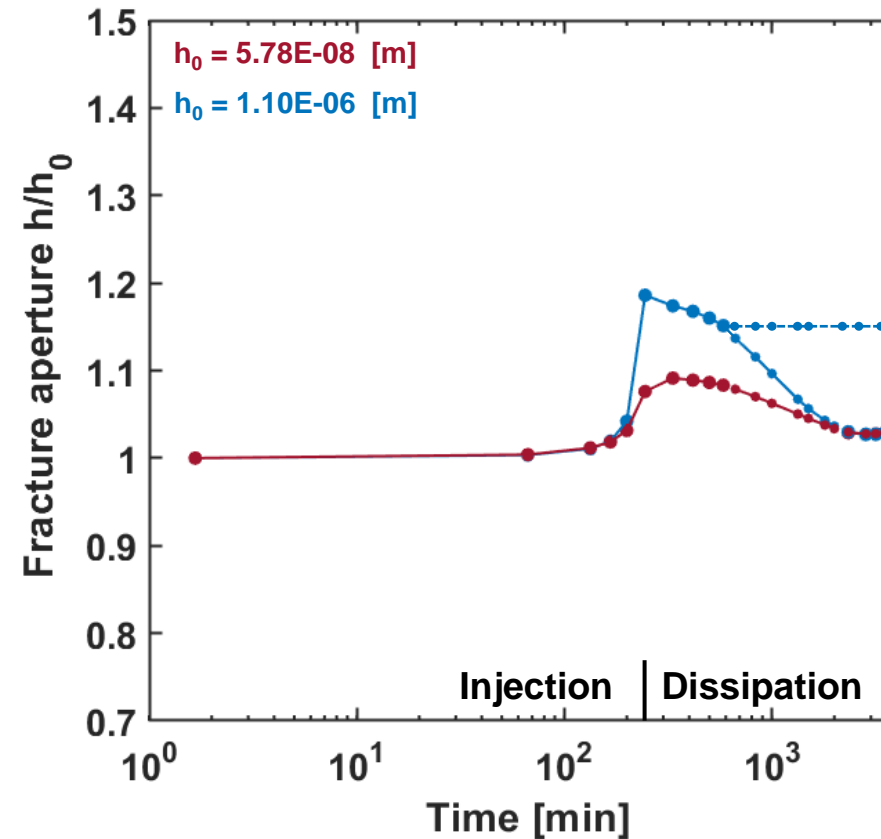
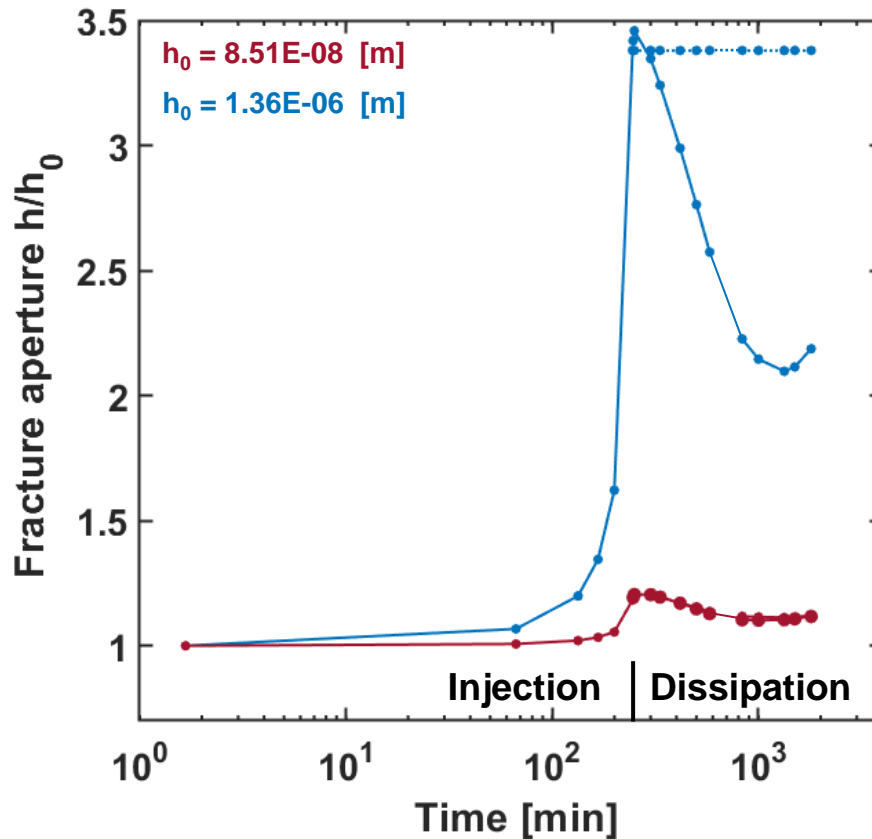
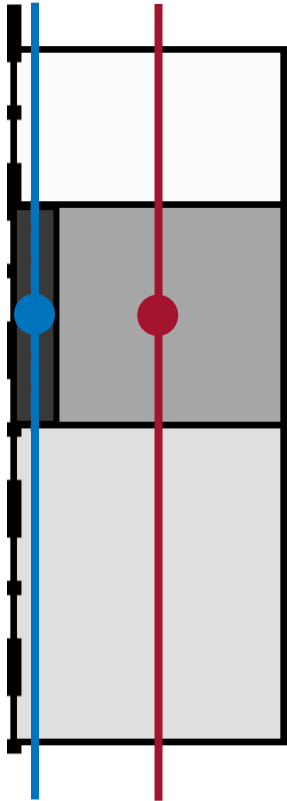


# Gas injection experiment

Fracture aperture

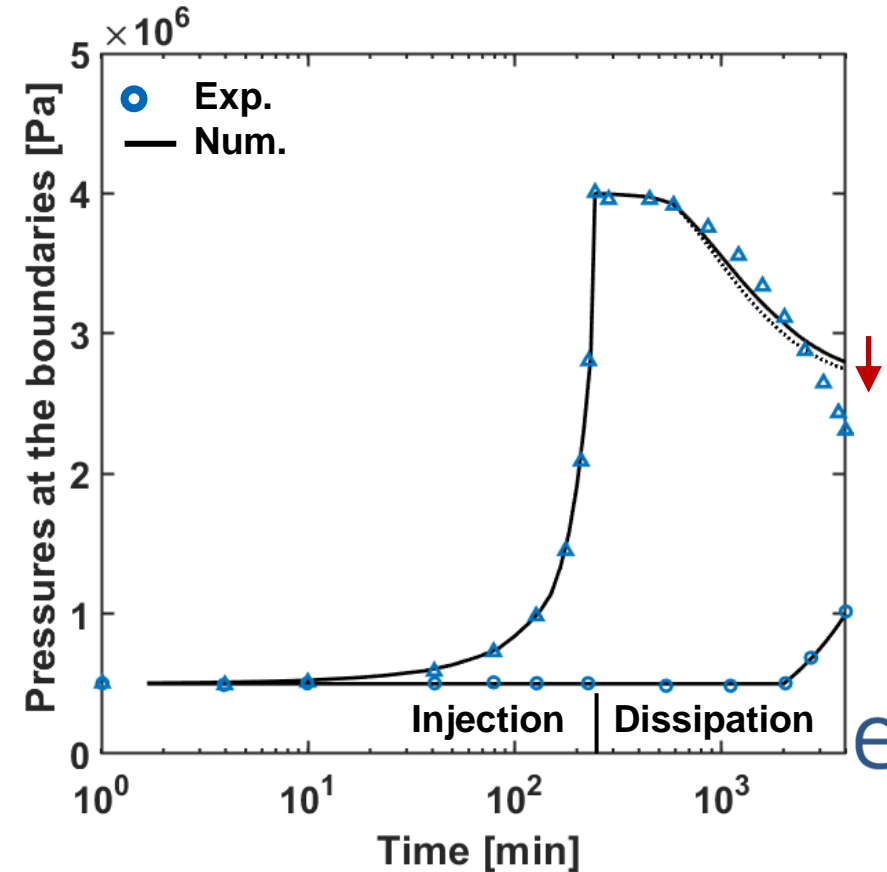
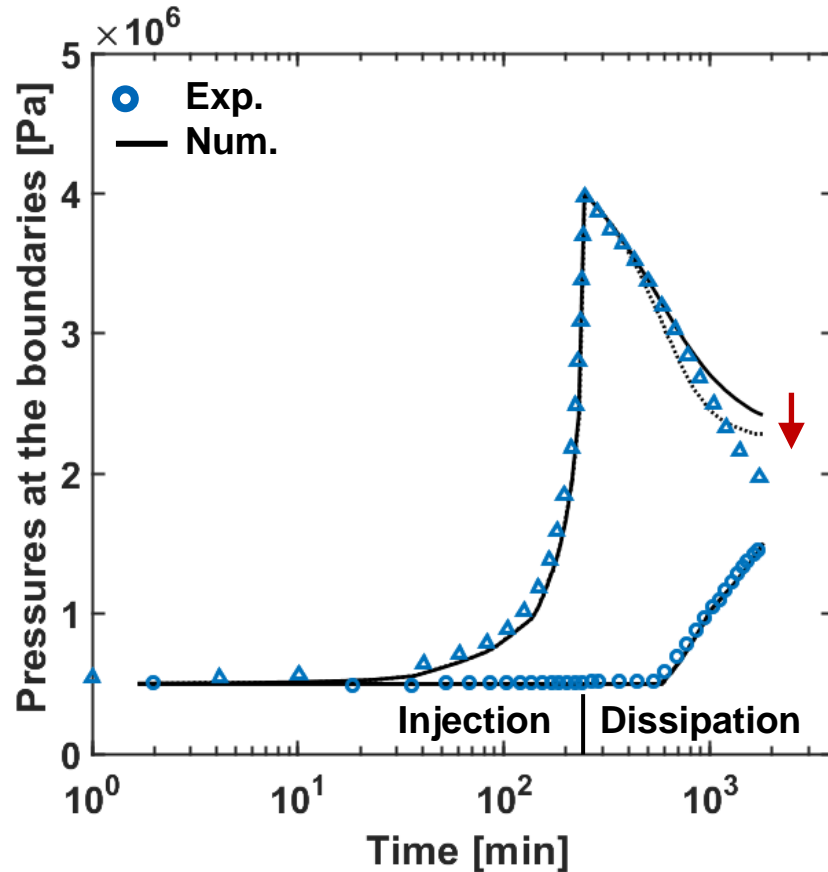
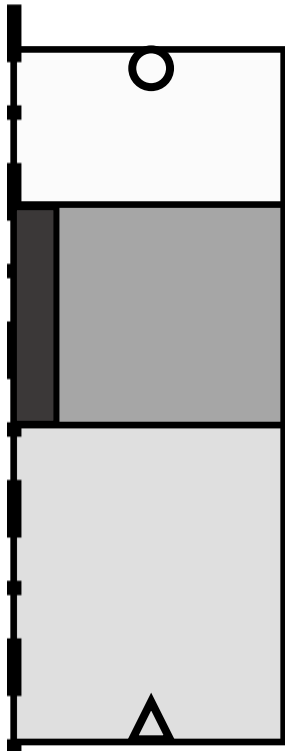
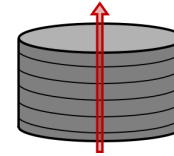
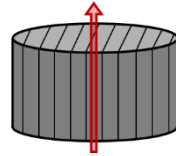


Experimental observations:  
Opened fractures after injection  
*Gonzalez-Blanco & Romero (2022)*



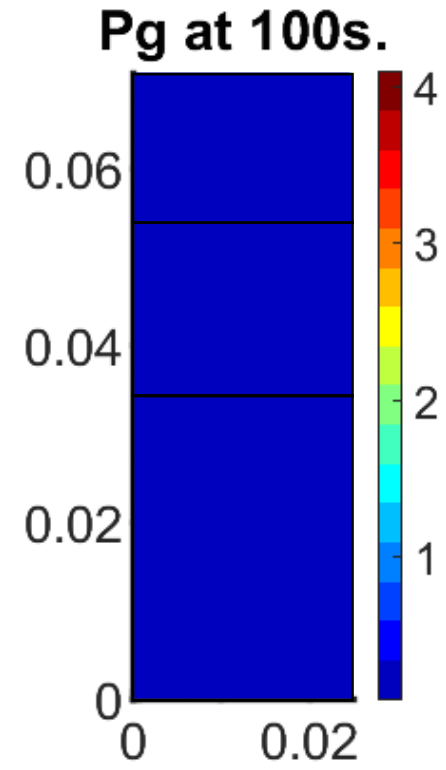
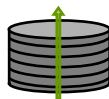
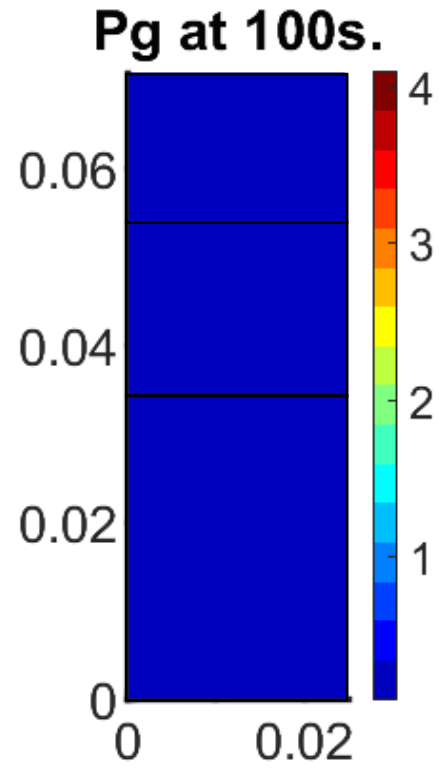
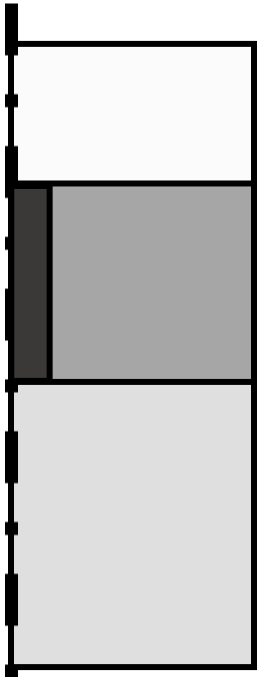
# Gas injection experiment

Injection and recovery pressures



# Gas injection experiment

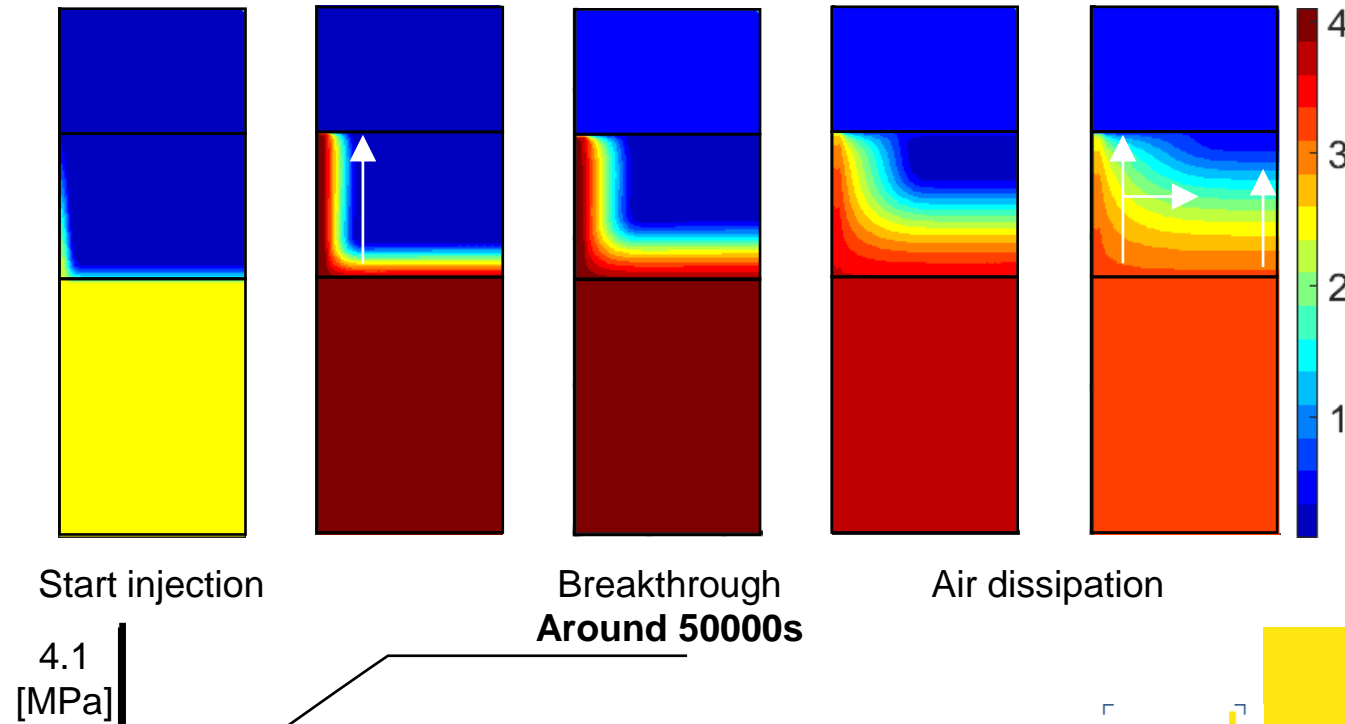
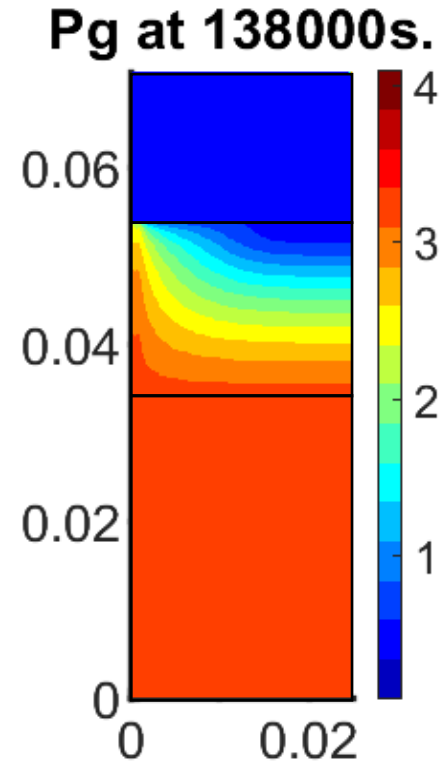
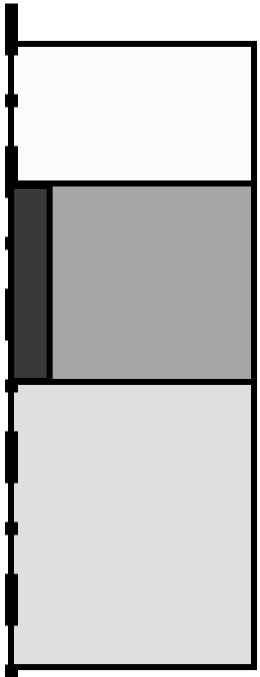
Injection and recovery pressures





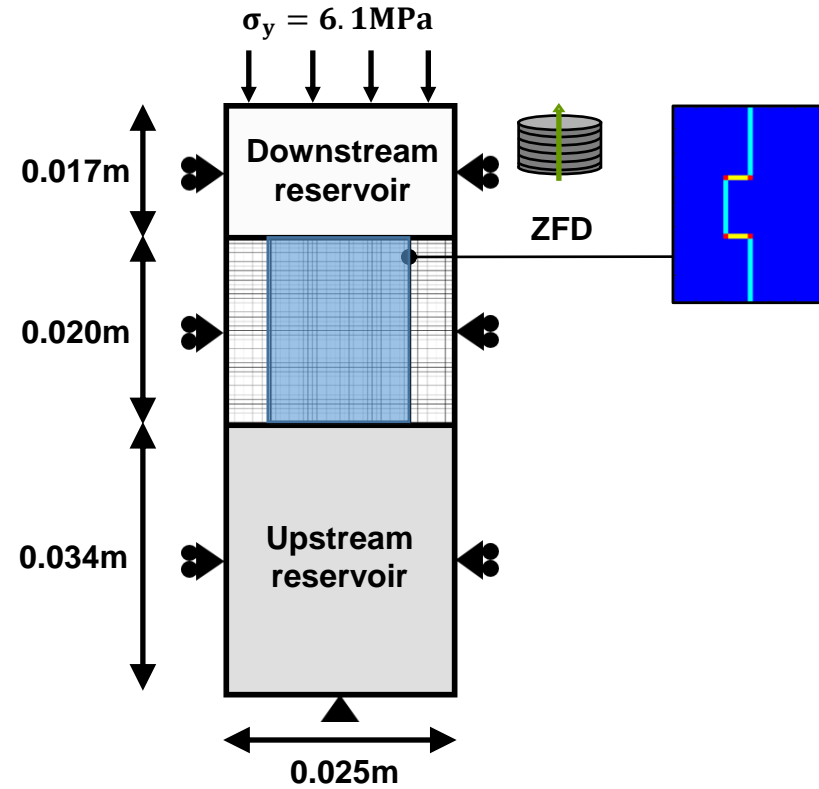
# Gas injection experiment

## Injection and recovery pressures

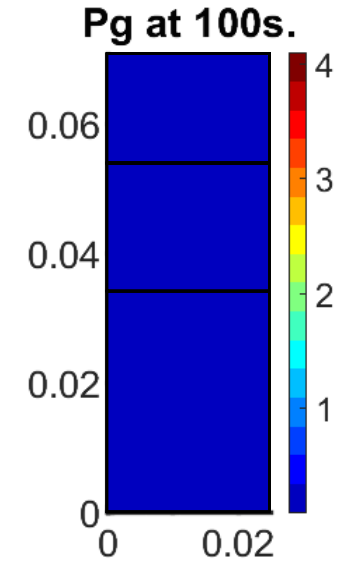


# Gas injection experiment

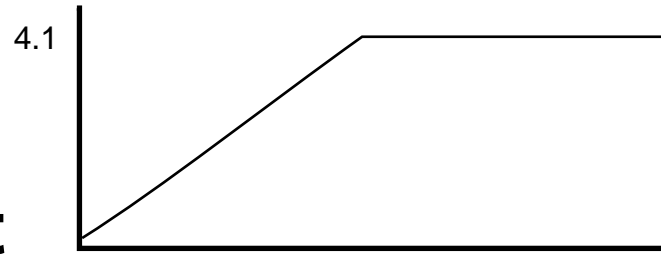
Effect of the connectivity of the planes



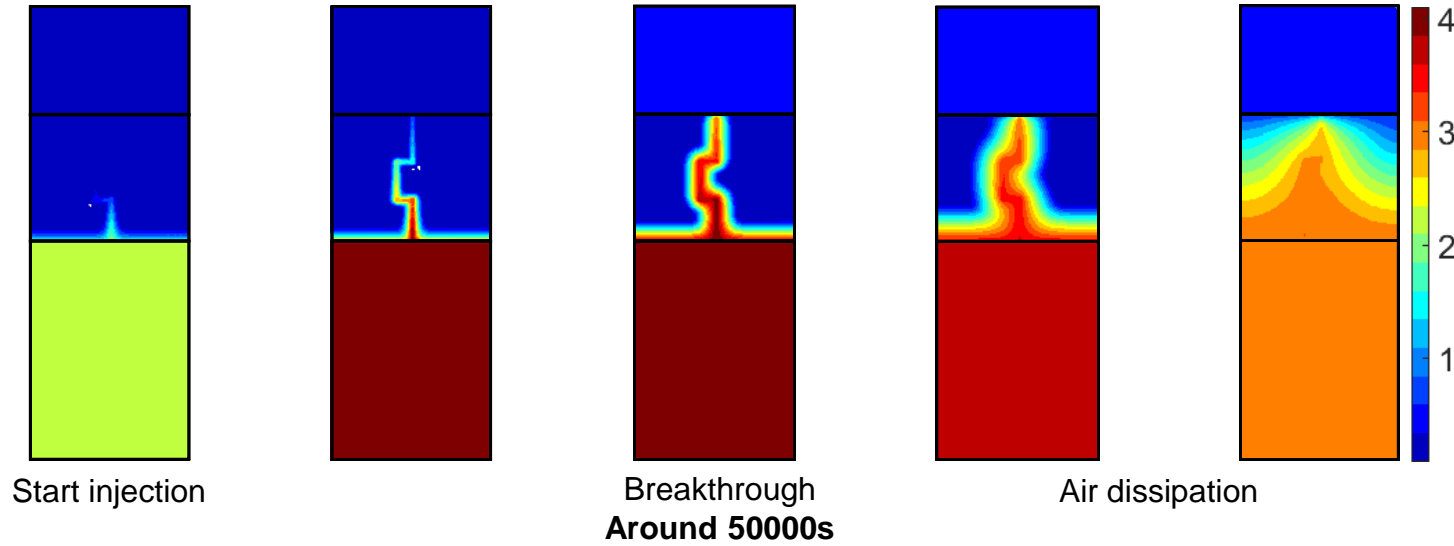
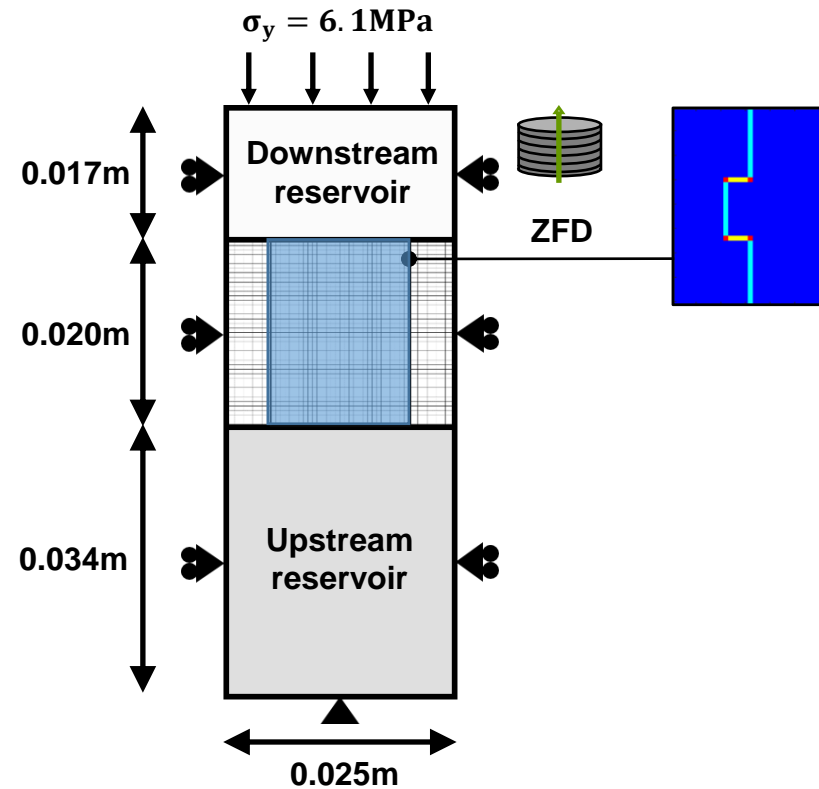
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes



# Gas injection experiment

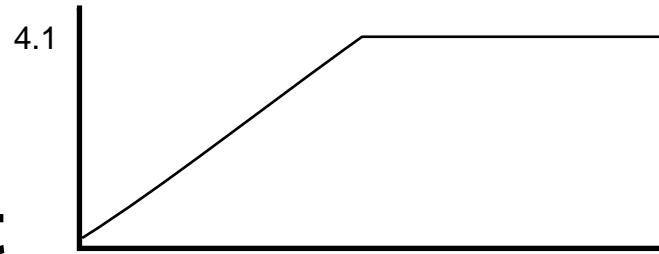


Effect of the connectivity of the planes

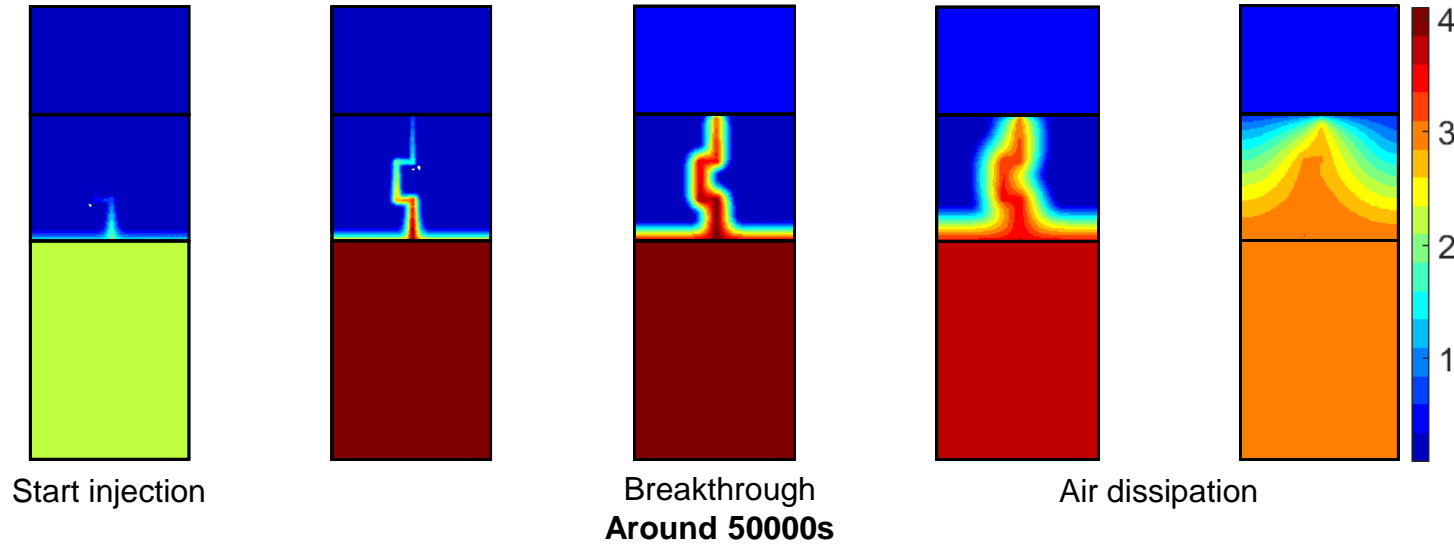
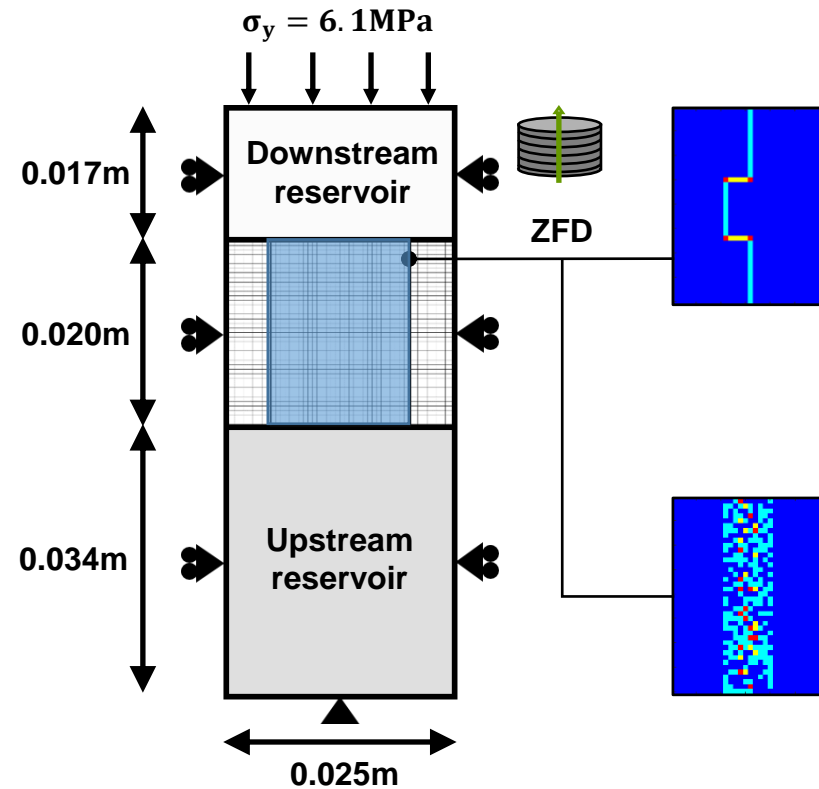


- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

# Gas injection experiment

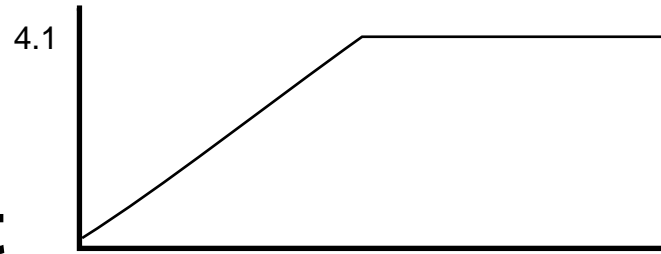


## Effect of the connectivity of the planes

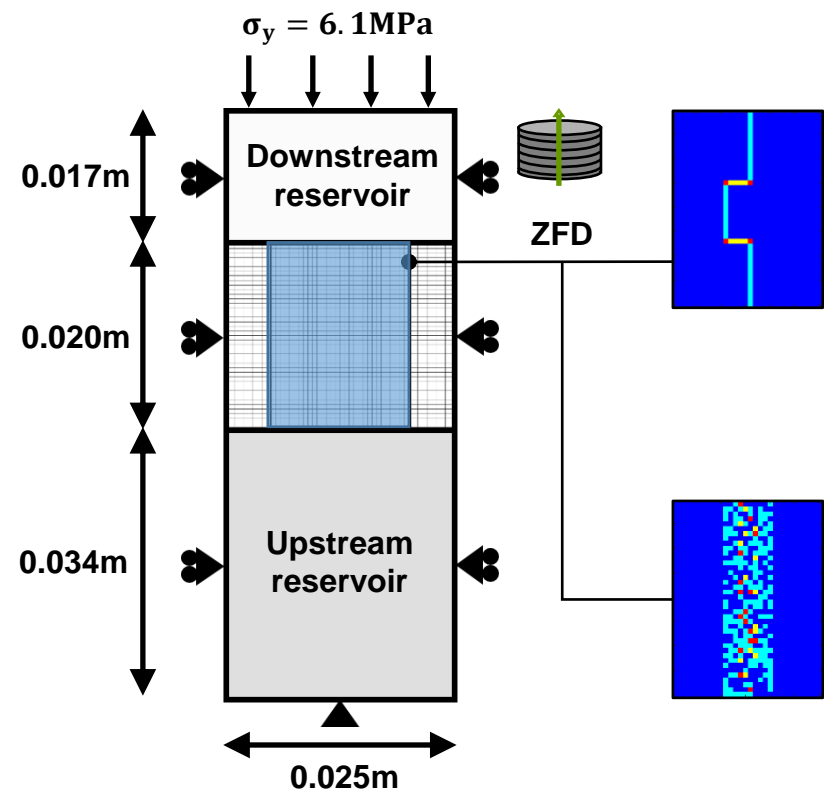


- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

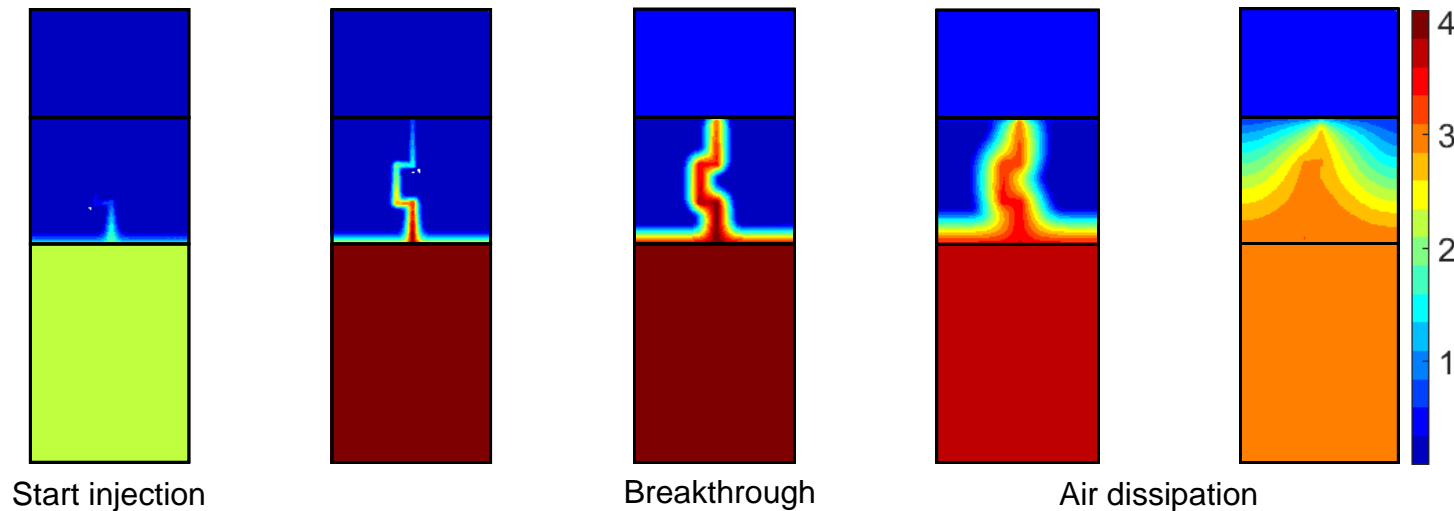
# Gas injection experiment



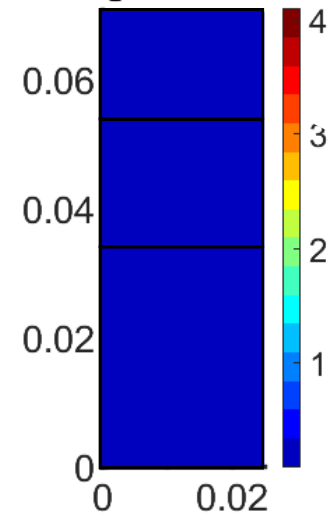
Effect of the connectivity of the planes



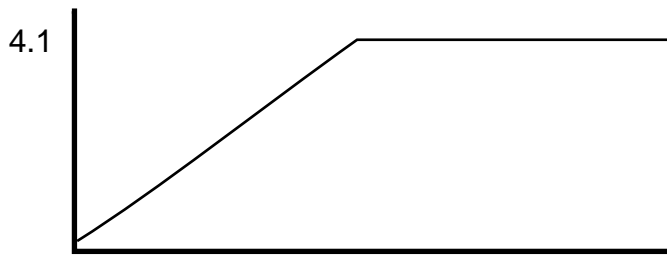
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes



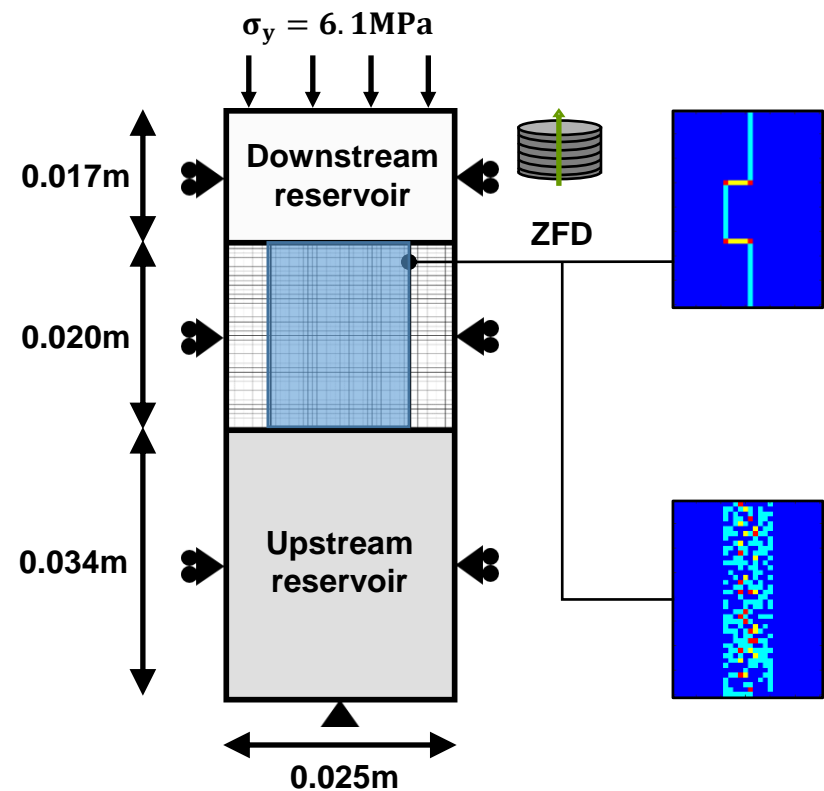
**Pg at 100s.**



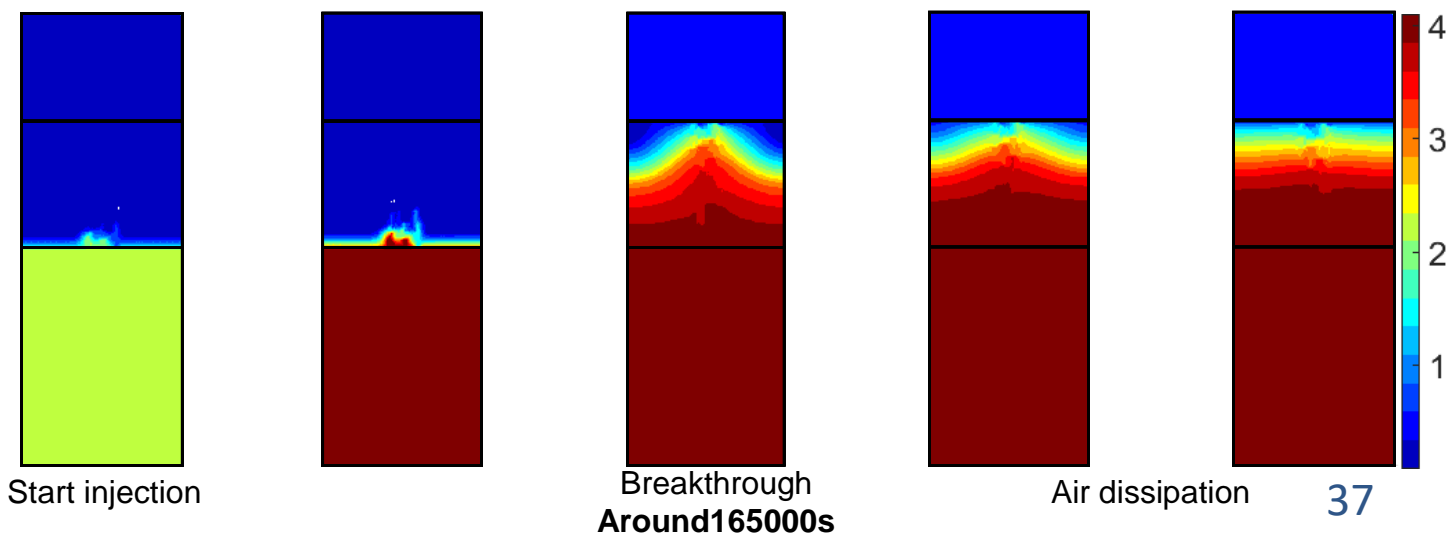
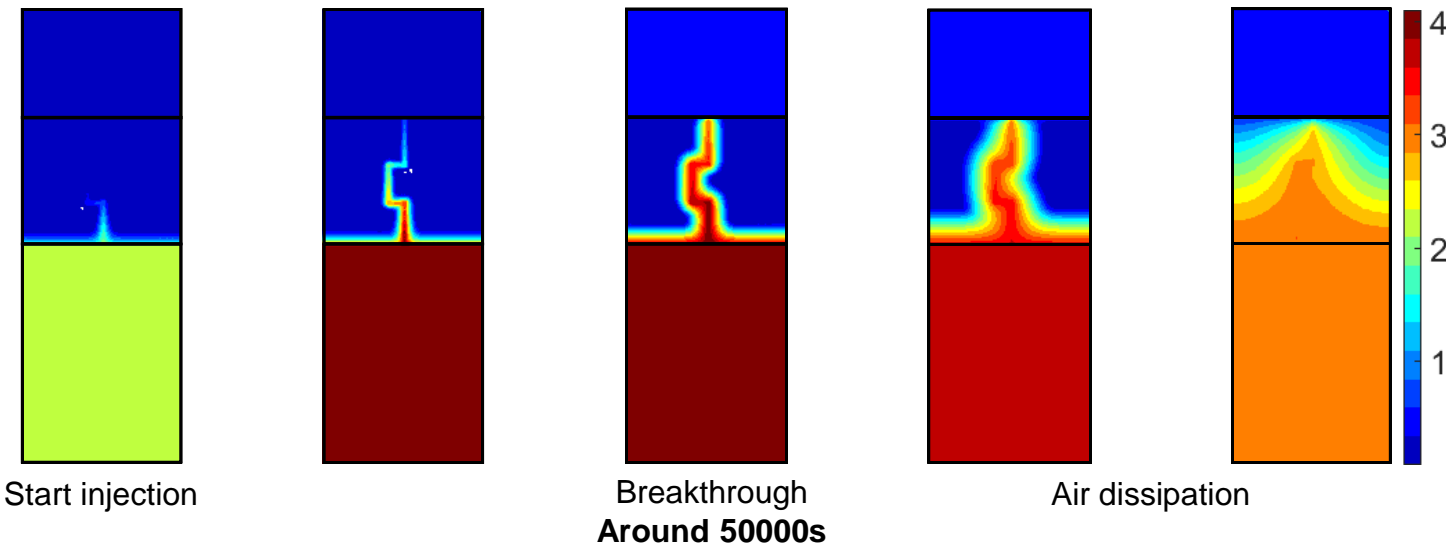
# Gas injection experiment



## Effect of the connectivity of the planes

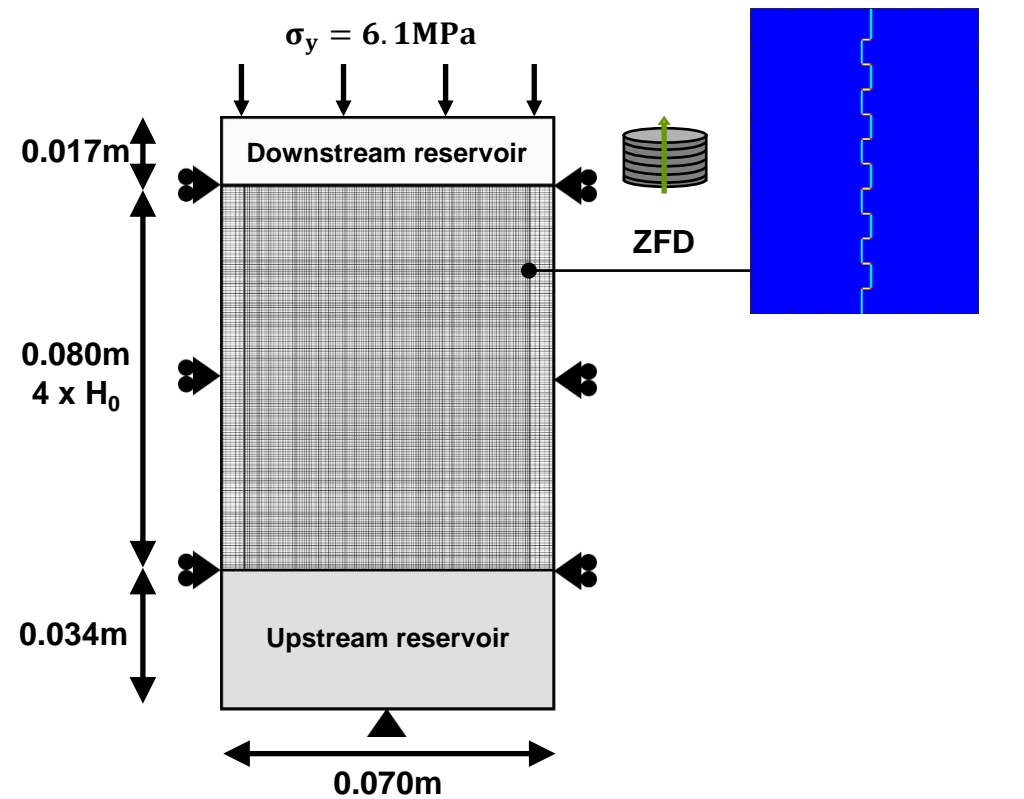


- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
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# Gas injection experiment

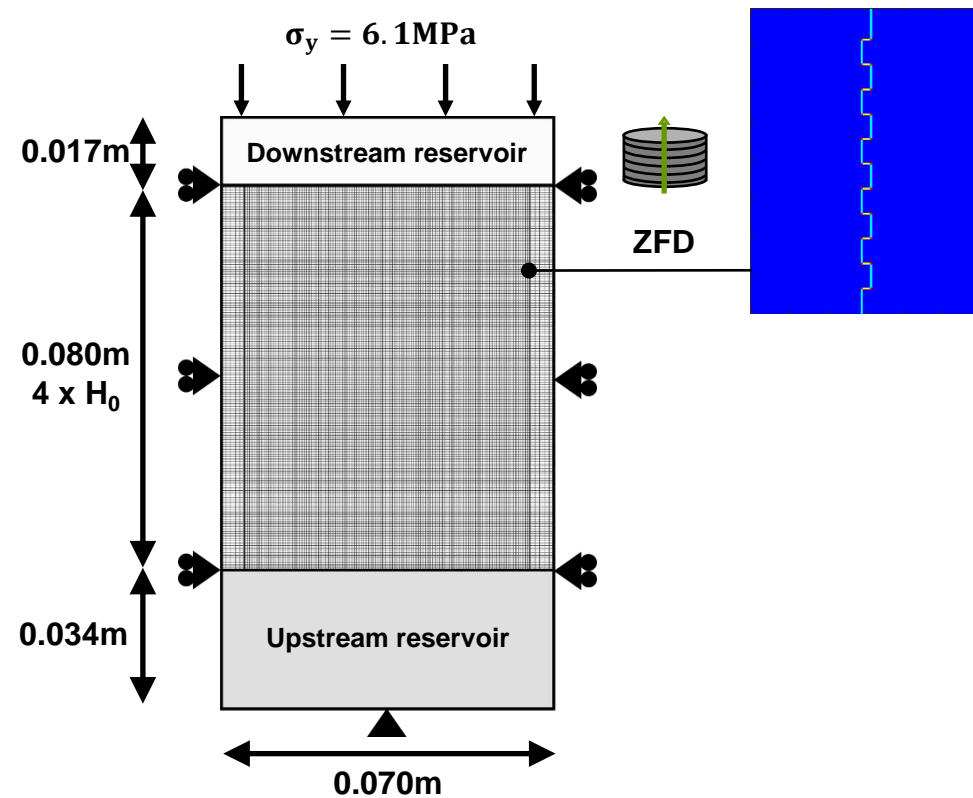
Effect of the connectivity of the planes under up-scaling



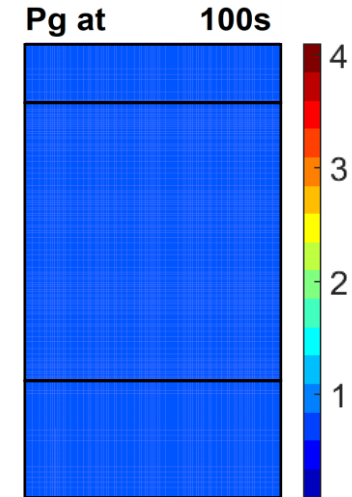
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

# Gas injection experiment

Effect of the connectivity of the planes under up-scaling



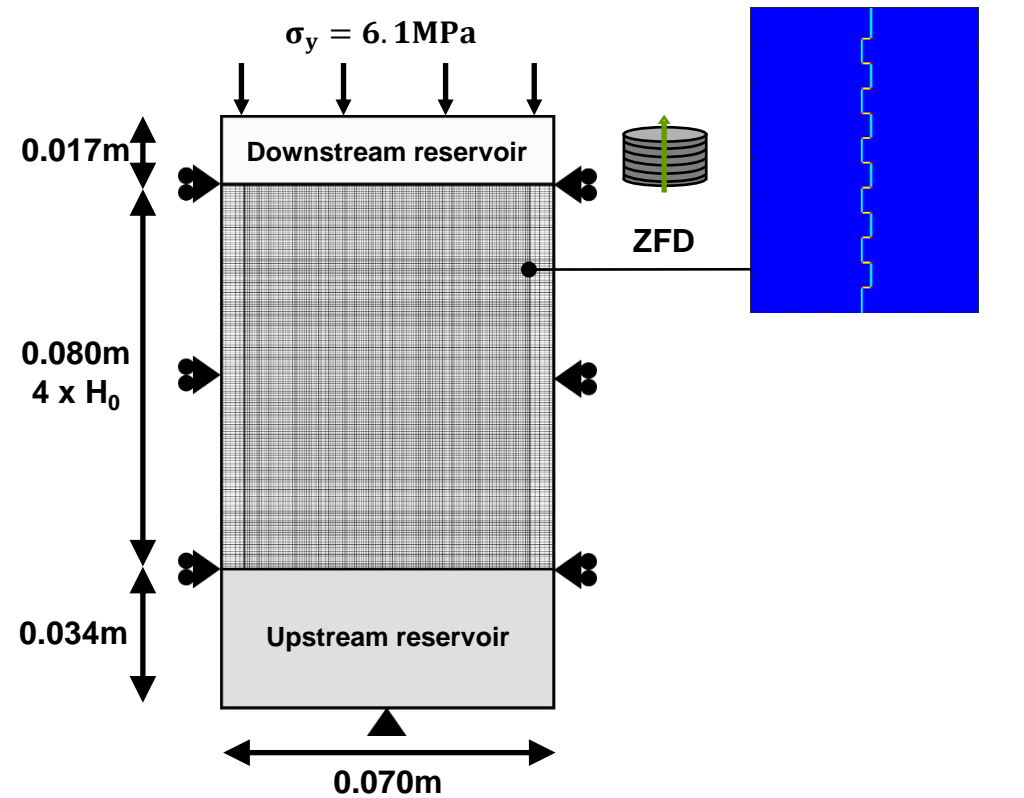
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes





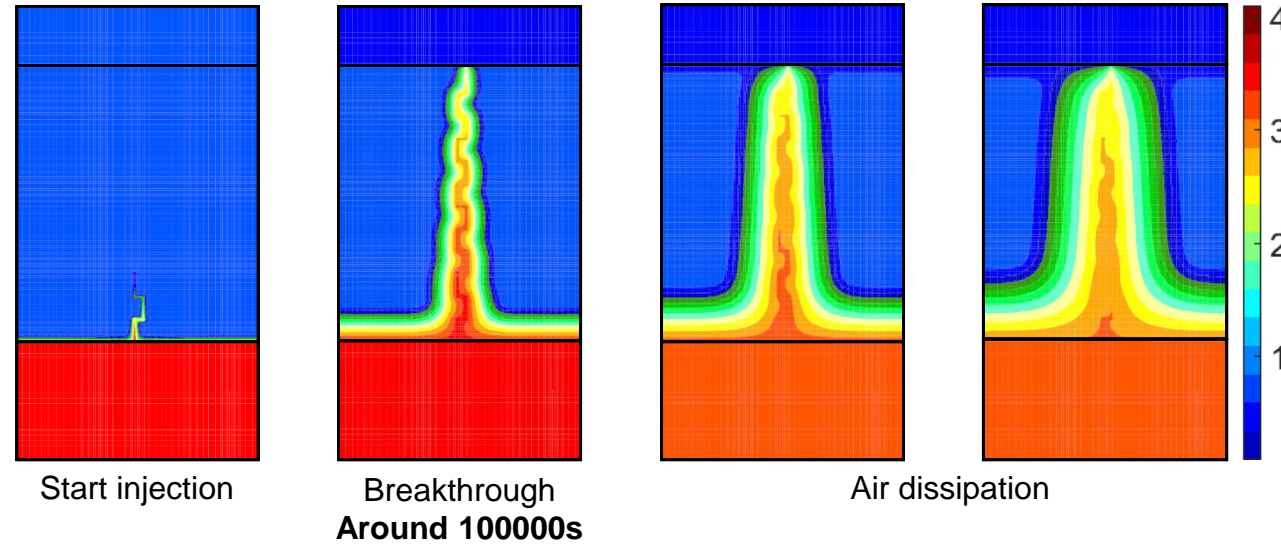
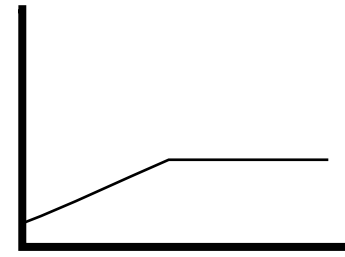
# Gas injection experiment

Effect of the connectivity of the planes under up-scaling



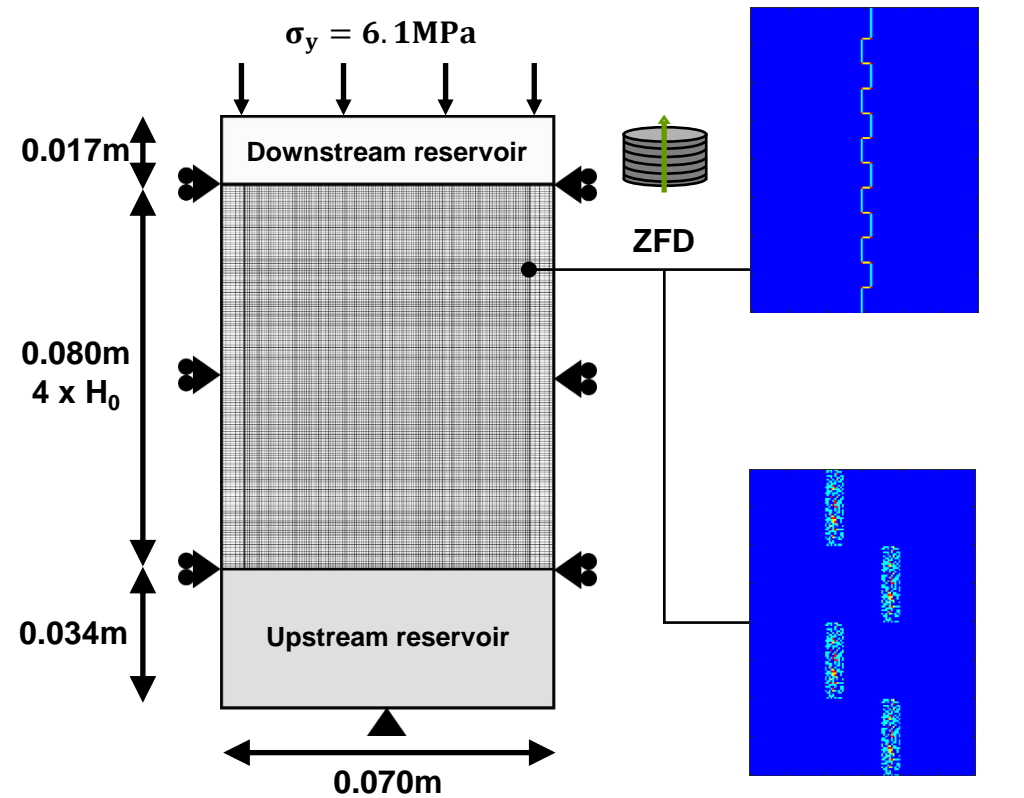
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

4.1



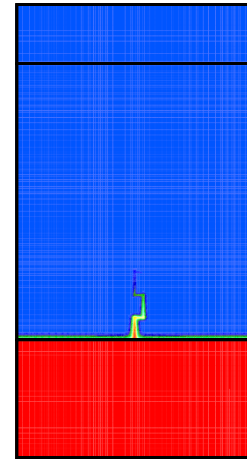
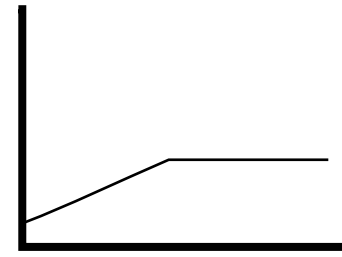
# Gas injection experiment

Effect of the connectivity of the planes under up-scaling

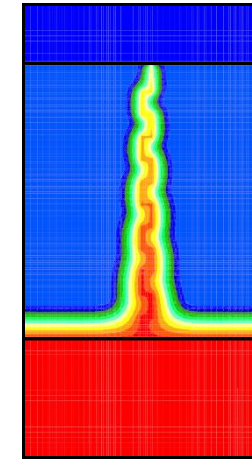


- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

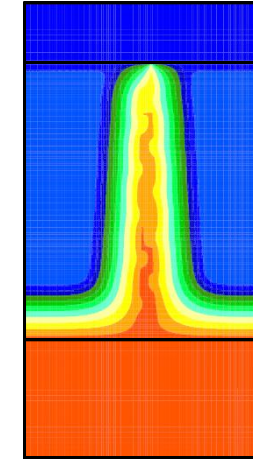
4.1



Start injection



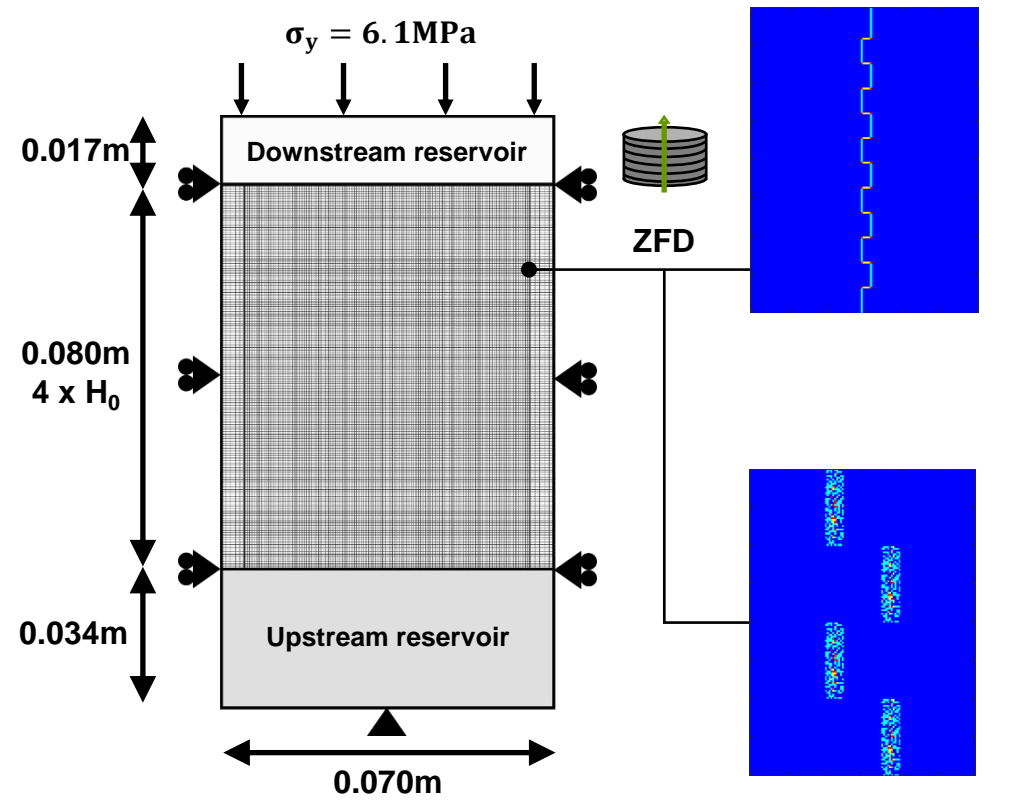
Breakthrough  
Around 100000s



Air dissipation

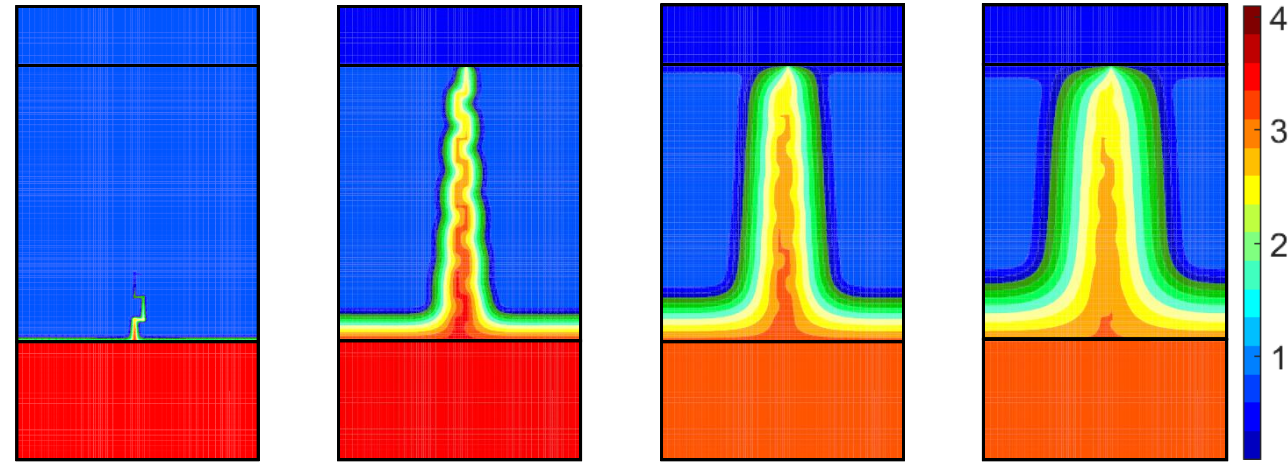
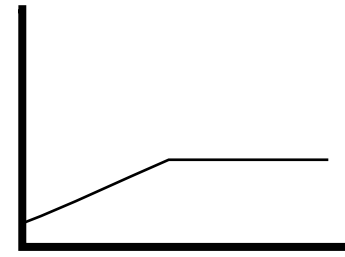
# Gas injection experiment

Effect of the connectivity of the planes under up-scaling



- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes

4.1

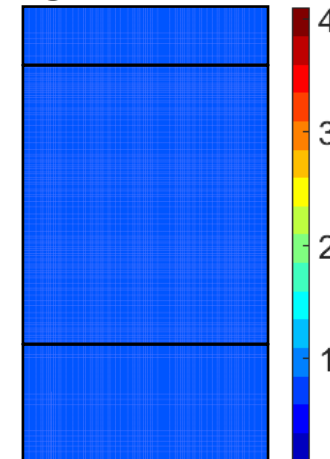


Start injection

Breakthrough  
Around 100000s

Air dissipation

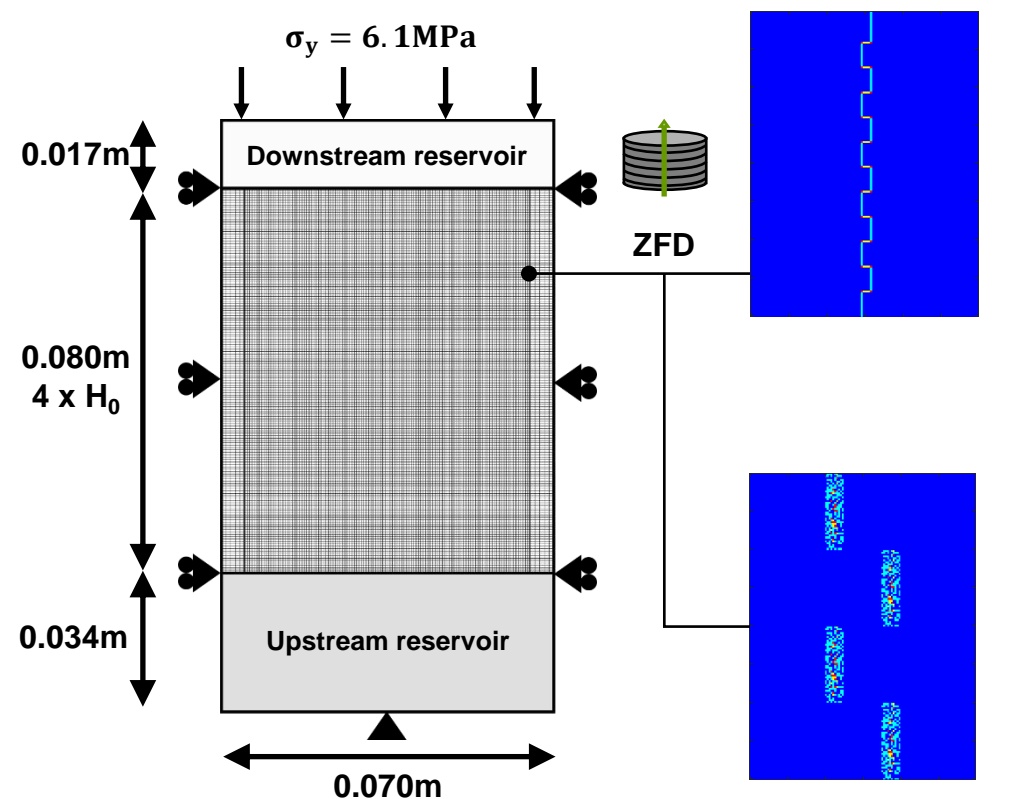
Pg at 100s



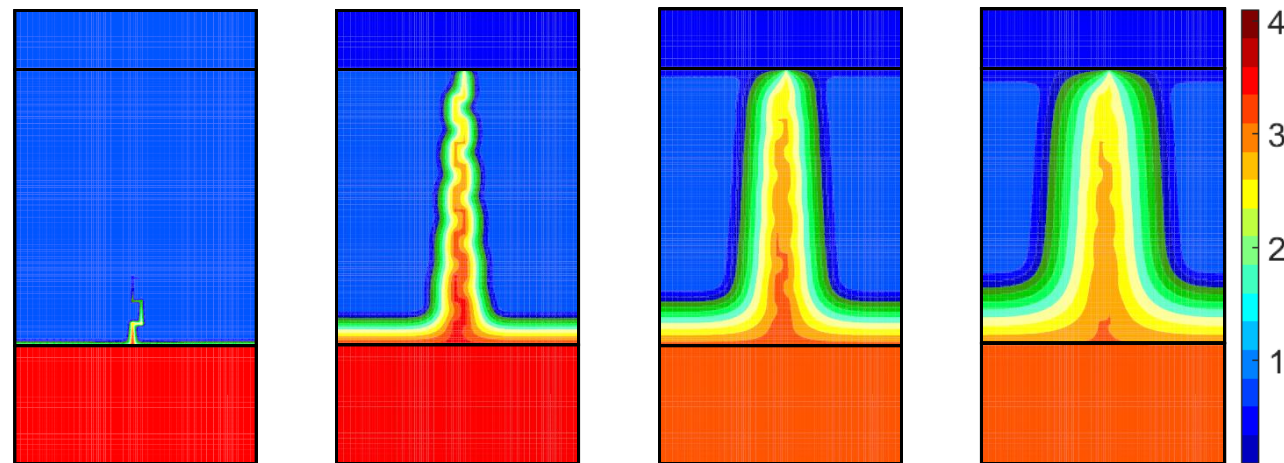
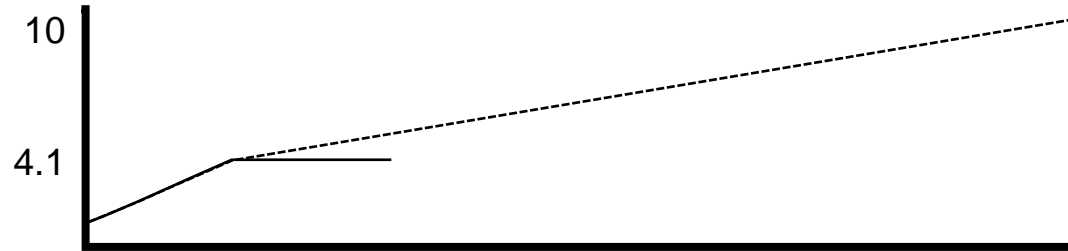


# Gas injection experiment

Effect of the connectivity of the planes under up-scaling



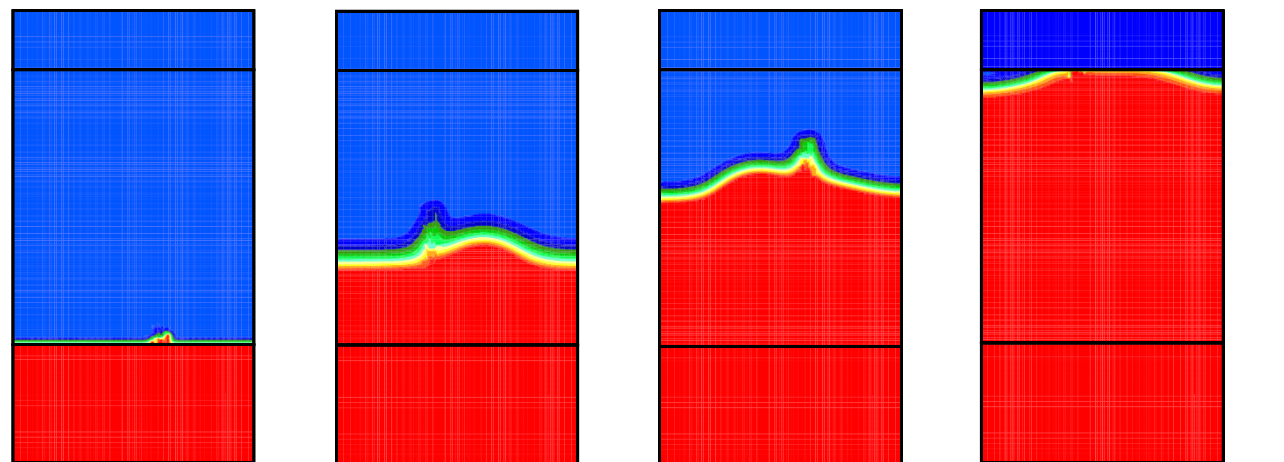
- Undisturbed Boom Clay
- Disturbed bridging planes
- Disturbed bedding and bridging planes
- Disturbed bedding planes



Start injection

Breakthrough  
Around 100000s

Air dissipation



Start injection

Breakthrough  
Around 325000s



# Content

- ① Context
- ② From experimental evidence to modelling
- ③ Multi-scale modelling approach
- ④ Preliminary modelling
- ⑤ Modelling gas injection experiment
- ⑥ Conclusions

# Conclusions

We **developed** a multi-scale model able to

1. Simply idealise the microstructure of the rock with fractures and tubes
2. Reproduce mechanisms inherent to gas migrations in sound rock layers

We **showed** that

1. Macro-pores, bedding planes and bridging planes play different roles in gas flows
2. Preferential flow paths can be generated through fractures with weaker properties
3. Different gas mechanisms occur in the presence of weaker bridging planes



Alert Geomaterials



# Advanced multiphysics of geomaterials: multiscale approaches and heterogeneities

ALERT OZ / EURAD GAS & HITEC Summer School  
28 August – 01 September 2023 • Liège (Belgium)

Pierre BÉSUELLE, Frédéric COLLIN,  
Anne-Catherine DIEUDONNÉ, Sebastia OLIVELLA



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